

# Using Options to Buy Stocks Build Wealth with Little Risk and No Capital 

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## PREFACE

There comes a time in the life of every investor when he or she runs out of money to invest: the birth of a baby, purchase of a home, a second child, braces, another baby (oops!), and, later on, tuition payments, wedding expenses, a second home. All of these can temporarily suspend regular investment plans. Permanent crimps in investing can arise when retirement plans are fully funded or retirement itself commences.
Professionals and nonprofessionals alike are subject to the laws of supply and demand, and can find themselves at times between jobs, underemployed, or just plain out of work. These things happen to us all, and for most, the idea of maintaining regular investment plans during such tribulations seems impossible. Where will the money come from?

I have been a regular investor for over three decades, faithfully putting aside the dollars needed for retirement and stuffing them into stocks, bonds, and mutual funds. Imagine my surprise the day my financial adviser informed me that my retirement plan was now fully funded. This was a good-news/bad-news situation. The good news was that I would now be able to retire at 60 percent of my peak earnings for the rest of my life. The bad news was that as a compulsive saver and avid investor, I would no longer be able to contribute new capital with which to play the market, either for the purpose of buying new issues or for acquiring additional shares of my favorite companies. I could sell existing equities to do such things, but as an inveterate "buy-and-hold" investor, I was loath to trade in any of my equity holdings.

My need to continue my investment program beyond what I was legally permitted to contribute to my retirement plan was driven by four concerns:

1. What will happen if I outlive what the actuarial tables said were going to be my golden years?
2. Will there be enough in my retirement plan so I can spoil my grandchildren while I am still alive, yet leave enough in my estate for my wife, my children, and (alas) the cut due the Internal Revenue Service?
3. I knew I would miss the research, discussions, evaluations, and decision making that go into the selection and buying of stocks.
4. And, hey, the difference between being an old man and an elderly gentleman is money.

The first strategy that occurred to me for continuing my investment program was to go on margin. Most brokers will lend you up to 50 percent of the value of your account to buy more stocks. The trouble with this method is that you have to repay these funds with interest. The interest rate is high-often higher than what can be safely earned on bonds, preferred stock, and even the appreciation on many growth stocks. Furthermore, the specter of a dreaded margin call because of a market slump, however temporary, made me (as it does most investors) very leery.

It then occurred to me that there is a great way to acquire stocks without trading what you've got or using borrowed funds. Simply stated, the method involves selling longterm options on highly rated companies and using the premiums received to further your investment program. There is no interest paid on the funds received; the funds never have to be repaid (because they have not been borrowed); and the equity requirements needed to do this are much lower than those for regular margin buying. Although I adapted and perfected this technique to suit my own needs and situation, it can be used by any investor who has built up some measure of equity and would like to acquire additional stocks without contributing additional capital. As you will see later, the potential benefits far outweigh any incremental risks, especially when appropriate hedges and proper safeguards are incorporated.

What makes this technique so effective is that it exploits the fact that option prices do not reflect the expected long-term growth rates of the underlying equities. The reason for this is that standard option pricing formulas, used by option traders everywhere, do not incorporate this variable. With short-term options, this doesn't matter. With long-term options, however, this oversight often leads the market to over-
value premiums. Taking advantage of this mispricing is the foundation of my strategy.
I have been using this technique for the past five years-very cautiously at first because of the newness of these long-term options (they were invented in 1990) and the almost complete lack of information regarding their safety and potential. It was this lack of analysis that led me to start my own research into the realm of long-term equity options. Having determined their relative risk/reward ratio, I am now very comfortable generating several thousand dollars a month in premiums that I use to add to my stock positions. I am often told that what I am doing is akin to what a fire or hazard insurance company does, generating premiums and paying claims as they arise. A better analogy might be to a title insurance company because with proper research, claims should rarely occur.

This book is divided into four sections: The first one consists of Chapters 1 through 5 and describes the basic approach in using long-term options to further investment programs. The second section, Chapters 6 through 12, refines this approach and shows how to institute controls to reduce risk. The potential reward and the long-term safety of the basic approach and refinements are established through extensive computer simulation and backtesting. This is accomplished by going back ten years and asking what would have been the outcome if the various techniques had been applied in as consistent a manner as possible during that period.

The third section, Chapters 13 through 15, contains the analytic formulas for the rapid computation of volatility and option premiums for both European- and American-style options. The 1997 Nobel prize in economics was awarded to Myron Scholes and Robert Merton, who along with Fischer Black were the original developers of these formulas. With minor variations, they are still used today for calculating option premiums by market makers and option traders alike. Although college mathematics is needed to understand the formulas, the short, simple algorithms given for their numerical evaluation can be used by virtually anyone who knows BASIC or can set up a spreadsheet on a personal computer. For readers without access to computer tools, there are various appendices containing tables for looking up option premiums and assignment probabilities.

Finally, Chapters 16 and 17 contain suggested resources for additional information, including Internet Web sites and capsule reviews of introductory, intermediate, and advanced books on options.

The methods developed in this book are based on my three decades of investing in real estate and the equities market, plus the modeling experience gained through the development of analytic, decision-making tools for various agencies of the federal government and numerous trade associations, research institutes, and private-sector clients. My first book, Decision Making in Federal Real Estate: How the Government Decides Whether and with Whom to Buy, Build or Lease, remains the classic in its field.

I wish to thank the various investment analysts and members of the brokerage industry for their insightful comments and suggestions. These include Ed Elfenbein, publisher of the Microcap Stock Digest, who reviewed and edited the first version of the book, Buying Stocks without Money, and Charlie Meyers, senior vice president for investments at Legg Mason Wood Walker, Inc., who introduced me to the world of options. Special thanks to Cynthia Zigmund, editorial director at Dearborn Financial Publishing, Inc., for her help in bringing this project to fruition. I am particularly grateful to the numerous investors like myself that I have met in investment chat rooms on America Online. I know them only by their Internet screen names, but their collective insights into the stock and options markets added much to my own knowledge. More than that, I found the instant feedback of such interactions to be invaluable as I bounced new ideas off a jury of my peers and refined my own thoughts in the process. Finally, I owe special thanks to my wife, Doris, for the encouragement she provided and sacrifices she made to keep me at this task until the job was done.

## PART ONE-

THE BASIC APPROACH

## 1-

## Introduction

## What Is an Option?

Although options are typically bought and sold through security dealers and brokers, it is important to understand that options are not securities. Unlike stocks, warrants, or corporate bonds, options are not authorized or issued by any company on its behalf. Rather, an option is simply a contract between two parties, a buyer and a seller. The buyer is often referred to as the owner or option holder, and the seller is often referred to as the option writer. A call option gives the option holder the right to buy an asset at a set price within a certain time, while a put option gives the option holder the right to sell an asset at a set price within a certain time. In neither case is the option holder ever obligated to buy or sell.

For an example of an option contract, suppose you're in the market for a new car. Sitting there in the dealer's showroom is that spectacular model you'd love to own. Because it is popular, there is little discount from the sticker price of $\$ 40,000$. You tell the salesman that you get your bonus in three months. Anxious to make a deal, he says, "Okay, the price may well go up between now and then, but if you give us a nonrefundable check for $\$ 250$ today, I'll guarantee that price for the next 90 days. Not only that, but if the price goes down, you can back out of the deal." This sounds good to you, so you write the dealer a check for $\$ 250$. Congratulations! You have just entered into a bona fide option contract.

Why did this seem like a good idea to you? By the terms of the deal, no matter how high the sticker price goes in the next 90 days, your effective purchase price will be $\$ 40,250$, which includes the $\$ 250$ premium you paid. If the sticker price increased by 10 percent, to $\$ 44,000$, you would be $\$ 3,750$ ahead of the game. On the other hand, if the sticker price dropped to $\$ 39,000$ (and such things can happen), your effective price would be $\$ 39,250$. This is because by the terms of the deal you are not obligated to buy the car for $\$ 40,000$ and are free to buy it from that dealership or anywhere else at the market price of $\$ 39,000$. In that situation, you would still be $\$ 750$ better off than if you had purchased the car for $\$ 40,000$ today.

But that's not all. After writing that check for $\$ 250$, you are asked by the salesman if you would like to buy "lemon" insurance. "What's that?" you ask. "Well," says the salesman, "for just $\$ 100$ more, I will give you the privilege of selling the car back to me at whatever price you paid for it within 30 days of purchase, no questions asked." This too sounds good, and you write the dealer a check for another $\$ 100$. Congratulations again. You have just entered into your second option contract of the day.

The first option contract is a classic example of a call option because it gives you the right, but not the obligation, to buy the car. The second option contract is a classic example of a put option because it gives you the right, but not the obligation, to sell (i.e., put back) the car to the dealership. Notice that when used in this manner, both option contracts served to reduce risk. The call option protects you against an unanticipated price increase, and the put option protects you against buying a lemon. You may not realize it at first, but the second option also protects you against a significant price decrease right after buying the car. If the price did drop to $\$ 39,000$ within 30 days of buying the car for $\$ 40,000$, you could return the car to the dealer, get your money back, and buy an equivalent new one for $\$ 39,000$. (In practice, the dealership would likely refund the difference in cash-which is just as good as far as you're concerned.)

Whether it entailed a call or a put, the option involved was essentially characterized by three principal variables: (1) the buy/sell price of the underlying asset (the car), (2) the time period during which the option could be exercised (30 or 90 days), and (3) the premium involved
( $\$ 100$ or $\$ 250$ ). One other important feature of at least the call option in this case is that it is likely transferable. If you decided not to buy the car within the 90 -day period, you could have sold the option to a friend for whatever price the two of you agreed on. If the sticker price increased to $\$ 44,000$, that right to buy the car for $\$ 40,000$ would be worth more than the $\$ 250$ you originally paid for it. On the other hand, if the price decreased or remained the same, the value of the right to buy the car for $\$ 40,000$ would have shrunk to zero by the time the 90-day period expired.

Option contracts in which the underlying assets are corporate stocks do not differ in principle from the ones described above and are also characterized by the buy/sell price of the underlying asset (the stock), the period during which the option can be exercised, and the premium involved. The difference is that in the case of investment assets, option contracts are used for a much wider range of purposes, including risk reduction, profit enhancement, and leveraged control.

People often use option contracts to decrease the risk associated with stock ownership. Suppose you own 100 shares of Intel and want to protect yourself against a significant drop in value. Wouldn't it be nice to have someone else contractually promise to buy those shares from you for a guaranteed amount no matter what, even if the price fell to zero? That person will want a reasonable fee for providing that assurance, of course. As with fire or auto insurance, you hope never to file a claim. But if loss did occur because a house collapsed (or stock plummeted), financial disaster can be averted or substantially mitigated, depending on the terms of the policy and extent of the coverage elected. In this situation, an option contract is the exact analog of an insurance policy.

Another reason people use options is to enhance portfolio income. Those 100 shares of Intel you own are probably not paying a dividend worth writing home about. For a reasonable fee, you might grant someone else the right to purchase those 100 shares from you, within a specified period, at a price pegged above today's market value. Real estate operators and landowners do this all the time, offering tenants or developers the right to purchase property at a specified price by some future date in return for an up-front cash payment. If the right to purchase is exercised, it means the owner got his or her price. If the right to pur-
chase expires without exercise, the extra cash augments whatever rental payments are being received - thereby increasing the effective yield rate. In either event, the up-front payment is retained by the property owner.

The third reason people use options is to control a large amount of stock without having to buy or own it. Suppose an investor feels that Intel (or any other stock) is about to rise significantly in price. Wouldn't it be nice to pay a current owner of that stock a reasonable fee for the right to purchase his or her shares at a mutually agreed on price within a certain period? In this situation, the potential purchaser is the exact analog of the real estate developer in the previous example who seeks to control a potential project without committing valuable cash resources until market conditions warrant.

Investors who believe a stock is about to "tank" also enter into option contracts for the right to sell a stock within a specified period a price reflecting its current value. This transaction is simpler and requires much less cash than taking on the potentially unlimited risk associated with short selling. (A short sale occurs when the investor borrows shares of a stock and sells them in the hope that they can be subsequently purchased back at a lower price and then returned to the original shareholder. Substantial collateral is required and numerous technical conditions must be met to conduct short sales.)

## Features of Standardized Equity Options

If every component and clause had to be negotiated each time an option contract was set up, the options market would grind to a halt. To maintain a rapid but orderly options market, option contracts are assigned six standard parameters:

## 1. Product

2. Type
3. Unit of trade
4. Strike price
5. Expiration date
6. Style

## Product.

Options are distinguished by the underlying product involved: If the underlying product is one of several market indexes, such as Standard \& Poor's 100 (S\&P 100), the option is called an index option. If the underlying product involves common stock, it is called an equity option. In addition to index and equity options, options are now available on interest rates, Treasury securities, commodities, and futures. This book will deal exclusively with equity options.

## Type.

Options are also classified by the type of privilege (either buying or selling) granted the option holder. As you have seen, a call option gives the option holder the right to purchase a specified number of shares, ordinarily 100 , of the underlying security at a specified price at any time within a specified period. In contrast, a put option gives the option holder the right to sell a specified number of shares, ordinarily 100 , of the underlying security at a specified price at any time within a specified period. The price specified in the option contract is referred to as the exercise or strike price, and the last day on which this right to purchase or sell can be exercised is called the expiration date. An example of a call option (or, simply, call) would be the right to buy 100 shares of Intel at $\$ 120$ per share at any time up to and including the third Friday in April. An example of a put option (or, simply, put) would be the right to sell 100 shares of Intel at $\$ 60$ per share during the same period.

Note that the holder of a call does not have to exercise his or her right to purchase. Similarly, the holder of a put does not have to exercise his or her right to sell. This lack of obligation on the part of option holders is one of the major differences between an option and a futures contract. On the other hand, option writers (sellers) are obligated to sell (in the case of call options) or buy (in the case of put options) the agreed-on number of shares at the agreed-on price if the option holder exercises his or her rights within the period specified in the option contract.

## Unit of Trade.

The number of shares specified in an option contract is called the unit of trade. As mentioned earlier, it is ordinarily 100 shares of the underlying equity. In the event of stock splits, mergers, and acquisitions, the unit of trade is adjusted accordingly. For example, when Travelers, Inc., split 4:3 in 1997, the unit of trade for existing option contracts became 133 shares. When 3Com Corporation (COMS)
merged with U.S. Robotics (USRX) that same year, 1.75 shares of COMS were exchanged for each share of USRX; the unit of trade of the existing option contracts on USRX thus became 175 shares of 3Com (with corresponding adjustments in the exercise price). It is even possible for the unit of trade to be less than 100 shares, such as when reverse stock splits occur (wherein a greater number of shares is exchanged for a lesser number of shares of the underlying security).

## Strike Price.

Strike price intervals for standard equity options are set in increments of $\$ 2.50$ when the price of the underlying equity (stock price) is between $\$ 5$ and $\$ 25$, $\$ 5$ when the stock price is between $\$ 25$ and $\$ 200$, and $\$ 10$ when the stock price is over $\$ 200$. Options are ordinarily not available on stocks priced under $\$ 5$. Strike prices are adjusted for splits, major stock dividends, recapitalizations, and spinoffs, when and if they occur during the life of the option.

## Expiration Date.

At any given time there are four potential expiration dates available for standard option contracts: (1) the current or spot month, (2) the immediate following month, (3) an intermediate month, and (4) a far month (being not more than eight months away). Whichever expiration month is chosen, option contracts always expire at noon on the Saturday following the third Friday of that month. Because trading stops on the day prior to formal expiration (with Saturday morning activity reserved for broker corrections and clearing house operations), the effective expiration date for option contracts is the third Friday of the specified month. For this reason, investors usually speak in terms of "expiration Friday." The section on option cycles later in this chapter will further explain expiration dates.

## Style.

Option contracts are also classified by the basis of the window during which option holders may exercise their rights. American-style options give holders the right to buy or sell at any time prior to expiration of the option. Holders of European-style option contracts may exercise their rights during a very limited period, ordinarily on the day of or day before expiration. At present, all exchange-traded equity options are Americanstyle.

## Puts versus Short Sales

It is certainly cheaper and ordinarily far less risky to buy a put option than to effect a short sale of a stock. For example, assume America Online (AOL) is at $\$ 120$ a share and an investor believes it to be overpriced. The margin or collateral requirement to effect a short sale of 100 shares of AOL at $\$ 120$ is 150 percent of the stock price- $\$ 18,000$ in this case. The first $\$ 12,000$ of this are the proceeds received from the sale of the stock. These funds must be left on deposit to ensure the short seller will return the borrowed shares. The additional $\$ 6,000$ that must be deposited in this case helps to guarantee that the short seller will be able to replace the borrowed shares in the event that the price of AOL stock rises rather than falls. This additional amount also serves as the source of funds for any dividends that the original shareholder is entitled to along the way.

On the other hand, suppose the AOL puts with a strike price of $\$ 120$ command a premium of $\$ 8$ a share. The margin requirement in this case will be the premium cost of $\$ 800$ plus 20 percent of the stock value, or just $\$ 3,200$ in all. Besides the greater margin required, short selling can be particularly risky because of the potential for unlimited loss should the stock rise rather than fall. In addition, the short seller must arrange for the borrowing of shares (often difficult in the case of thinly traded issues) and wait for an uptick in price, whereas the put buyer can act immediately.

## Option Class and Series

All option contracts on the same underlying security having the same type (put versus call) and style (American versus European) are referred to as constituting an option class. Thus, all TWA (Trans World Airlines) calls comprise an option class, as do all Intel puts.

Further, all option contracts within the same class having the same unit of trade (i.e., 100 shares), strike price, and expiration date are referred to as comprising an option series. Thus, the July 2001 AOL $\$ 100$ calls constitute an option series, as do the April 2001 General Electric $\$ 85$ puts.

The last parameter that distinguishes one option from another belonging to the same series is the particular stock exchange where the
various options are traded. For example, TWA options are independently traded on the American, Chicago, and Philadelphia Stock Exchanges. Thus, an October 2001 TWA $\$ 10$ call option contract purchased on the American Stock Exchange can be closed by a sale of the equivalent option contract on the Philadelphia Stock Exchange. The purchase and sale of these two option contracts will precisely offset each other because the contracts belong to the same option series.

## Premiums

A common characteristic of all contracts, including options, is that they involve consideration. For option holders, this refers to the right to exercise the option at the price and terms specified. For option writers, it is the premium, or amount of money paid to them by the option buyers for those exercise rights. Whether or not the option is ever exercised by the option holder, the option writer retains the premium. It is universally acknowledged that there are seven factors that determine the premium:

1. Current stock price
2. Exercise or strike price
3. Time to expiration
4. Current risk-free interest rate
5. Cash dividends

## 6. Option style (European vs. American)

7. Volatility of the underlying equity

The first three parameters (stock price, strike price, and expiration date) are part of every option contract and are readily understood. The next three parameters (risk-free interest rate, ${ }^{*}$ dividends, and option style) certainly have an effect on premiums but only in a relatively minor way. The final parameter, volatility, measures the degree to which the price of the stock fluctuates from day to day. It is important to understand that the greater the volatility and the longer the time to expiration, the higher the premium. This is because the greater the

[^0]daily fluctuation in stock price and the longer the duration of coverage, the greater the uncertainty as to where the stock price will be at any subsequent moment. Equally crucial is the fact that option premiums do not ordinarily reflect the expected rate of growth of the stock price. A demonstration of this remarkable fact is given in Chapter 13. This phenomenon forms the basis of the investment approach developed in this book.

## Exercise and Assignment

If and when an option holder decides to exercise his or her option to buy or sell, the brokerage firm sends a notice to exercise to the Options Clearing Corporation (OCC), which in turn assigns fulfillment of that option to a current option writer of the same series, on either a random or a first-in, first-out basis. The OCC, created in 1972, serves not only as a clearing house for option trades but also as the ultimate guarantor of contract performance. On receipt and verification of the terms of the option contract at the time it was made between buyer and seller (and checking that they match in all respects), the OCC steps in and severs the contractual relationship between the parties, thus becoming the "buyer" to every option writer and the "writer" to every option holder. Owing to this, it does not matter that the original option writer (or every writer for that particular series) may have disappeared from the face of the earth.

## Option Codes

To facilitate trading, options are symbolized by a three- to five-character trading symbol made up of a root symbol designating the underlying equity, a single letter designating the expiration month, and a single letter designating the strike price. Table 1.1 contains the expiration month codes and Tables 1.2 and 1.3 contain the strike price codes for whole- and half-dollar amounts. I keep a copy of these tables pinned on the wall by my telephone.

Let's consider some examples. For most stocks listed on the New York and American Stock Exchanges, the root symbol for the option (no matter where the option itself is traded) is the same as its ordinary trading symbol. Thus, March $\$ 45$ Gillette calls would be coded as G

Table 1.1
Expiration Month Codes
Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
$\begin{array}{llllllllllllll}\text { Calls } & \text { A } & \text { B } & \text { C } & \text { D } & \text { E } & \text { F } & \text { G } & \text { H } & \text { I } & \text { J } & \text { K } & \text { L }\end{array}$
$\begin{array}{llllllllllllll}\text { Puts } & M & N & O & P & Q & R & S & T & U & V & W & X\end{array}$

Table 1.2
Strike Price Codes (Whole Dollars)

| A | $\$ 5$ | $\$ 105$ | $\$ 205$ | $\$ 305$ | $\$ 405$ | $\$ 505$ | $\$ 605$ | $\$ 705$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| B | 10 | 110 | 210 | 310 | 410 | 510 | 610 | 710 |
| C | 15 | 115 | 215 | 315 | 415 | 515 | 615 | 715 |
| D | 20 | 120 | 220 | 320 | 420 | 520 | 620 | 720 |
| E | 25 | 125 | 225 | 325 | 425 | 525 | 625 | 725 |
| F | 30 | 130 | 230 | 330 | 430 | 530 | 630 | 730 |
| G | 35 | 135 | 235 | 335 | 435 | 535 | 635 | 735 |
| H | 40 | 140 | 240 | 340 | 440 | 540 | 640 | 740 |
| I | 45 | 145 | 245 | 345 | 445 | 545 | 645 | 745 |
| J | 50 | 150 | 250 | 350 | 450 | 550 | 650 | 750 |
| K | 55 | 155 | 255 | 355 | 455 | 555 | 655 | 755 |
| L | 60 | 160 | 260 | 360 | 460 | 560 | 660 | 760 |
| M | 65 | 165 | 265 | 365 | 465 | 565 | 665 | 765 |
| N | 70 | 170 | 270 | 370 | 470 | 570 | 670 | 770 |
| ( |  | 175 | 275 | 375 | 475 | 575 | 675 | 775 |


| $\mathbf{P}$ | 80 | 180 | 280 | 380 | 480 | 580 | 680 | 780 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Q}$ | 85 | 185 | 285 | 385 | 485 | 585 | 685 | 785 |
| $\mathbf{R}$ | 90 | 190 | 290 | 390 | 490 | 590 | 690 | 790 |
| $\mathbf{S}$ | 95 | 195 | 295 | 395 | 495 | 595 | 695 | 795 |
| $\mathbf{T}$ | 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 |

Table 1.3
Strike Price Codes (Half Dollars)

| $\mathbf{U}$ | $71 / 2$ | $371 / 2$ | $671 / 2$ | $971 / 2$ | $1271 / 2$ | $1571 / 2$ | $1871 / 2$ | $2171 / 2$ |
| :--- | ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{V}$ | $121 / 2$ | $421 / 2$ | $721 / 2$ | $1021 / 2$ | $1321 / 2$ | $1621 / 2$ | $1921 / 2$ | $2221 / 2$ |
| $\mathbf{W}$ | $171 / 2$ | $471 / 2$ | $771 / 2$ | $1071 / 2$ | $1371 / 2$ | $1671 / 2$ | $1971 / 2$ | $2271 / 2$ |
| $\mathbf{X}$ | $221 / 2$ | $521 / 2$ | $821 / 2$ | $1121 / 2$ | $1421 / 2$ | $1721 / 2$ | $2021 / 2$ | $2321 / 2$ |
| $\mathbf{Y}$ | $271 / 2$ | $571 / 2$ | $871 / 2$ | $1171 / 2$ | $1471 / 2$ | $1771 / 2$ | $2071 / 2$ | $2371 / 2$ |
| $\mathbf{Z}$ | $321 / 2$ | $621 / 2$ | $921 / 2$ | $1221 / 2$ | $1521 / 2$ | $1821 / 2$ | $2121 / 2$ | $2421 / 2$ |

(for Gillette) + C (March call) +I (\$45), or GCI. February $\$ 30$ Boeing puts would be coded as BA (for Boeing) + N (February put) +F (\$30), or BANF. And June $\$ 67.50$ America Online puts would be coded as AOL (for America Online) + R (June put) + U (\$67 1/2), or AOLRU.

In the first example for Gillette, the option trading symbol GCI happens to coincide with the stock trading symbol that is used for the

Gannett Company. In the second example for Boeing, the option trading symbol BANF happens to coincide with the stock trading symbol for BancFirst Corporation. Because of such potential conflicts, brokerage houses and options exchanges preface option trading symbols with some sort of character that unambiguously signals that what follows is an option, not a stock. Quotation requests submitted to the Chicago Board Options Exchange (CBOE) use a period so that .GCI and .BANF designate the particular options quotes on Gillette and Boeing, while GCI and BANF are used for the stock quotes on Gannett and BancFirst. Because the decimal point is sometimes hard to see, some brokerage houses use the prefix "Q" in transmitting orders to their trading desks, thus coding the examples given as QGCI, QBANF, and QAOLRU. (The letter Q can be safely used this way because no stock symbols on any of the exchanges where options are traded begin with that letter.)

Because the trading symbols for Nasdaq stocks have at least four characters in them, they are all assigned three-letter option symbols that often have no relation to the trading symbol. For example, Intel (INTC) has the option symbol INQ, Inktomi (INKT) has the option symbol QYK, and Madge Networks (MADGF) the option symbol MQE. Because very few stock symbols contain the letter Q , this letter is often utilized in the creation of option symbols to avoid conflict with already existing trading symbols. Thus, October $\$ 100$ Intel calls are coded as INQ (for Intel) + J (October call) + T (\$100), or INQJT, and March \$30 Inktomi puts are coded as QYK (for Inktomi) + O (March put) + F (\$30), or QYKOF.

The system described seems pretty simple at first blush. A difficulty, however, arises when a stock is so volatile that the spread in strike prices would require more than one occurrence of the same price code for the same expiration month. In those circumstances, the various exchanges that set up trading symbols are sometimes forced to adopt an alternative option symbol for the underlying stock, or even to assign price code symbols that bear little relation to those in Tables 1.2 and 1.3. Thus, the January 1998 Intel $\$ 45$ puts were coded by the American Stock Exchange at the time as NQMI (rather than INQMI); the August 1997 Intel $\$ 67.50$ calls were coded as INQHW (rather than

INQHU); and the July 1997 Intel $\$ 87.50$ puts were coded as INQSB (rather than INQSY).

Half-dollar amounts typically arise as a result of 2:1 stock splits. For stock splits other than 2:1 (for example, $3: 1$ or 4:3), the resulting trading symbols can often be even more arbitrary.

In view of this, utmost care must be given to determining the proper option codes before transacting trades or submitting such requests to brokers. Because of the large number of options available and the fact that new strike positions and expiration months are continually being created, no printed list of symbol tables could possibly be kept timely enough. One of the best online sources for obtaining accurate trading symbols (and with them, bid and ask quotations on a 20 -minute delayed basis) is from the Chicago Board Options Exchange. Its Internet address is www.cboe.com, and many Internet providers expedite the process of connecting to this Web site through the use of an embedded keyword such as "CBOE" or "OPTIONS" (both used by America Online, for example). Access to CBOE is free, and a wealth of material is available in addition to delayed quotes and the trading symbols for the calls or puts you are interested in.

## Option Cycles

When listed options began trading for the first time, they were each assigned four quarterly expiration dates throughout the year. Cycle 1 options expired in the months of January, April, July, and October. Cycle 2 options expired in the months of February, May, August, and November. And cycle 3 options expired in the months of March, June, September, and December.

The system was subsequently modified so that every equity option has four expiration dates consisting of the nearest two months and two additional months taken from one of the original quarterly cycles. Table 1.4 illustrates the system, with the added month shown in bold italics.

The spot month in Table 1.4 refers to the month in which the next expiration date occurs. The spot month begins the Monday after expiration Friday and ends on the following expiration Friday, thus spanning parts of two calendar months. As the spot month opens, options for that month and two other months will have already been trading. If options for the next nearest month do not exist, options for that month will be opened for trading. If options for the two nearest months have
already been trading, the fourth option opened for trading will be the next one in sequence from the respective quarterly cycle.

Table 1.4
Standard Options Available
Spot
Month Cycle 1 Options $\quad$ Cycle 2 Options $\quad$ Cycle 3 Options

| Jan | Jan | Feb | Apr | Jul | Jan | Feb | May | Aug | Jan | Feb | Mar | Jun |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Feb | Feb | Mar | Apr | Jul | Feb | Mar | May | Aug | Feb | Mar | Jun | Sep |
| Mar | Mar | Apr | Jul | Oct | Mar | Apr | May | Aug | Mar | Apr | Jun | Sep |
| Apr | Apr | May | Jul | Oct | Apr | May | Aug | Nov | Apr | May | Jun | Sep |
| May | May | Jun | Jul | Oct | May | Jun | Aug | Nov | May | Jun | Sep | Dec |
| Jun | Jun | Jul | Oct | Jan | Jun | Jul | Aug | Nov | Jun | Jul | Sep | Dec |
| Jul | Jul | Aug | Oct | Jan | Jul | Aug | Nov | Feb | Jul | Aug | Sep | Dec |
| Aug | Aug | Sep | Oct | Jan | Aug | Sep | Nov | Feb | Aug | Sep | Dec | Mar |
| Sep | Sep | Oct | Jan | Apr | Sep | Oct | Nov | Feb | Sep | Oct | Dec | Mar |
| Oct | Oct | Nov | Jan | Apr | Oct | Nov | Feb | May | Oct | Nov | Dec | Mar |
| Nov | Nov | Dec | Jan | Apr | Nov | Dec | Feb | May | Nov | Dec | Mar | Jun |

A handbook that is particularly useful for dealing with options is the Directory of Exchange Listed Options, available without charge from the Options Clearing Corporation by calling 800-OPTIONS (678-4667). This directory contains much useful information, including a list of option trading symbols, option cycles, and the exchange (s) where each option trades.

## 2-

## Long-Term Options

## Introduction

An incredible number of books have been written on the subject of options and options trading. A search using the keyword "options" on the online bookstore Amazon.com yielded over 300 titles, ranging from academic treatises to texts on elementary, intermediate, and advanced trading techniques. There is no particular need for yet another book on how to construct and utilize spreads, straddles, and other option combinations. Instead, the purpose of this book is to highlight the fact that option premiums in general do not reflect the expected long-term growth rate of the underlying equities and to explain an investment strategy that can be used to take maximum advantage of this phenomenon.

As I mentioned before, my own interest in this subject stems from the fact that I could no longer contribute additional funds to my retirement plan. As a long-term investor in the market, I had assembled a stock portfolio over many years, and I simply did not wish to raise cash by selling any of my winners. My few losers and laggards had long since been disposed of and the proceeds used to buy more shares of my better-performing stocks. I'm not a short-term, in-and-out investor, but I wanted to keep buying.

Options seemed the way to go, but as with stocks, purchasing calls requires money. What's more, options can only be paid for in cash, so going on margin and borrowing the funds from my broker was out of
the question. My next thought was, if I'm going to raise cash, why not sell covered calls on my portfolio? I tried this a few times and promptly had some of my stocks called away from me when their share prices sharply increased as a result of takeover rumors or positive earnings surprises. I wasn't too happy about having to buy back shares using the little cash I had remaining to cover the gap between the exercise price received and the higher repurchase price. So much for covered calls.

By process of elimination, the only strategy remaining was selling puts. This method, you will recall, generates up-front money through the premiums received. Option premiums must be paid on the next business day and are available for reinvestment even faster than proceeds from the sale of stock (which settle within three business days). And because these funds represent premiums paid, not dollars borrowed, they are yours to keep.

However, as the fine print in most travel ads states, "certain restrictions apply." Premiums have to stay in your account in case they are needed later in the event of assignment. But because they are in your account, you can use them to acquire additional equities. The problem with this approach, I soon discovered, is that applying it to standard options does not bring in much money, especially in relation to the risk assumed in potentially having the underlying stock assigned to you. You can certainly sell a put whose exercise price is well below the current stock price, thereby minimizing the risk of assignment, but doing this brings in a very small premium.

A larger premium can be generated by selling a put with an exercise price much closer to or just below the current price, but this can entail significant risk of assignment. Substantial premiums seen on out-of-the-money ${ }^{*}$ puts typically indicate highly volatile stocks or instances where the market (probably correctly) anticipates a sharp drop in the value of the underlying equity-situations that had no appeal to me whatsoever.

And if all that isn't enough, there is also the fact that dealing in standard options, with their quickly changing market values, typically

[^1]requires substantial, if not full-time, commitment to the task. Most option traders I've met have had little time for anything else during their working days and have often spent a good deal of their evenings and weekends conducting research into what trades to enter and when to cover and get out. This kind of nerve-wracking, nail-biting, glued-to-theconsole environment is not what I wanted either.

It then occurred to me that there was a solution to this dilemma. There does exist a class of options whose premiums are relatively large, which bear less risk than standard options, and which, because the underlying equities are comparatively stable, do not have to be monitored with anywhere near the same intensity as standard options. What distinguishes this class of options is their long-term expiration date, which permits the market price of the underlying equity plenty of time to recover should the overall market, industry sector, or the company itself encounter a temporary downturn or adverse conditions. It occurred to me that by selling puts on stronger, well-endowed firms whose intermediate- and long-term prospects are above average, it might be possible to achieve high returns without incurring undue risk.

## LEAPS

The class of options that fits this description was actually created by the Chicago Board Options Exchange in 1990. Because standard options expire at most eight months after their inception, the CBOE introduced a new product for investors wishing to hedge common stock positions over a much longer time horizon. These options, called LEAPS (Long-term Equity AnticiPation Securities), are long-term options on common stocks of companies that are listed on securities exchanges or that trade over the counter. LEAPS expire on the Saturday following the third Friday in the month of January approximately two and a half years from the date of the initial listing. They roll into and become standard options after the May, June, or July expiration date corresponding to the expiration cycle of the underlying security.

In most other ways, LEAPS are identical to standard options. Strike price intervals for LEAPS follow the same rules as standard options (i.e., they are $\$ 2.50$ when the stock price of the underlying equity is between $\$ 5$ and $\$ 25, \$ 5$ when the stock price is between $\$ 25$ and $\$ 200$, and $\$ 10$ when the stock price is over $\$ 200$ ). As for standard
options, strike prices for LEAPS are adjusted for splits, major stock dividends, recapitalizations, and spin-offs when and if they occur during the life of the option. Like standard options, equity LEAPS generally may be exercised on any business day before the expiration date.

Margin requirements for LEAPS follow the same rules as standard options. Uncovered put or call writers must deposit 100 percent of the option proceeds plus 20 percent of the aggregate contract value (the current price of the underlying equity multiplied by $\$ 100$ ) minus the amount, if any, by which the LEAP option is out of the money. The minimum margin is 100 percent of the option proceeds plus 10 percent of the aggregate contract value. I will have a lot to say about margin requirements in Chapter 4.

## LEAP Premiums

Option premiums in general vary directly with the remaining time to expiration. As a result of their longer lives, LEAPS have premiums that can be considerably greater than those of their standard option counterparts. Table 2.1 shows the premiums per share for an at-the-money put option where the stock price and strike price are both $\$ 100$, the riskfree interest rate is 6 percent, and the effect of dividends is ignored. As outlined in Chapter 1, the only other parameters are expiration time, stock volatility, and option style. Each entry in the table is the theoretical premium corresponding to the expiration time in months shown in column 1 and the stock volatility, ranging from a fairly low level of 0.15 to a fairly high level of 0.65 . The premiums shown were calculated using the simple Black-Scholes pricing formula for European-style options that is described in Chapter 14. A more detailed set of premium tables for European-style options appears in Appendix A. For comparison and reference purposes, the analog at-the-money call premiums are shown in Table 2.2.

Intel's stock, for example, has a volatility of about 0.35 , so when the stock price reaches $\$ 100$, an at-the-money put option should command a premium of \$829.60 (\$8.296 $\times 100$ shares) with six months to expiration and a premium of $\$ 1,313.40(\$ 13.314 \times 100$ shares) with 24 months to expiration. Chapter 13 shows how volatility is calculated from historical stock prices.

The at-the-money premiums shown in Table 2.1 for puts and in Table 2.2 for calls scale directly with the price level involved. That is, if the stock price and strike price are both $\$ 50$, the corresponding per share premiums are exactly half the amounts shown.

The first question people often ask is why the at-the-money call premiums are so much greater than the corresponding put premiums for the same time horizon and volatility level. Note, for example, that for a stock with a volatility of 0.35 and an expiration date 30 months away, the put premium is $\$ 14.035$ per share versus $\$ 27.964$ for the call premium. Is this difference due to general inflation and/or the expected growth rate in the underlying equity?

The answer is no. The reason the call premiums are greater is that option pricing models assume that stock prices are just as likely to increase by, say, 10 percent as they are to decrease by 10 percent on any given day. On a cumulative basis, there is therefore no limit to how high prices can go up over time, but there is a definite lower limit (zero) to how low prices can go. It is this possibility of unrestricted price movement upward versus restricted price movement downward that explains why calls are more expensive than puts.

## Commissions

There is another major advantage associated with LEAPS. Because of the inherently greater premium levels involved, the brokerage commissions charged are going to be a smaller percentage of the proceeds received. At a full-service firm, the brokerage commission to buy or sell a single option might be $\$ 45$. In percentage terms, this amount is almost 12 percent of the premium for the one-month Intel option, but just 3.2 percent of the premium for the 30 -month LEAP option. Commission costs per contract rapidly decrease at a full-service firm if more than one contract is involved and might range from $\$ 25$ to $\$ 35$ each for three contracts down to just $\$ 15$ to $\$ 20$ each for ten contracts.

At a discount broker's, the commission might be $\$ 20$ each, but it is typically subject to a minimum fee of $\$ 40$ and a maximum fee of $\$ 70$ on transactions involving one to ten contracts. For online, deep-discount, and option-specialized brokers, the commission might be $\$ 15$ each but is typically subject to a minimum fee of $\$ 35$ and a maximum fee of $\$ 60$ on transactions of one to ten contracts.

Table 2.1
European-Style At-the-Money Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100
$$

Strike Price $=\$ 100$

|  |  |  | Volatility |  |  |  |  |  |  |  |  |  |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |  |
| 1 | 1.485 | 2.057 | 2.629 | 3.202 | 3.776 | 4.349 | 4.922 | 5.495 | 6.067 | 6.639 | 7.211 |  |
| 2 | 1.965 | 2.767 | 3.572 | 4.378 | 5.185 | 5.991 | 6.797 | 7.603 | 8.408 | 9.212 | 10.015 |  |
| 3 | 2.283 | 3.258 | 4.237 | 5.220 | 6.202 | 7.185 | 8.167 | 9.149 | 10.128 | 11.107 | 12.083 |  |
| 4 | 2.520 | 3.636 | 4.760 | 5.888 | 7.018 | 8.147 | 9.275 | 10.401 | 11.526 | 12.649 | 13.769 |  |
| 5 | 2.705 | 3.943 | 5.192 | 6.447 | 7.703 | 8.959 | 10.214 | 11.466 | 12.716 | 13.963 | 15.207 |  |
| 6 | 2.854 | 4.199 | 5.560 | 6.927 | 8.296 | 9.665 | 11.032 | 12.397 | 13.758 | 15.115 | 16.468 |  |
| 7 | 2.976 | 4.419 | 5.879 | 7.348 | 8.819 | 10.290 | 11.760 | 13.225 | 14.687 | 16.143 | 17.594 |  |
| 8 | 3.079 | 4.608 | 6.160 | 7.722 | 9.287 | 10.852 | 12.414 | 13.973 | 15.526 | 17.073 | 18.613 |  |
| 9 | 3.164 | 4.774 | 6.410 | 8.058 | 9.709 | 11.361 | 13.009 | 14.653 | 16.291 | 17.921 | 19.544 |  |
| 10 | 3.237 | 4.920 | 6.634 | 8.362 | 10.094 | 11.826 | 13.555 | 15.278 | 16.994 | 18.702 | 20.400 |  |
| 11 | 3.298 | 5.049 | 6.836 | 8.639 | 10.446 | 12.254 | 14.057 | 15.855 | 17.644 | 19.423 | 21.192 |  |
| 12 | 3.349 | 5.165 | 7.020 | 8.892 | 10.771 | 12.649 | 14.523 | 16.390 | 18.248 | 20.095 | 21.929 |  |
| 13 | 3.393 | 5.267 | 7.187 | 9.125 | 11.071 | 13.016 | 14.956 | 16.889 | 18.811 | 20.721 | 22.617 |  |
| 14 | 3.429 | 5.360 | 7.339 | 9.340 | 11.349 | 13.358 | 15.361 | 17.355 | 19.338 | 21.307 | 23.262 |  |
| 15 | 3.460 | 5.442 | 7.479 | 9.539 | 11.608 | 13.677 | 15.739 | 17.792 | 19.832 | 21.858 | 23.867 |  |
| 16 | 3.485 | 5.516 | 7.607 | 9.724 | 11.850 | 13.975 | 16.094 | 18.203 | 20.298 | 22.377 | 24.437 |  |


| 17 | 3.505 | 5.583 | 7.725 | 9.895 | 12.076 | 14.256 | 16.429 | 18.590 | 20.737 | 22.866 | 24.975 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 18 | 3.521 | 5.642 | 7.834 | 10.055 | 12.287 | 14.519 | 16.743 | 18.955 | 21.151 | 23.328 | 25.483 |
| 19 | 3.533 | 5.696 | 7.934 | 10.204 | 12.486 | 14.767 | 17.041 | 19.300 | 21.543 | 23.765 | 25.964 |
| 20 | 3.542 | 5.744 | 8.026 | 10.343 | 12.672 | 15.001 | 17.321 | 19.627 | 21.915 | 24.180 | 26.420 |
| 21 | 3.548 | 5.787 | 8.111 | 10.472 | 12.847 | 15.222 | 17.587 | 19.937 | 22.267 | 24.573 | 26.853 |
| 22 | 3.552 | 5.825 | 8.189 | 10.594 | 13.012 | 15.431 | 17.839 | 20.231 | 22.601 | 24.947 | 27.264 |
| 23 | 3.553 | 5.859 | 8.262 | 10.707 | 13.168 | 15.628 | 18.077 | 20.509 | 22.919 | 25.302 | 27.655 |
| 24 | 3.551 | 5.889 | 8.329 | 10.813 | 13.314 | 15.815 | 18.304 | 20.774 | 23.222 | 25.640 | 28.027 |
| 25 | 3.548 | 5.915 | 8.390 | 10.913 | 13.452 | 15.992 | 18.519 | 21.026 | 23.509 | 25.962 | 28.382 |
| 26 | 3.543 | 5.938 | 8.447 | 11.006 | 13.583 | 16.159 | 18.723 | 21.266 | 23.783 | 26.269 | 28.719 |
| 27 | 3.536 | 5.957 | 8.499 | 11.093 | 13.706 | 16.318 | 18.917 | 21.495 | 24.044 | 26.561 | 29.041 |
| 28 | 3.527 | 5.974 | 8.547 | 11.174 | 13.822 | 16.469 | 19.102 | 21.712 | 24.293 | 26.840 | 29.348 |
| 29 | 3.517 | 5.988 | 8.591 | 11.251 | 13.932 | 16.612 | 19.277 | 21.919 | 24.531 | 27.106 | 29.640 |
| 30 | 3.506 | 6.000 | 8.631 | 11.322 | 14.035 | 16.747 | 19.444 | 22.117 | 24.757 | 27.360 | 29.920 |

Although there can be significant differences in total commission costs between fullservice brokers and other firms, I prefer to work with options-knowledgeable people at a full-service firm. I can readily do this because I am not a short-term investor, and the relatively small number of trades I do per year does not result in significant commissions in terms of absolute dollars. This is particularly true when one remembers that in selling options that subsequently expire worthless, only one commission is involved, not two.

Table 2.2
European-Style At-the-Money Call Premiums as a Function of Time and Volatility

| Stock Price $=\mathbf{\$ 1 0 0}$ |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Strike Price $=\mathbf{\$ 1 0 0}$ |  |  |  |  |  |  |  |  |  |  |  |
| Volatility |  |  |  |  |  |  |  |  |  |  |  |
| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| 1 | 1.984 | 2.555 | 3.128 | 3.701 | 4.274 | 4.848 | 5.421 | 5.993 | 6.566 | 7.138 | 7.710 |
| 2 | 2.960 | 3.762 | 4.567 | 5.373 | 6.180 | 6.986 | 7.792 | 8.598 | 9.403 | 10.207 | 11.010 |
| 3 | 3.772 | 4.746 | 5.726 | 6.708 | 7.691 | 8.674 | 9.656 | 10.637 | 11.617 | 12.596 | 13.572 |
| 4 | 4.500 | 5.616 | 6.740 | 7.868 | 8.998 | 10.127 | 11.255 | 12.382 | 13.506 | 14.629 | 15.749 |
| 5 | 5.174 | 6.412 | 7.661 | 8.916 | 10.172 | 11.428 | 12.683 | 13.935 | 15.185 | 16.432 | 17.676 |
| 6 | 5.809 | 7.155 | 8.515 | 9.882 | 11.252 | 12.621 | 13.988 | 15.352 | 16.714 | 18.071 | 19.423 |
| 7 | 6.416 | 7.858 | 9.319 | 10.787 | 12.259 | 13.730 | 15.199 | 16.665 | 18.126 | 19.583 | 21.034 |
| 8 | 7.000 | 8.529 | 10.081 | 11.643 | 13.208 | 14.773 | 16.335 | 17.894 | 19.447 | 20.994 | 22.534 |
| 9 | 7.565 | 9.174 | 10.810 | 12.458 | 14.110 | 15.761 | 17.410 | 19.053 | 20.691 | 22.322 | 23.944 |
| 10 | 8.114 | 9.797 | 11.511 | 13.239 | 14.971 | 16.703 | 18.432 | 20.155 | 21.871 | 23.579 | 25.277 |
| 11 | 8.649 | 10.401 | 12.188 | 13.990 | 15.798 | 17.605 | 19.409 | 21.206 | 22.995 | 24.775 | 26.544 |
| 12 | 9.173 | 10.988 | 12.843 | 14.716 | 16.594 | 18.473 | 20.347 | 22.213 | 24.071 | 25.918 | 27.753 |
| 13 | 9.686 | 11.561 | 13.480 | 15.419 | 17.364 | 19.309 | 21.250 | 23.182 | 25.104 | 27.014 | 28.910 |
| 14 | 10.190 | 12.120 | 14.100 | 16.101 | 18.110 | 20.118 | 22.121 | 24.115 | 26.098 | 28.068 | 30.022 |
| 15 | 10.685 | 12.668 | 14.705 | 16.765 | 18.834 | 20.902 | 22.965 | 25.018 | 27.058 | 29.084 | 31.093 |
| 16 | 11.173 | 13.205 | 15.296 | 17.412 | 19.538 | 21.664 | 23.783 | 25.891 | 27.986 | 30.065 | 32.125 |


| 17 | 11.654 | 13.731 | 15.874 | 18.044 | 20.225 | 22.405 | 24.577 | 26.739 | 28.885 | 31.014 | 33.123 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 18 | 12.128 | 14.249 | 16.441 | 18.662 | 20.894 | 23.126 | 25.350 | 27.562 | 29.758 | 31.935 | 34.090 |
| 19 | 12.596 | 14.759 | 16.996 | 19.266 | 21.549 | 23.830 | 26.103 | 28.363 | 30.606 | 32.828 | 35.027 |
| 20 | 13.059 | 15.260 | 17.542 | 19.859 | 22.188 | 24.517 | 26.838 | 29.143 | 31.431 | 33.696 | 35.937 |
| 21 | 13.516 | 15.754 | 18.079 | 20.440 | 22.815 | 25.190 | 27.555 | 29.904 | 32.234 | 34.541 | 36.821 |
| 22 | 13.968 | 16.241 | 18.606 | 21.010 | 23.429 | 25.847 | 28.255 | 30.647 | 33.018 | 35.364 | 37.681 |
| 23 | 14.416 | 16.722 | 19.125 | 21.570 | 24.031 | 26.491 | 28.941 | 31.373 | 33.783 | 36.166 | 38.519 |
| 24 | 14.859 | 17.197 | 19.637 | 22.121 | 24.622 | 27.123 | 29.612 | 32.082 | 34.529 | 36.948 | 39.335 |
| 25 | 15.298 | 17.665 | 20.141 | 22.663 | 25.203 | 27.742 | 30.269 | 32.777 | 35.260 | 37.713 | 40.132 |
| 26 | 15.733 | 18.128 | 20.637 | 23.196 | 25.773 | 28.350 | 30.913 | 33.457 | 35.974 | 38.459 | 40.910 |
| 27 | 16.164 | 18.586 | 21.128 | 23.721 | 26.334 | 28.947 | 31.545 | 34.123 | 36.673 | 39.190 | 41.669 |
| 28 | 16.591 | 19.039 | 21.611 | 24.239 | 26.886 | 29.533 | 32.166 | 34.776 | 37.358 | 39.904 | 42.412 |
| 29 | 17.015 | 19.486 | 22.089 | 24.748 | 27.429 | 30.110 | 32.775 | 35.417 | 38.029 | 40.604 | 43.138 |
| 30 | 17.436 | 19.929 | 22.560 | 25.251 | 27.964 | 30.677 | 33.374 | 36.046 | 38.686 | 41.289 | 43.849 |

## LEAPS Available

LEAPS are currently traded on over 300 widely followed equities (as well as on numerous industry sector, domestic, and international indices). Table 2.3 at the end of this chapter lists the equity LEAPS available in August 1999 and shows the name of the underlying security, its stock symbol, the standard option symbol, the exchange code(s) showing where the option is traded, the options cycle govern-
ing when the LEAP option rolls over into a standard option, and the option symbol for the LEAPS expiring in the years 2001 and 2002. Omitted from the table are issues for which no new LEAPS will be listed as a result of mergers and acquisitions that have taken place.

## Exchange Codes.

LEAPS are traded on one or more of four major exchanges, ${ }^{*}$ as indicated by the following symbols:

A American Stock Exchange
C Chicago Board Options Exchange
P Pacific Stock Exchange
X Philadelphia Stock Exchange

## Expiration Cycles.

These are the January, February, and March cycles that control how and when each LEAP option rolls over into a standard option. It is important to note that the trading symbol for a LEAP option will change when it does roll over and become a standard option, and quote requests, statements, trades, close-outs and exercise instructions should reflect this. In Table 2.3, the numerical codes used for the expiration cycles are:

## 1 January Sequential

## 2 February Sequential

3 March Sequential
The expiration cycle of a given class of options also tells you the specific month that the corresponding LEAP is due to open for trading. For example, Intel is cycle 1 , so the next set of Intel LEAPS is supposed to open right after the May expiration. Boeing is cycle 2, so the next set of Boeing LEAPS is supposed to open right after the June expiration. And Pfizer is cycle 3, so the next set of Pfizer LEAPS is supposed to open right after the July expiration.

## LEAP Symbols.

To facilitate trading, LEAPS are symbolized by a four- to six-character trading symbol made up of a root symbol

[^2]designating the underlying equity, a single character designating the expiration month, and a single letter designating the strike price involved. Because LEAPS expire only in January, the code letter for the expiration month is always $A$ for calls and $M$ for puts. The root symbols for the underlying equity began with the letter $V$ for the January 1999 LEAPS and the letter $L$ for the January 2000 LEAPS, and begin with the letter $Z$ for the January 2001 LEAPS and the letter $W$ for the January 2002 LEAPS. This $V / L / Z / W$ sequence of initial letters is repeated every four years, so the letter $V$ will likely be assigned as the starting letter for the year 2003 LEAPS. As each LEAP option rolls over into a standard option approximately a half year prior to expiration, the root symbol portion of the trading code is changed to that of the standard option. Because of conflicts that frequently arise with existing trading symbols of stocks and standard options, there is often no consistency in the designations of LEAP root symbols. Note too that although the LEAP root symbols are three letters long, in some instances they consist of just two letters. A dash indicates that there was no LEAP option offered for that year on a particular security, often because of a pending merger or acquisition.

It is frequently the case that as a result of a wide fluctuation in stock price (as well as mergers, acquisitions, and stock splits), there is going to be more than one LEAP root symbol for a given stock and expiration year. Table 2.3 shows in each case the principal root symbol. For example, the January 2001 LEAPS for Yahoo have the root YZY for strikes between $\$ 22.5$ and $\$ 35$; ZYH for strikes $\$ 37.50$ through $\$ 85$; ZGH for strikes $\$ 90$ through $\$ 135$; ZYO for strikes $\$ 150$ through $\$ 200$; and ZYM for strikes between $\$ 210$ and $\$ 250$. The only sure way to determine the correct root symbol for a given LEAP option series is to consult an online table showing the specific LEAPS available, such as the one maintained by the Chicago Board Options Exchange at www.cboe.com. Or you can call the CBOE directly at 800-OPTIONS (678-4667).

## Position Limits.

Not shown in Table 2.3 because of rapidly changing conditions is the maximum number of open contracts that are permitted on any option class. As opposed to stocks, whose outstanding shares often number in the hundreds of millions, the maximum number of open option contracts (including LEAPS and standard options)
permitted on the underlying equity is heavily limited. These limits are set in accordance with the number of outstanding shares and the trading volume of the underlying equity. The larger, more frequently traded stocks are assigned initial position limits of 75,000 contracts, while less active issues are assigned initial position limits of either 60,000, $31,500,22,500$, or as few as 13,500 contracts for the smallest of traded issues. As a result of stock splits, mergers, acquisitions, and other factors, these limits are periodically adjusted. Position limits are imposed by the various options exchanges to prevent any person or entity from controlling the market on a given issue. Because every option contract has both a buyer and a seller, the open contract count is the sum of the number of opening calls bought and the number of opening puts sold, so as not to double count.

## Using Options to Buy Stocks

There's no way around it, buying stocks takes money. But by now you've guessed where the money for buying stocks can come from: not out of your pocket but from the premiums accumulated from the sales of the LEAP puts. As described in the preface, the purpose of my selling LEAP puts was not just to enhance the cash flow and dividend yield of my stock portfolio. Rather, it was to furnish the funds with which to continue stock acquisition.

The appropriate strategies for generating option premiums consistent with a high rate of premium retention and low rate of financial exposure are the subject of the next several chapters.

Table 2.3
LEAPS Available August 1999

| Underlying | Stock |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Squity | Symbol | Option <br> Symbol | Exchange <br> Code | Cycle No. 2001 LEAP 2002 LEAP |


| Abbott | ABT | ABT | CX | ZBT |
| :--- | :--- | :--- | :--- | :--- | :--- |

Laboratories

Abercrombie ANF \& Fitch

| Acuson | ACN | ACN | P | 1 | ZAU | WAU |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Adaptec | ADPT | APQ | A | 1 | ZYA | WYA |
| Adobe <br> Systems | ADBE | AEQ | P | 1 | ZAE | WAE |
| Advanced <br> Micro <br> Devices | AMD | AMD | CP | 1 | ZW | WW |


| Aetna | AET | AET | A | 1 | ZLY | WLY |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Allied Signal | ALD | ALD | X | 3 | ZAL | WAD |
| Allstate | ALL | ALL | ACP | 1 | ZZL | WLZ |
| Altera | ALTR | LTQ | CP | 3 | ZZT | WZT |
| ALZA | AZA | AZA | CP | 1 | ZZA | WZA |
| Amazon.com | AMZN | ZQN | ACPX | 1 | ZWE | WEW |
| Amerada Hess | AHC | AHC | X | 2 | ZHS | WHS |
| America Online | AOL | AOL | ACP | 1 | ZAN | WAN |
| American Express | AXP | AXP | AC | 1 | ZXP | WXP |


| American Home Products | AHP | AHP | A | 1 | ZAH | WHP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| American International Group | AIG | AIG | C | 2 | ZAF | WAP |
| American Tower | AMT | AMT | C | 1 | ZKC | WVY |
| Ameritech | AIT | AIT | C | 1 | ZIA | WFP |
| Ameritrade | AMTD | TAZ | ACP | 2 | ZXK | WKZ |
| Amgen | AMGN | AMQ | A | 1 | ZAM | WAM |
| AMR | AMR | AMR | A | 2 | ZAR | WAR |
| Andrew | ANDW | AQN | C | 1 | ZAQ | WWN |
| AnheuserBusch | BUD | BUD | X | 3 | ZBD | WBD |
| Apple Computer | AAPL | AAQ | A | 1 | ZAA | WAA |
| Applied Materials | AMAT | ANQ | CP | 1 | ZPJ | WPJ |
| ASA <br> Limited | ASA | ASA | A | 2 | ZSL | WSL |
| Associates First Capital | AFS | AFS | AC | 3 | ZA | WFB |
| At Home | ATHM | AHQ | ACP | 1 | ZHO | WHO |
| AT\&T | T | T | C | 1 | ZT | WT |
| Atlantic Richfield | ARC | ARC | C | 1 | ZFR | WFA |
| AutoNation | AN | AN | AC | 1 | ZYU | WYU |


| Avon <br> Products | AVP | AVP | C | 1 | ZVP | WVP |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Baker <br> Hughes | BHI | BHI | CP | 1 |  | ZBH | WBH

(Table continued on next page)

Table 2.3
LEAPS Available August 1999 (Continued)

| Underlying | Stock | Option | Exchange | Cycle No. | 2001 LEAP 2002 LEAP |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Equity | Symbol | Symbol | Code |  |  |

Boston
Scientific
BP Amoco
Bristol-Myers
Squibb

Broadcorn
BRCM
RCQ
ACPX
ZGJ
WGJ

Burlington
BNI
BNI
C
ZNI
WBU
Northern Santa
Fe
Cabletron
Systems

| Campbell Soup | CPB | CPB | C |
| :--- | :--- | :--- | :--- |
| Canadian | CNI | CNI | C |
| National <br> Railway |  |  |  |


| Caterpillar | CAT | CAT | A | 2 | ZKT | WKT |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| CBS | CBS | CBS | A | 1 | ZWX | WWX |
| C-Cube <br> Microsystems | CUBE | UQB | AC | 2 | ZCX | WCX |
| Cendant | CD | CD | ACX | 2 | ZUB | WLD |
| Centocor | CNTO | COQ | C | 1 | ZCT | WCT |
| Chase <br> Manhattan | CMB | CMB | A | 3 | ZCV | WCV |


| Chevron | CHV | CHV | A | 3 | ZCH | WCH |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Chiron | CHIR | CIQ | AC | 1 | ZHR | WCI |
| Chubb | CB | CB | C | 1 | ZCU | WCU |
| Cirrus Logic | CRUS | CUQ | CP | 3 | ZUR | WUR |
| Cisco Systems | CSCO | CYQ | CP | 1 | ZCY | WCY |
| CIT Group | CIT | CIT | AC | 1 | ZVF | WVF |
| Citigroup | C | C | CX | 3 | ZRV | WRV |
| Clarify | CLFY | QCY | C | 2 | ZGF | WLF |
| Clear Channel Communications | CCU | CCU | C | 1 | ZYC | WVX |
| CMG <br> Information Systems | CMGI | QGC | AC | 3 | ZCK | WCK |
| Coca-Cola | KO | KO | C | 2 | ZKO | WKO |
| Coca-Cola Enterprises | CCE | CCE | C | 2 | ZCC | WOD |
| Coeur d'Alene Mines | CDE | CDE | C | 2 | ZAG | - |
| Colgate- <br> Palmolive | CL | CL | C | 2 | ZGO | WTP |
| Columbia Energy Group | CG | CG | A | 2 | ZCG | WC |
| Columbia/HCA Healthcare | COL | COL | AC | 2 | ZYS | WOM |
| Comcast | CMCSK | CQK | CX | 1 | ZBB | WPV |
| Compania de Telecom. de Chile | CTC | CTC | AC | 2 | ZDT | WDT |


| Compaq Computer | CPQ | CPQ | P | 1 | ZKP | WKP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CompUSA | CPU | CPU | AC | 2 | ZWP | WVC |
| Computer Associates | CA | CA | C | 2 | ZCA | WOA |
| Compuware | CPWR | CWQ | C | 2 | ZWC | WWQ |
| Conseco | CNC | CNC | AC | 2 | ZCE | WCE |
| Corning | GLW | GLW | C | 2 | ZGL | WGU |
| Cracker Barrel Old Country Stores | CBRL | CBQ | P | 3 | ZBR | WBR |
| Cypress <br> Semiconductor | CY | CY | C | 3 | ZSY | WSY |
| DaimlerChrysler AG | DCX | DCX | C | 1 | - | WLG |
| Data General | DGN | DGN | CP | 3 | ZCW | WCW |
| Dayton Hudson | DH | DH | P | 1 | ZDH | WDH |
| Dell Computer | DELL | DLQ | X | 2 | ZDE | WDQ |
| Delta Air Lines | DAL | DAL | C | 1 | ZDA | WDA |
| Diamond Offshore Drilling | DO | DO | C | 3 | ZXD | WFJ |
| Disney | DIS | DIS | AC | 1 | ZDS | WDS |

(Table continued on next page)

Table 2.3
LEAPS Available August 1999 (Continued)

| Underlying Equity | Stock Symbol | Option <br> Symbol | Exchange Code | Cycle No. | 2001 LEAP | 2002 LEAP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dow Chemical | DOW | DOW | C | 3 | ZDO | WDO |
| du Pont (E.I.) de Nemours | DD | DD | AC | 1 | ZDD | WDD |
| Eastman Kodak | EK | EK | C | 1 | ZEK | WEK |
| Electronic Arts | ERTS | EZQ | C | 3 | ZQZ | WZW |
| Electronic <br> Data <br> Systems | EDS | EDS | X | 3 | ZED | WED |
| Electronics for Imaging | EFII | EFQ | C | 1 | ZEF | WEF |
| EMC | EMC | EMC | C | 1 | ZUE | WUE |
| Enron | ENE | ENE | C | 1 | ZOZ | WUM |
| Epicor Software | EPIC | PQS | C | 1 | ZPO | WPR |
| Equifax | EFX | EFX | P | 1 | ZQF | WQF |
| Ericsson (L.M.) Telephone | ERICY | RQC | ACX | 1 | ZYD | WRY |
| ESS <br> Technology | ESST | SEQ | C | 1 | ZES | WEY |
| Exxon | XON | XON | C | I | ZXO | WXO |
| Fannie Mae | FNM | FNM | CX | 3 | ZFN | WFN |

(Federal
Nat'l Mtg
Ass'n)

| FDX |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| (Federal <br> Express) |  | FDX |  | FDX | 1 | ZFX |

Federated
Department
Stores

| First FAM | FAM | CPX | 3 | ZCN |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

American

| First Union | FTU | FTU |
| :--- | :--- | :--- |
| Fleet | FLT | FLT |
| Financial |  |  |
| Group |  |  |


| Ford Motor | F | F | C | 3 | ZFO | WFO |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| FORE <br> Systems | FORE | FQO | ACPX | 1 | ZFY | WFY |
| Forest <br> Laboratories | FRX | FRX | C | 2 | ZML | WRT |
| Freddie Mac <br> (Federal <br> Home Loan <br> Mtg) | FRE | FRE | A | 1 | ZFM | WFF |
| Fruit of the <br> Loom | FTL | FTL | C | 2 | ZTL | WTL |
| Gannett | GCI | GCI | P | I | ZHJ | WHJ |
| Gap | GPS | GPS | C | 3 | ZGS | WGS |
| Gateway | GTW | GTW | ACP | 3 | ZWB | WGB |
| General <br> Electric | GE | GE | C | 3 | ZGR | WGE |


| General <br> Mills | GIS | GIS | P | 1 | ZGI | WGI |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| General <br> Motors | GM | GM | C | 3 |  | ZGM | WGM

Table 2.3
LEAPS Available August 1999 (Continued)

| Underlying | Stock <br> Symbol | Option <br> Symbol | Exchange <br> Code | Cycle No. 2001 LEAP 2002 LEAP |
| :--- | :--- | :--- | :--- | :--- | :--- |


| Household <br> International | HI | HI | A | 1 | ZIH | WOH |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| ICOS | ICOS | IIQ | C | 1 | ZIL | WJI |
| Ikon Office | IKN | IKN | C | 3 | ZKN | WKN |

Solutions

| Informix | IFMX | IFQ | AC | 2 | ZXF | WIF |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Inktomi | INKT | QYK | ACPX | 1 | ZIC | WHA |
| Inprise | INPR | BLQ | C | 1 | ZOB | WOB |
| Intel | INTC | INQ | A | 1 | ZNL | WNL |
| International <br> Business <br> Machines | IBM | IBM | C | 1 | ZIB | WIB |


| International <br> Game <br> Technology | IGT | IGT | A | 1 | ZGG | WGG |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| International <br> Paper | IP | IP | C | 1 | ZNP | WNP |
| Interpublic Group | IPG | IPG | C | 1 | ZIP | - |
|  <br> Johnson | JNJ | JNJ | C | 1 | ZJN | WJN |
| K Mart | KM | KM | C | 3 | ZKM | WKM |
| Kellogg | K | K | A | 3 | ZLK | WKG |
| Kimberly-Clark | KMB | KMB | A | 1 | ZKL | WKL |


| KLA Instruments | KLAC | KCQ | CP | 3 | ZXG | WXG |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Kroger | KR | KR | A | 1 | ZKK | WKK |
| Lain Research | LRCX | LMQ | P | 3 | ZPC | WPC |
| Lehman Brothers | LEH | LEH | AC | 1 | ZHE | WHE |
| Level 3 <br> Communications | LVLT | QHN | ACP | 3 | ZEV | WVK |
| Lilly (Eli) | LLY | LLY | A | 1 | ZYY | WIL |
| Limited | LTD | LTD | C | 2 | ZLT | WDL |
| Liposome | LIPO | LPQ | C | 2 | ZRZ | WXF |
| Loral Space \& Communications | LOR | LOR | C | 1 | ZLO | WLO |
| Lowe's | LOW | LOW | ACX | 1 | ZOY | WOY |
| LSI Logic | LSI | LSI | C | 1 | ZSI | WBS |
| Lucent <br> Technologies | LU | LU | ACX | 1 | ZEU | WEU |
| Madge Networks. | MADGF | MQE | AC | 2 | ZLM | - |
| Magna <br> International | MGA | MGA | C | 2 | ZGA | WMG |
| Marine Drilling | MRL | MRL | C | 2 | ZDQ | WIM |
| Mattel | MAT | MAT | AC | 1 | ZVC | - |
| Maytag | MYG | MYG | C | 1 | ZMY | WMY |
| MBNA | KRB | KRB | AC | 3 | ZK | WK |
| McDonald's | MCD | MCD | C | 3 | ZMC | WMN |
| McGraw-Hill | MHP | MHP | X | 2 | ZMP | WMP |


| MCI Worldcom | WCOM | LDQ | CP | 3 | ZQM | WQM |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| McKesson/HBOC MCK | MCK | CP | 2 | ZHG | WHG |  |
| MediaOne Group | UMG | UMG | A | 1 | ZUG | WUG |
| Medtronic | MDT | MDT | C | 2 | ZKD | WKV |
| MEMC <br> Electronic <br> Materials | WFR | WFR | A | 1 | - | WYC |
| Merck | MRK | MRK | C | 1 | ZMK | WMR |
| Merrill Lynch | MER | MER | AC | 1 | ZEM | WZM |
| Metromedia Fiber | MFNX | QFN | AC | 2 | ZFB | WOF |
| Micron <br> Technology | MU | MU | CP | 1 | ZGY | WGY |
| Microsoft | MSFT | MSQ | CP | 1 | ZMF | WMF |
| Minnesota <br>  <br> Manufacturing | MMM | MMM | C | 1 | ZMM | WMU |

(Table continued on next page)

Table 2.3
LEAPS Available August 1999 (Continued)

| Underlying Equity | Stock Symbol | Option <br> Symbol | Exchange Code | Cycle No. | 2001 LEAP | 2002 LEAP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mobil | MOB | MOB | C | 2 | ZMB | - |
| Monsanto | MTC | MTC | C | 1 | ZM | WMC |
| Morgan (J.P.) \& Co. | JPM | JPM | CX | 3 | ZJP | WJP |
| Morgan Stanley Dean Witter. | MWD | MWD | ACPX | 1 | ZWD | WWD |
| Motorola | MOT | MOT | A | 1 | ZMA | WMA |
| Nabisco Group | NGH | NGH | ACX | 3 | ZRJ | WRJ |
| Nabors Industries | NBR | NBR | ACX | 3 | ZRB | WRB |
| National Semiconductor | NSM | NSM | C | 2 | ZUN | WUN |
| Network Associates Inc. | NETA | CQM | ACP | 3 | ZNE | WNE |
| Newbridge Networks | NN | NN | CP | 3 | ZNW | WNW |
| News | NWS | NWS | ACX | 1 | ZLN | WLN |
| Nextel Communications | NXTL | FQC | C | 2 | ZFU | WFU |
| Nike | NKE | NKE | CP | 1 | ZNK | WNK |
| Nokia | NOK | NOK | AC | 1 | ZOK | WIK |
| Nordstrom | JWN | JWN | A | 1 | ZNZ | WNZ |


| Nortel Networks | NT | NT | C | 3 | ZOO | WNT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Northrop Grumman | NOC | NOC | C | 2 | ZOJ | WJO |
| Northwest Airlines | NWAC | NAQ | AC | 3 | ZWW | WAW |
| Novell | NOVL | NKQ | A | 2 | ZNN | WNN |
| Nucor | NUE | NUE | C | 1 | ZBN | WBN |
| Occidental Petroleum | OXY | OXY | C | 2 | ZXY | WXY |
| Office Depot | ODP | ODP | A | 1 | ZDP | WDP |
| Oracle | ORCL | ORQ | C | 3 | ZOR | WOQ |
| Orbital Sciences | ORB | ORB | AC | 3 | ZRI | WRZ |
| PacifiCare Health Systems | PHSY | HYQ | C | 2 | - | WHZ |
| Paine Webber Group | PWJ | PWJ | C | 1 | ZWJ | WWJ |
| PairGain Technologies | PAIR | PQG | C | 1 | ZGC | WGC |
| PeopleSoft | PSFT | PQO | ACP | 1 | ZPQ | WOZ |
| PepsiCo | PEP | PEP | C | I | ZPP | WP |
| Pfizer | PFE | PFE | A | 3 | ZPE | WPE |
| Pharmacia \& Upjohn | PNU | PNU | C | 1 | ZUP | WUP |
| Phelps Dodge | PD | PD | A | 1 | ZZP | WZP |
| Philip Morris Companies | MO | MO | A | 3 | ZMO | WRR |
| Pitney Bowes | PBI | PBI | A | 1 | ZBW | WBZ |


| Placer Dome | PDG | PDG | X | 3 | ZPD | WPD |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PMI Group | PMA | PMA | A | 3 | ZRW | WRW |
| PNC Bancorp | PNC | PNC | X | 2 | ZSM | WYL |
| Polaroid | PRD | PRD | C | 1 | ZRD | WRD |
| Potash of <br> Saskatchewan | POT | POT | C | 3 | ZPT | WPT |
| PPG Industries | PPG | PPG | X | 2 | ZP | WPN |
| Premiere <br> Technologies | PTEK | TQO | AC | 2 | ZTJ | WQJ |
|  <br> Gamble | PG | PG | A | 1 | ZPG | WPG |
| Providian <br> Financial | PVN | PVN | C | 3 | ZLA | WVR |
| Quaker Oats | OAT | OAT | X | 1 | ZQO | WQO |
| Qualcomm | QCOM | QAQ | C | 1 | ZLU | WLU |
| Qwest <br> Communications <br> Ralston Purina | RAL | RAL | C | 3 | ZWST |  |
| QWA | ACX | 1 | WWH |  |  |  |

(Table continued on next page)

Table 2.3
LEAPS Available August 1999 (Continued)

| Underlying Equity | Stock Symbol | Option Symbol | Exchange Code | Cycle No. | 2001 LEAP | 2002 LEAP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rambus | RMBS | BNQ | ACP | 2 | ZIX | WWO |
| Rational Software | RATL | RAQ | C | 1 | ZRA | WRA |
| Read-Rite | RDRT | RDQ | CP | 1 | ZJW | WJW |
| Reebok International | RBK | RBK | A | 1 | ZRK | WRK |
| Republic New York | RNB | RNB | X | 3 | ZJJ | WJJ |
| Rite Aid | RAD | RAD | CX | 1 | ZAD | WBV |
| SAFECO | SAFC | SAQ | C | 2 | ZLH | WGH |
| Safeskin | SFSK | FQK | A | 1 | ZFK | WFK |
| Safeway | SWY | SWY | AC | 3 | ZZO | WYF |
| Saks | SKS | SKS | X | 2 | ZSC | WSN |
| Santa Fe International | SDC | SDC | ACPX | 1 | ZEJ | WEJ |
| SAP | SAP | SAP | ACPX | 3 | ZSP | WTA |
| Sara Lee | SLE | SLE | A | 1 | ZZS | WZS |
| SBC <br> Communications | SBC | SBC | P | 1 | ZFE | WFE |
| Schering-Plough | SGP | SGP | CP | 2 | ZSG | WSG |
| Schlumberger Limited | SLB | SLB | C | 2 | ZZW | WUB |


| Schwab (Charles) | SCH | SCH | C | 3 | ZWS | WWS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Seagate Technology | SEG | SEG | A | 3 | ZTZ | WTZ |
| Sears Roebuck | S | S | C | 1 | ZS | WSI |
| Sepracor | SEPR | ERQ | C | 1 | ZQT | WQT |
| Skytel <br> Communications | SKYT | MMQ | C | 3 | ZME | WMM |
| SLM Holding | SLM | SLM | C | 1 | ZMZ | WQH |
| SmithKline Beecham | SBH | SBH | P | 2 | ZPF | WPF |
| Solectron | SLR | SLR | C | 1 | ZSR | WRL |
| Solutia | SOI | SOI | C | 1 | ZOA | WOL |
| Southwest Airlines | LUV | LUV | C | 3 | ZUV | - |
| Sovereign Bancorp | SVRN | SQV | X | 1 | ZSW | WSW |
| Sprint (FON Group) | FON | FON | CX | 2 | ZON | WO |
| $\begin{aligned} & \text { Sprint (PCS } \\ & \text { Group) } \end{aligned}$ | PCS | PCS | ACPX | 2 | ZVH | WVH |
| Storage <br> Technology | STK | STK | C | 3 | ZSK | WSK |
| Sun <br> Microsystems | SUNW | SUQ | CP | 1 | ZSU | WSU |
| Sunbeam | SOC | SOC | A | 1 | ZUM | WZO |
| SunTrust Banks | STI | STI | P | 1 | ZNJ | WNJ |


| Sybase | SYBS | SBQ | P | 3 | ZYB | WYB |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Telefonica de <br> Argentina | TAR | TAR | ACP | 1 | ZTD | WTD |
| Telefonos de <br> Mexico | TMX | TMX | ACX | 2 | ZTE | WTE |
| Tellabs | TLAB | TEQ | P | 3 | ZEP | WEP |
| Tenneco | TEN | TEN | A | 2 | ZTG | WTG |
| Terex | TEX | TEX | AX | 1 | ZYW | WEI |
| Texaco | TX | TX | A | 1 | ZTC | WTC |
| Texas <br> Instruments | TXN | TXN | C | 1 | ZTN | WTN |
| 3Com | COMS | THQ | CP | 1 | ZTH | WTH |
| Tiffany | TIF | TIF | X | 2 | ZFF | WTF |
| Time Warner | TWX | TWX | CX | 3 | ZTW | WTY |
| TJX Companies | TJX | TJX | C | 1 | ZJT | WJT |
| Tommy Hilfiger | TOM | TOM | C | 2 | ZSO | WSV |
| Toys "R" Us | TOY | TOY | C | 3 | ZTY | WYT |
| Table continued on next page) |  |  |  |  |  |  |

Table 2.3
LEAPS Available August 1999 (Continued)
\(\left.$$
\begin{array}{lllllll}\text { Underlying Equity } & \begin{array}{l}\text { Stock } \\
\text { Symbol }\end{array} & \begin{array}{l}\text { Option } \\
\text { Symbol }\end{array} & \begin{array}{l}\text { Exchange } \\
\text { Code }\end{array}
$$ \& Cycle No. \& 2001 <br>

LEAP\end{array}\right]\)| 2002 |
| :--- |
| LEAP |


| VLSI Technology | VLSI | VLQ | AC | I | ZQV | WQU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Vodaphone/AirTouch | VOD | VOD | AC | 1 | ZYE | - |
| Wal-Mart Stores | WMT | WMT | C | 3 | ZWT | WWT |
| Warner-Lambert | WLA | WLA | A | 1 | ZWL | WWL |
| Washington Mutual | WM | WM | A | 1 | ZWI | WWI |
| Waste Management | WMI | WMI | ACX | 1 | ZUY | WUZ |
| Wave Systems | WAVX | AXU | ACP | 2 | ZKW | WEO |
| Wells Fargo | WFC | WFC | AP | 1 | ZWF | WWF |
| Wendy's | WEN | WEN | P | 3 | ZVE | WVE |
| Williams Companies | WMB | WMB | C | 2 | ZXE | WYM |
| Winstar Communications | WCII | WQS | AC | 1 | ZRX | WWR |
| World Access | WAXS | WXQ | ACX | 1 | ZNC | WCD |
| Xerox | XRX | XRX | CP | 1 | ZXR | WXR |
| Xilinx | XLNX | XLQ | CP | 3 | ZXJ | WXJ |
| Yahoo | YHOO | YHQ | ACPX | 1 | ZYH | WYH |
| YPF Sociedad Anonima | YPF | YPF | AC | 1 | ZYP | WYP |

## 3-

## Basic Strategy

## The Underlying Premise

As stated earlier, option premiums do not reflect inflation or the growth prospects of the underlying issue. This does not matter much for standard options because of the relatively short time to expiration-eight months at the most. It does matter, however, for LEAPS, which can expire as many as 30 months later. By not taking inflation or the growth prospects of the underlying issue into account, the level of risk of a put option winding up in the money and being exercised against the writer appears to be larger than it really is. As a result, premiums for long-term put options are often overpriced with respect to the true level of risk involved. A quick glance at the tables in Appendix C shows why the chances of a LEAP put winding up in the money are that much smaller when inflation and growth prospects are taken into account.

As an example, suppose you were considering the sale of an at-the-money put on a stock priced at $\$ 100$ a share whose volatility was 0.40 and that pays no dividend. The risk-free interest rate is currently 6 percent. You are considering the sale of a standard put expiring in three months or a LEAP put expiring in two years. From Table A. 5 in Appendix A we see that the premium for the three-month European-style put is $\$ 7.185$ a share, and for the 24 -month LEAP put it is $\$ 15.815$ a share. Neither premium reflects the earnings growth rate of 15 percent a year forecast for the company. From Table C. 5 in Appendix C we see that without growth in earnings or the stock price, the probability of the
three-month put winding up in the money is 0.431 , while for the 24 -month LEAP put it is 0.310 .

For a 15 percent growth in earnings, however, Table C. 32 shows that the probability of winding up in the money falls to 0.358 for the three-month put and to just 0.153 for the 24-month LEAP put. (These probabilities hold independently of whether a European- or an American-style pricing formula was used to determine the premiums.) Thus, the effect of earnings growth was to lower the relative chances of financial exposure by only about one-sixth $(0.358 \div 0.431=0.831)$ for the three-month put but by over one-half $(0.153 \div 0.310=0.494)$ for the 24 -month LEAP put.

The analogy isn't quite exact, but I think of this as being akin to selling earthquake insurance to homeowners on the East Coast based on the claim rate in California or health insurance to nonsmokers based on the claim rate for smokers. Yes, there will be claims-earthquakes happen everywhere given enough time, and even nonsmokers get sick-but on a statistical basis there will be far fewer claims from East Coast homeowners and nonsmokers. Or in the case of LEAPS, from the put holders on growing companies.

## The Fundamental Approach

From the foregoing premise, it seemed to me that a good investment strategy was to sell LEAP puts on companies whose long-term prospects were so good, and balance sheets so strong, that the possibility of being assigned the stock or otherwise incurring a loss was remote. The premiums received could then be used to purchase more of my favorite stocks. At the time I started doing this, in 1993, the number of long-term LEAPS available was much smaller than it is today. When the CBOE introduced LEAPS in October 1990, it started with calls on just 14 stocks. LEAP puts were first instituted about a year later. By 1993, equity LEAPS were available on only 100 or so issues, about one-third the number that were available by 1999.

In the beginning, I approached LEAP option selection very conservatively. The underlying stocks had to have Standard \& Poor's ratings of B+ or better, the exercise prices had to be at least two price intervals out of the money, the expiration date had to be at least 15 months away, and sales were limited to a single contract. In each instance, the under-
lying issue also had to be a large-cap, blue chip company that, if assigned to me, would fit right into my portfolio of conservative stocks. As time progressed, I relaxed several of these restrictions, selling LEAP puts on stocks with S\&P ratings of B or better and expiration dates as close as eight months away, and sales were expanded to multiple contracts. Exercise prices were set at the money if I relished the thought of being assigned the stock and set one strike interval below that if I was more or less indifferent to having to purchase that issue for my equity portfolio.

As a rule, I also try to avoid stocks with volatilities that are extremely low or extremely high. I often calculate the volatility of a stock using one or both of two different methods. The first is by a direct calculation based on the daily price history over the past 12 months. This history is available without charge from many Internet providers (I use America Online), and the calculation is readily performed using the method described in Chapter 13. The second method is to calculate the implied volatility level that is derivable from quoted option premiums by means of the approach described in Chapter 14.

Stocks with extremely low volatilities will typically have premiums too low to justify the commission and margin requirement involved. Stocks with extremely high volatilities (say 0.75 and above) typically represent issues that are so unstable that the prospects of doubling or nothing (bankruptcy) may be commensurately equal. This is not to say that you should avoid stocks with moderately high volatilities. Tables C. 1 though C.4, for example, show that the chances of in-the-money puts expiring in the money decrease significantly with increasing volatility, while Table C. 5 shows that the chances of at-themoney puts expiring in the money are roughly independent of volatility. In any event, I try to write LEAP puts of such combinations of strike price, expiration date, and volatility that they will generate premiums of $\$ 500$ or more per contract. I don't always get that, but that is the standard figure I shoot for. By the way, the largest premium I have generated to date for an out-of-the money LEAP put was $\$ 3,600$ per contract (for the January 2000 LEAP puts, strike $\$ 160$, at the time Dell Computers was at $\$ 180$ in July 1997). Larger premiums than this are available on equities with far higher volatilities, such as Internet stocks with little (if any) earnings and little (if any) operating history.

Because of the relatively large premiums involved, I estimated that the net cost (strike price less premium received) of any stock assigned to me would be in most instances less than the market price at the time the option was exercised. That is, suppose a stock is trading for $\$ 102$ a share and a LEAP put with strike price $\$ 100$ is written for a premium of $\$ 12$. At expiration, suppose the stock has fallen ten points to $\$ 92$ and is therefore assigned. My effective purchase price is thus $\$ 90$ ( $\$ 102$ less $\$ 12$ ), $\$ 2$ a share below market value. This ignores commissions, but the effects of the latter are not as great as you might think. Whatever commissions are charged for purchase of the stock are going to be offset in good measure by the interest earned on the $\$ 1,200$ premium (or imputed interest if the premium was used to buy stock) over a period of as long as 30 months.

## Margin and Collateral

Although put writers are not going on margin (they are not borrowing money from their brokers to buy securities), they do have to be approved to open a margin account. There is no minimum dollar requirement to open a margin account as such, but brokers will typically require equity (securities and cash) of at least $\$ 25,000$ and evidence of stock market experience before permitting customers to sell puts.

The collateral requirement for writers of at-the-money puts is 20 percent of the value of the underlying stock plus the premium received. (For deep out-of-the-money puts this percentage drops to just 10 percent.) In the previous example, 100 shares of the underlying equity was worth $\$ 10,200$ at the time the LEAP put was sold. To enter this transaction, you would have to have at least $\$ 2,000$ in collateral (the exact formula is a complex one and is discussed in Chapter 4). The $\$ 25,000$ in your margin account would in principle be sufficient to collateralize a dozen such contracts. You would not want to do this, of course, because collateral requirements are calculated on a daily basis, and any downturn in the market, no matter how temporary, would result in a margin call.

My comfort level if I were a relatively small investor with $\$ 25,000$ in stock market assets would be the sale of two such put contracts. In the event that the option was unexpectedly exercised, the $\$ 25,000$ in the account plus $\$ 2,400$ in premiums would be more than enough to
cover the acquisition cost of the 200 shares of stock at $\$ 100$ a share that would have to be purchased under the terms of the option contract. As my stock market account grew to an intermediate size of $\$ 250,000$, my comfort level expanded to a limit of 20 contracts at any one time. With enough time, a large account with $\$ 2.5$ million would be sufficient to handle 200 contracts comfortably. I hope you succeed in achieving this level.

## Selection and Timing

Over the years, I have found that which long-term option contract to enter is much more important than when to enter it. In this sense, dealing in long-term LEAPS employs much the same buy-and-hold philosophy that I have used to purchase stocks. This approach differs markedly from that taken by short-term equity and options traders, who may buy an issue at 10:00 AM and sell it by 2:00 PM, hoping for eighth-and quarterpoint increases (or decreases). To adequately describe the intensity of a trading environment is difficult. Suffice it to say that for a trader, news that the kitchen is on fire is an unpardonable distraction.

My approach to the selection of a LEAP put to sell is the same as my approach to choosing a stock. In a certain sense, it is easier to pick a good LEAP option than to pick a good stock because the universe of stocks contains thousands of issues and the screening needed to separate the potentially good ones from the rest can occupy a substantial amount of time. On the other hand, there are 300 or so stocks with LEAPS, and it is easy enough to track their historical performance by creating a hypothetical portfolio and using almost any Internet provider to update it automatically on a daily basis. Although the number of stocks in any one portfolio may be restricted to, say, 100 issues, most providers will permit multiple portfolios.

The purpose of this book is not to tell you how to select good stocks-there are plenty of books and other informational resources for that. I personally use a number of free, Internet-accessible information sources to narrow the field of eligible stocks, among them the Web sites described in detail in Chapter 16. These include Hoover's StockScreener, Wall Street Research Net, Yahoo !Finance, StockSmart, Zacks Investment Research, FinancialWeb, Daily Stocks, and the broad-based services provided through America Online. (America Online is not free,
of course, but you have to pay somebody to access the Internet.) The various criteria I bring to bear can be summed up in two questions: (1) Would I buy this stock in its own right for my long-term stock portfolio? and (2) Would I mind having it unexpectedly "put to me" at the net acquisition cost (strike price less premium received) as a result of temporary market conditions and a panicky put holder?

As far as timing is concerned, I follow the same sort of dollar cost averaging procedure used by millions of conservative, long-term equity investors. To minimize the impact of fluctuating prices, dollar cost averaging adherents invest the same amount of money in stocks on a consistent, nonvarying periodic schedule. I follow an analogous procedure by selling the same dollar value of LEAP puts almost every month throughout the year. This procedure means that I do not have to guess whether stock prices are high or low, or whether they are going to go higher or lower over the short run.

## Tactical Decision Making

If selecting underlying equities by means of these methods is thought of as strategic decision making, choosing the appropriate parameters of the individual LEAP contracts can be though of as tactical decision making. The three independent parameters are the strike price, expiration date, and number of contracts written. Which to select will depend on how much you are willing to risk (i.e., the chance of exercise and assignment) to obtain a given reward (i.e., the LEAP premium offered).

Strike prices can range from deep out of the money to deep in the money. In addition, there will typically be two or three expiration dates available, such as January 2001, January 2002, and (when opened) January 2003. The number of contracts will depend on the risk/reward ratio, of course, but will more likely be a function of the margin, collateral, and assets needed to comfortably handle the transaction(s) involved. Whether to select a conservative, aggressive, or neutral at-the-money approach to strike prices depends on a number of factors that will be discussed in detail in the chapters to come. In situations where more than one contract for a given equity is being considered, the best position may turn out to be a mix of strike prices and expiration dates.

## Selling Puts versus Good-till-Canceled Orders

As I've said, my main objective in selling LEAP puts is to pocket the option premium and let the option expire worthless. In addition to this, I frequently sell LEAP puts when my specific goal is to have the option exercised against me as a way of acquiring stock at a net price significantly below the current market value. In this situation, I select a strike price a few steps higher than the one I would normally use for the pure premium retention play. Naturally, the higher the strike price, the greater the premium received and the higher the chances that the LEAP put will be assigned to me. The strike price so selected is typically one or two steps into the money-but rarely more than this. If too deep an into-the-money put is sold, the net acquisition cost (strike price less option premium) may not be significantly below the current market value.

Although some would say that selling in-the-money puts is a high-risk tactic, it is not very different from acquiring stock using a good-till-canceled (GTC) order at a price pegged that much below the current market value. That is, suppose a stock with a volatility of 0.40 that is paying no dividend sells for $\$ 100$ today. Assume the risk-free interest rate is 6 percent. Suppose investor A places a one-year GTC order to buy the stock at $\$ 92$ a share, and investor B sells a LEAP put with strike price $\$ 110$, expiring in 12 months.

Table A. 3 in Appendix A shows that for a risk-free interest rate of 6 percent and for a stock paying no dividends, the corresponding put premium is almost exactly $\$ 18$ per share. If the stock closes above $\$ 110$ (without an intermediate dip), investor B is the clear winner because the $\$ 18$ premium is retained. If the stock closes between $\$ 92.01$ and $\$ 110$ (again without an intermediate dip to $\$ 92$ or below), investor B is again the winner as his or her effective price will be $\$ 92$ for a stock worth somewhere between that figure and $\$ 110$. And if the stock closes at or below $\$ 92$, then the cost basis for both investors will have been $\$ 92$ a share and their (unrealized) losses will be close to identical.

In actual practice, investor B will be ahead even in the latter situation for two reasons: (1) the option premium of $\$ 1,800$ will have been earning interest over the one-year period, and (2) the GTC order will
more likely than not have been triggered earlier than the assignment, thereby incurring a larger opportunity (or borrowing) cost on the $\$ 9,200$ needed to purchase the stock. About the only circumstances in which investor A would come out ahead is if the stock were to temporarily fall to $\$ 92$ (or below), triggering the GTC order, and then close above $\$ 110$ without the LEAP option ever having been exercised. Almost everyone agrees that the use of GTC orders at prices pegged below market is a sound and conservative approach to stock acquisition. Selling puts to achieve the same ends can be even more cost effective.

## Sometimes Life Deals You Lemons

Over the years there have been few instances when a LEAP option proved unprofitable to me. I do not mean to imply by this that the numerous LEAP puts I sold almost always expired out of the money and were therefore worthless to the option holder. On the contrary, on a certain number of occasions I did have to utilize mitigation procedures in order to preserve my profits and eliminate the potential for exercise and assignment against me. It was often the case that an out-of-the-money LEAP put went into the money along the way because of subsequent price dips in the underlying issue.

On only 6 occasions (out of more than 600 transactions) was I ever required to purchase the underlying issue because an option was exercised against me with months to go before the expiration date. The reason for this is simple: option holders of LEAP puts in most instances have bought them for insurance purposes and hope for recovery and a rise of the stock price to the same extent as the option writer. Under normal circumstances, they will not exercise the right to put the stock to the option writer until close to the end of the insurance period, as the expiration date approaches.

In all such instances, however, assignment actually turned out to be a blessing. That's because the assignment relieves you of the time value component of the then current option premium. A specific example will make this clear. Suppose you sold a LEAP put on a fairly volatile stock such as America Online at a time when the stock price was $\$ 125$. The strike price selected was $\$ 100$, the expiration date was 24 months away, the risk-free interest rate was 6 percent, and the volatility was 0.65 .

Using the procedures developed in Chapter 15, the premium for an American-style LEAP put is going to be $\$ 23.57$ ( $\$ 2,357$ per contract).

Suppose that one year later the price of America Online has tumbled to $\$ 80$ a share. Ouch! Assuming no change in volatility and interest rate, the corresponding premium of an American-style put with 12 months to expiration, stock price of $\$ 80$, and strike price of $\$ 100$ is going to be $\$ 31.03$ ( $\$ 3,103$ per contract). The LEAP contract you wrote now commands a premium $\$ 7.46$ more than what you originally received, and if you were to buy back the put and close the position (without instituting any repair and recovery strategy), your net loss per contract would be $\$ 746$. Very soon thereafter, the option holder exercises the put and you are assigned the AOL stock for $\$ 100$ a share. You decide to immediately sell the shares for $\$ 80$, receiving $\$ 20$ a share less than what you just paid for them. Taking account of the original premium, though, being assigned has thus transformed the potential loss of $\$ 746$ into an overall profit of $\$ 357$ ( $\$ 2,357$ less $\$ 2,000$ ) per contract.

## Risk Reduction Using Spreads

One way of reducing risk is to set up a hedging strategy. This is particularly useful if you are going to sell LEAP puts on lower-'rated companies or those known to be highly volatile. One strategy I have occasionally used is to simultaneously purchase a LEAP put with a strike price well below the strike price of the LEAP put I was selling.

If the same expiration date is selected, this is referred to as a bull put spread. It may not always be possible to do this, however, because of the narrow set of strike prices that may be available (each 30-month LEAP series is ordinarily introduced for just three strike prices: one at the money, one in the money, and one out of the money). If that is the case, the LEAP put purchased with a lower strike price will have an expiration date one year prior to that of the LEAP put sold, a hedging strategy usually referred to as a diagonal put spread. This short leg of the spread can be subsequently rolled out to match the expiration date of the longer LEAP put whenever that strike price opens up.

What this hedging technique does is reduce potential profit and potential loss. Profit is reduced because the net premium received is going to be the difference between the premium received from the sale of the higher-strike LEAP put and the premium paid for the purchase

Table 3.1
European-Style 30-Month Put Premiums as a Function of Strike Price

$$
\begin{aligned}
& \text { Stock Price }=\$ 100 \\
& \text { Volatility }=0,35
\end{aligned}
$$

## Strike Price

$\$ 100$

95

90

85

80

75

70

65

60

## LEAP Premium

\$14.035
11.952
10.032
8.283
6.708
5.312
4.096
3.061
2.201
of the lower-strike LEAP put. On the other hand, the maximum amount of financial exposure is reduced from that of the strike price of the LEAP put sold to that of the difference between the two strike prices involved.

To estimate the costs of lower-strike LEAP puts, the set of tables in Appendix A has been prepared showing the theoretical values for European-style LEAP put premiums. Like the figures in Table 1.2, they are based on a stock price of $\$ 100$, a risk-free interest rate of 6 percent, and no dividend. The premiums shown were calculated using the simple Black-Scholes pricing formula for European-style options that is described in Chapter 14. In Table 2.1, we noted that the theoretical premium for a 30 -month, at-the money LEAP put for a stock priced at $\$ 100$ with volatility 0.35 was $\$ 14.035$ per share ( $\$ 1,403.50$ per contract). If we lower the strike price in steps of $\$ 5$, the corresponding premiums, as extracted from the tables in Appendix A, are shown in Table 3.1.

Suppose, for example, we hedged the 30 -month, at-the-money LEAP put by purchasing
the corresponding 30 -month LEAP put with a strike price of $\$ 80$ (assuming it was available) for $\$ 6.708$ per share. The net profit per contract would be $\$ 1,403.50$ less $\$ 670.80$, or $\$ 732.70$, still a sizable amount. The maximum potential exposure, however, drops from $\$ 100$ (without an offsetting LEAP put) to just $\$ 20$ per share (the difference between the two strike prices involved).

If the 30 -month LEAP put with the $\$ 80$ strike was not available, you could set up a partial hedge by purchasing an 18-month LEAP put with strike price $\$ 80$ for just $\$ 4.908$ a share, as indicated in Table A.9.

The net premium this way would be $\$ 1,403.50$ less $\$ 490.80$, or $\$ 912.70$ per contract. As the expiration date of the shorter LEAP put approached, you could close out both LEAPS, replace the expiring one with a 12 -month LEAP put whose expiration date matched that of the original 30 -month LEAP put, or let it expire without replacement because the price of the underlying stock was now significantly higher (say 15 percent or more) than its original market value, thus transforming the original at-the-money put into one that was considerably out of the money.

## Using Rollouts to Recover

Let's consider again the example when at the time the stock price is $\$ 102$ a share, a LEAP put with strike price $\$ 100$ is sold for a premium of $\$ 12$ a share. Suppose further that as the expiration date had approached, the stock had fallen ten points to $\$ 92$. Rather than accept assignment, the idea now is to roll the option out and down. The first step in doing this is to buy back the put, thereby closing out your position in the original option. Because expiration is relatively close (presumably a month or less away), closing out the option will cost not much more than its intrinsic value of $\$ 8$ a share ( $\$ 100$ less $\$ 92$ ). To be conservative, suppose this is $\$ 9$ a share, or $\$ 900$ to close the contract of 100 shares. At the same time, you sell a LEAP put whose expiration date is two years away (the rollout) and with a strike price of $\$ 90$ (the rolldown).

Suppose the premium generated from the sale of this replacement LEAP put is again $\$ 1,200$. The overall effect of this maneuver is to net another $\$ 300$ ( $\$ 1,200$ received less the $\$ 900$ outlay) for an overall profit of $\$ 1,500$. Doing this also gives the underlying stock an additional two years to recover. Note that recovery no longer means coming back to the original $\$ 100$ level. As far as you, the option writer, are concerned, being at or above $\$ 90$ in two years is going to be good enough. This process can be continued indefinitely, in most instances, until such time as the stock price stabilizes.

Suppose the premium on the replacement LEAP put happened to be less than the closeout price of the prior LEAP put and is, say, $\$ 700$. In that situation, the net out-ofpocket cost would be $\$ 200$ ( $\$ 700$
received less the $\$ 900$ outlay). This offsets the original $\$ 1,200$ premium by $\$ 200$ but still results in an overall profit of $\$ 1,000$.

In rare instances a replacement LEAP put may not be available, a situation indicated by the occasional dashes in Table 2.3. (The primary reason this occurs is because of announced or pending mergers and acquisitions that never materialize.) Depending on how you feel about the company and its prospects, the simplest thing to do under these circumstances is to close out the option or accept assignment. This situation has never happened to me.

It is possible, of course, to incur a loss as a result of writing a naked put. The worst-case situation theoretically is where the stock price falls to zero as a result of bankruptcy or total financial catastrophe. It would be a truly unusual circumstance if one of the big-cap firms underlying almost all LEAPS went out of business, however. For a big-cap stock, a more credible worst-case situation might be a 25 percent decline in stock price as a result of a general market correction (in the unusually sharp correction of October 19, 1987, the market fell 22.6 percent). If the price of the stock in our example thereby fell from $\$ 102$ to $\$ 76.50$ and the stock was assigned to you at the strike price of $\$ 100$, the immediate financial exposure would be the strike price of $\$ 100$ less the market value of $\$ 76.50$ plus the premium of $\$ 12$, or $\$ 11.50$ per share. From Table A.5, we see that by immediately writing a near-the-money LEAP put with a strike price of $\$ 75$, we would expect to receive a premium of about $\$ 10$ for an expiration date 24 months away $(0.75 \times \$ 13.314$ $=\$ 9.99$ ). If this were done and the stock didn't decline further, the overall loss would be $\$ 11.50$ less $\$ 10$, or just $\$ 1.50$ a share. This potential loss of $\$ 150$ per contract under the circumstances described is small in comparison to the potential benefits.

## A Double-Glove Approach

Medical or rescue workers facing uncertain situations often put on an extra pair of gloves for added protection. Analogously, it is possible for you to do the same when future prospects or other market conditions are not as strong as you would like. To ensure double protection in selling LEAP puts, you can sell a put that is at least one strike interval below the at-the-money level and then additionally hedge by pur-
chasing a LEAP put that is several strike intervals below that one. The premiums can still be significant.

Suppose the stock price is $\$ 100$ a share. Looking at Table 3.1, if you were to sell a LEAP put with strike price $\$ 95$ and buy one with strike price $\$ 80$, your net premium would be $\$ 1,192.50$ less $\$ 670.80$, or $\$ 521.70$ per contract. Your maximum financial exposure would now be $\$ 95$ less $\$ 80$, or $\$ 15$ per share. This double-glove approach is my favorite one in those marginal situations involving stocks with higher volatilities and/or lower ratings that might have otherwise been eliminated from consideration.

## Protective Stops

There is yet another method of protecting option positions that is theoretically available, namely the use of stop and stop-limit orders. For call or put option owners, a stop sell order is an instruction to the broker to sell (thereby closing) a position at a specified price or at the best price below it if it is unavailable. A stop-limit sell order is an instruction to sell (thereby closing) a position at a specified price and no other. For call or put writers, a stop buy order is an instruction to the broker to buy (thereby closing) a position at a specified price or at the best price above it if it is unavailable. A stop-limit buy order is an instruction to buy (thereby closing) a position at a specified price and no other.

As an example of a stop buy order, suppose you had written a LEAP put for a $\$ 10$ premium and would like to buy it back and close your position if it goes to $\$ 12$. If you entered a stop-limit buy order for $\$ 12$ and the price jumped from anywhere below $\$ 12$ say, to $\$ 12.25$, your transaction would not be executed. If you had entered a stop buy order for $\$ 12$, under the same circumstances your position would be closed out for $\$ 12.25$.

The use of stop buy or stop-limit buy orders seems at first blush like an ideal way to hedge against an unanticipated move in the wrong direction (downward) for LEAP put writers. The difficulty is in the execution. Although all four stock exchanges that handle listed options (CBOE, American, Philadelphia, and Pacific) permit the use of stop and stop-limit orders, as a matter of course most brokerage firms will not accept option stop orders or stop-limit orders from individual cus-
tomers. One reason commonly cited by brokerage houses for this is the fact that the rules for option stop orders and option stop limits vary from exchange to exchange.* Another reason is the inability of in-place computer software and communication systems to reliably handle the complex instructions that must be wired to the trading floor. Stop buy and stop-limit buy orders are everyday occurrences on the stock exchanges but are typically done on behalf of institutional investors or those having direct links to the floor traders.

There is another reason I prefer not to use stop orders or stop-limit orders (even if I could readily do so). Over a multiyear period, the steady earnings growth of a solid company will result in a stock price movement up and away from the specified strike price. However, it is quite possible to experience a short-term price decrease in the underlying stock because of normal volatility in the equity markets. Once stop and stop limit orders are triggered because of a temporary downturn in stock price, it is not possible to capitalize on the eventual recovery in stock price and the associated erosion in the LEAP put that was in all likelihood going to expire worthless.

One more reason I don't like to use stop orders is because they are executed in a different manner for options than for stocks. Suppose you owned a stock that had a bid price of $\$ 10$ and an asked price of $\$ 10.25$, and you submit a stop loss order at $\$ 9$ to protect your position. If the bid/asked falls to $\$ 9 / \$ 9.25$, your trade will be executed because the price you want to sell at matches the bid price offered by buyers.

This would not be the case if the same situation involved an option, however. By the rules of the game, your $\$ 9$ stop loss order would not go off until either the asked price reached $\$ 9$ (in which case the bid might be $\$ 8.75$ ) or a trade went off at $\$ 9$, whichever occurred first. The analogous situation holds with respect to stop buy orders. Difficulties in trying to explain all this to customers may be the real reason brokerage houses will not accept stop orders on options.

[^3]
## Timing the Market

There may be individual investors who are good at timing the market, but I am not one of them. For this reason, I adopted a long-term, buy-and-hold approach to stocks and a regular, almost dollar cost averaging, approach to acquiring stocks during 30 years of investing. I have tried to adopt this philosophy with regard to options activity, selling just a few LEAP puts per month throughout the year rather than attempting to jump in and do it all during the three-month window in June, July, and August, when the new round of LEAPS is being established.

On the other hand, I do not ignore market conditions. When the market is especially volatile, I will often hedge by selling LEAP puts that are further out of the money than I would otherwise. Doing this is especially useful when the market appears overbought and a market correction appears possible. Of course, if such a market correction appears likely, I usually suspend selling LEAP puts and adopt a wait-and-see approach.

## 4-

## Margin

## Introduction

Writers of naked puts and uncovered calls are considered to be short the stock because of the obligation of the option writer to purchase the underlying equity should the option holder exercise his or her rights. As a result, writers of naked puts and uncovered calls must maintain margin accounts in much the same way that any short seller does. Because of the potential need to purchase stock or close out positions, investors must have sufficient collateral in their accounts (in the form of capital and/or equities) to ensure that such obligations can be met. For writers of naked puts and uncovered calls, the collateral required is the greater of:
$0.20 \times$ Stock Price - OTM Amount + Current Premium [1]
or
$0.10 \times$ Stock Price + Current Premium [2]
The OTM amount in the first formula is the amount by which the option is out of the money. For puts this is defined as the amount by which the stock price exceeds the strike price. For calls this is defined as the amount by which the strike price exceeds the stock price. By regulation, this collateral must be maintained in a margin account, and for that reason it is often referred to as the margin required.

## Examples

In late May 1999, XYZ Corporation is at $\$ 53.375$, and you write a January 2001 LEAP put with strike price $\$ 55$. The stock pays no dividend and has a volatility of 0.35 . The risk-free interest rate is 6 percent. From the tables in Appendix B, or using the computer algorithm in Chapter 15, the premium for an American-style put with 20 months to expiration comes to $\$ 8.28$. Based on this, the initial margin requirement for this slightly in-the-money option is calculated as $0.20 \times \$ 53.375 \times 100+\$ 8.28 \times 100$, or $\$ 1,895.50$. (Note that 10 percent of the stock price plus the premium would only be $\$ 533.75+\$ 828$, or $\$ 1,361.75$.)

Suppose, six months later, that XYZ's stock has moved up to $\$ 58.50$ a share. With 14 months to expiration, the premium for that option will have fallen to $\$ 5.46$. The current margin requirement for this option is $0.20 \times \$ 58.50 \times 100-(\$ 58.50-\$ 55) \times 100+\$ 5.46$ $\times 100$, or $\$ 1,366$ ( 10 percent of the stock price plus premium would only be $\$ 585+$ $\$ 546$, or $\$ 1,131$ ).

Further suppose, six months later, that XYZ's stock has moved up to $\$ 62.75$ a share. With just eight months to expiration, the premium for that option will now have fallen to just $\$ 2.87$. The margin requirement for this option is now $0.10 \times \$ 62.75 \times 100+\$ 2.87 \times$ 100 , or $\$ 914.50$ (the regular formula gives $0.20 \times \$ 62.75 \times 100-(\$ 62.75-\$ 55) \times 100+$ $\$ 2.87 \times 100$, or $\$ 767$ ).

Now suppose that, some time after, XYZ's stock zooms to $\$ 150$ a share (perhaps due to a buyout offer) and that the premium for that option falls essentially to zero. The margin requirement for this option is now $0.10 \times \$ 150 \times 100$, or $\$ 1,500$. This amount is greater than the $\$ 914.50$ margin required when the stock was at $\$ 62.75$ and even more than the $\$ 1,320$ margin required when the stock was only at $\$ 58.50$ a share. The put is getting safer and safer, yet the margin requirement is getting larger and larger!

The reason this paradox occurs is simply that the margin formulas used here were originally developed for uncovered (naked) call options: as the stock price increases, the greater the exposure to the call writer and the greater the margin has to be to ensure the writer's ability to meet his or her obligation (either to purchase the stock or buy back the call).

Rather than develop alternative formulas for put options, the regulators simply adopted the same rules for use with puts. If the margin requirement becomes too high because of this quirk, the solution for investors is rather easy: simply buy back the option and close the position. A full-service brokerage firm that wants your business will often charge just a nominal amount to close out an essentially worthless option under such circumstances. It is in its best interest to do so, for this permits investors to write additional puts and generate further commissions on an immediate basis rather than waiting for the original option to expire. If your broker does not wish to discount the commission under these circumstances, you should consider finding one who does.

## Collateral Requirements

The amount of collateral that must be maintained in your account is determined not only by the naked puts and uncovered calls you have written but by the extent to which you have purchased stocks, bonds, and other securities on margin using funds borrowed from the broker to finance some portion of their acquisition. Collateral (margin) requirements for these other types of securities can range from 50 percent for stocks and mutual funds all the way down to just 10 percent for U.S. Treasury obligations. Because the combined value of these assets may decrease, the net equity (market value less borrowings) must meet certain minimum maintenance requirements established by the Federal Reserve Board, the New York Stock Exchange, and the brokerage house itself.

The minimum required maintenance equity on marginable securities is 25 percent of asset value under Rule 431 of the New York Stock Exchange but is usually set at a higher level, such as 30 percent, by most brokerage firms. The net equity in your account must be greater than the sum of the minimum maintenance equity on the marginable securities and the required margin on the naked puts, uncovered calls, and any other margined transactions (such as short sales, with their margin of 150 percent of the short sale value - a figure set high enough to guarantee replacement of the borrowed securities and payment of interim dividends). For example, suppose your account has $\$ 100,000$ in marginable stocks and mutual funds and that the required margin for the puts you wrote is $\$ 25,000$. How much can you borrow against your
equity if the house rules require a minimum maintenance of 30 percent?
If $B$ is the amount borrowed, the remaining equity will be $\$ 100,000-B$. This figure must not fall below the sum of the $\$ 25,000$ option margin plus 30 percent of the $\$ 100,000$ market value; that is:
$\$ 100,000-B \geq \$ 25,000+0.30 \times \$ 100,000=\$ 55,000$
This shows that the maximum value that can be borrowed is $\$ 45,000$. It would be dangerous to borrow that much (or anywhere near that amount), because any decrease in equity value or increase in required option margin would instantly invoke a margin call, requiring the investor either to sell securities or to deposit enough cash or securities into his or her account to bring the account into balance. This is unfortunately exactly what happened to Victor Niederhoffer, who had bet the wrong way on an unbelievable number of currency and index options on the fateful day in October 1987 when the Dow Jones Industrial Average fell 554 points in a single session and he received an additional collateral call of $\$ 45$ million or so (which he did not have). His autobiography, Education of a Speculator, published in early 1996 by John Wiley \& Sons, is worthwhile reading.

All brokers produce a daily margin report for each client maintaining a margin account, showing security by security and option by option the margin requirement for each item and how the combined amounts stand in relation to overall limits independently imposed by the brokerage house and Rule 431 of the New York Stock Exchange. Most reports will also show when the net equity falls below the internal warning level of 50 percent specified by Regulation T of the Federal Reserve Board.

## Who Can Deal in Options?

There is much confusion as to which investors can utilize options as part of their investment programs. Fiduciaries (those administrating funds on behalf of others) are bound by the prudent-man rule of common law as well as by that of ERISA (Employees Retirement Income Security Act) for retirement accounts. Selling puts seems to meet the standard of the prudent-man rule in that the use of such a mechanism does not in and of itself violate the prudent-man rule. There are no
legal restrictions on the use of options by persons investing for themselves in nonretirement accounts; in this situation, limitations placed on options activity are matters between the investor and the broker(s) involved.

The prudent-man restrictions of ERISA do not apply to self-administered pension, retirement, and profit-sharing plans covering a single employee (or the employee and his or her spouse). The reasoning behind this exemption is that as long as the individual is making his or her own investment decisions, it is not the government's place to restrict the level of risk or the investment activities involved, however speculative they may be.

The reason there is confusion about this is because such a laissez-faire philosophy was not always the case. Prior to the enactment of ERISA in 1974, the Internal Revenue Service took the position that no security in a pension plan could be purchased at a price that exceeded the market price at the time of purchase. That would certainly seem to inhibit the writing of naked puts, because any assignment that took place would by definition involve the purchase of stock at (strike) prices greater than the market value whenever exercised. The word inhibit rather than prohibit is used here because, in theory, if the investor was nimble enough, an in-the-money put could be bought back and the position closed prior to the option being exercised, thereby circumventing such an occurrence.

In addition, Section 4975 of the Internal Revenue Code prohibits certain account holders from borrowing funds or using their funds as security for loans. This has been interpreted by some to mean that pension, retirement, and profit-sharing accounts cannot be margined or have the contingent liability of a stock purchase imposed by a naked put or uncovered call. This is not the case, however.

What it comes down to is the fact that it is the brokerage houses, which serve as custodians for IRAs, SEPs, Keoghs, $401(\mathrm{k}) \mathrm{s}$, and the like, that determine the extent to which options may be utilized as part of an individual's investment strategy. Some firms are so conservative that they discourage purchasing calls, protective puts, or even the sale of covered calls - even though a margin account is not needed to conduct any of these option activities. Some brokerage houses will not permit retirement accounts to purchase calls or protective puts, limit-
ing option transactions to the selling of covered calls alone. Even if option activities are permitted by the house rules, bear in mind that individual brokers may discourage such activities simply because of their unfamiliarity with, and lack of experience in, doing options.

Many brokerage firms do, however, extend margin privileges to pension, retirement, and profit-sharing plans so they can participate in a wider range of option activities, including the sale of naked puts. In such instances, the range and scope of option activities that brokerage houses permit depend on the experience, account balance, and investment objectives of the account holden

## Establish Your Comfort Zone

To allow for day-to-day fluctuations in the market, and even modest corrections in stock prices along the way, you will want to maintain enough collateral in your brokerage account to avoid virtually any threat of a margin call. How much more collateral to have on hand in relation to the maintenance requirements depends on the premium yield rate desired and the corresponding comfort zone. By the premium yield rate, I mean the dollars received in premiums from the sale of LEAP puts each year as a fraction of your overall portfolio account.

Premium yield is maximized when collateral is equal to the minimum margin requirement. To get some idea of what this might be, let's determine the margin requirements associated with the receipt of each $\$ 10,000$ worth of LEAP put premiums. From Table 2.1, we see that for a stock price of $\$ 100$ a share, premiums for a Europeanstyle at-the-money LEAP put for a stock with a midlevel volatility of 0.30 range from $\$ 8.892$ to $\$ 11.322$ per share ( $\$ 889$ to $\$ 1,132$ per contract) for times to expiration ranging from 12 to 30 months, respectively. For American-style at-the money LEAP puts, Table B. 5 shows the premiums ranging from $\$ 9.547$ to $\$ 13.276$ ( $\$ 955$ to $\$ 1,328$ per contract).

On this basis, we can adopt a conservative figure of $\$ 1,000$ in premiums per contract for every $\$ 100$ in stock price. Thus $\$ 10,000$ in premiums would be the amount received if we sold at-the-money LEAP puts on 10 contracts of a $\$ 100$ stock. The aggregate stock price on these ten 100 -share lots is $10 \times 100 \times \$ 100$, or $\$ 100,000$. Because the margin requirement on at-the-money options is 20 percent of the stock price (plus option premium), you would need $\$ 20,000$ in cash and
equities in your account to generate the $\$ 10,000$ in premiums. The premiums so received would have to be retained in your account as additional margin (but of course could be used to acquire more stock). If the average time to expiration was 18 months, the annualized premium yield would be $\$ 10,000 \div(\$ 20,000 \times 1.5)$, or 33.3 percent per year.

It would be foolish, of course, to sell anywhere near the number of options permitted by the margin requirements. As a practical matter, I would want to have at least three or four times the equity called for under the margin requirements in my account, or perhaps $\$ 60,000$ to $\$ 80,000$ in the situation described. Under these circumstances, the annualized premium yield would thus be $\$ 10,000 \div(\$ 70,000 \times 1.5)$, or roughly 10 percent per year. I have found that generating premiums equal to 10 percent of one's portfolio value is a readily achievable, conservative policy. When combined with dividends and capital appreciation, it can mean a substantial difference in the overall growth of an investor's portfolio.

## Earthquakes Happen

Historically, there have been days when the bottom seemed to drop out of the market. Whether triggered by a sudden collapse of a foreign stock market, an unexpected increase in interest rates, or other causes, these crashes can result in domestic stock markets falling 10 or 15 percent during the course of a day or week. On October 19, 1987, the market fell a record 22.6 percent in a single trading session, and a substantial number of investors who were short puts with expiration dates not far away were impacted significantly. Because the market recovered within 18 months, had the same investors been short LEAP puts with expiration dates up to 30 months away, the financial impact would have been significantly lessened. (Of course, LEAPS did not come into being until 1990, so this was not a possibility at the time.)

Events such as these, when they do occur, have a threefold impact on your portfolio. To start with, the value of your equity portfolio will likely decrease in the same proportion as the overall market. In addition to this, a great many of your short put positions may move from being out of the money to being in the money. And because of the manner in which margin is computed, the collateral requirements to main-
tain those short put positions may increase significantly (as they did for trader Niederhoffer).

In a worst-case scenario, your required margin could move from the minimum level of 10 percent to the maximum level of 20 percent of the value of the underlying equities. Such an occurrence could in principle trigger a margin call for additional collateral for very aggressive investors overpositioned with far too many short puts.

When this happens, I have always used the opportunity to make additional money while reducing the risk of eventual assignment. In most instances, market drops reflect oversold situations which are temporary in nature. When this happens, I immediately take advantage of the situation not only by rolling the puts that have gone into the money out and down, but also by increasing the number of contracts.

Let's go back to our previous example in which, in May of 1999, XYZ Corporation is at $\$ 53.375$ and you write a January 2001 LEAP put with strike price $\$ 55$ and receive a premium of $\$ 8.28$. The reason you confidently entered this transaction was because the company earned $\$ 2.50$ a share and earnings were projected to increase to between $\$ 2.90$ and $\$ 3$ in one year. As calculated earlier, the initial margin requirement for this option (based on 20 percent of the stock price plus the premium) is $\$ 1,895.50$. One year later, earnings are $\$ 2.94$ and XYZ moves up to $\$ 62.75$ a share. The premium for that option has fallen to $\$ 2.87$, for which the margin requirement for this option (based on 10 percent plus premium) falls to just $\$ 914.50$. Earnings are projected to go to $\$ 3.40$ to $\$ 3.50$ one year after that.

Now suppose that shortly after that, the market falls a whopping 15 percent, with the stock price dropping to $\$ 53.375$, thus wiping out an entire year's gain overnight. With eight months to expiration, the premium jumps to $\$ 6.03$, with a corresponding margin requirement of $0.20 \times \$ 53.375 \times 100+\$ 603$, or $\$ 1,670.50$, more than 1.8 times what it was the day before. Although you have taken a conservative approach to put writing, the aggregate impact on your overall margin requirements (because the market break has affected all your put positions in the same way) can be disconcerting. To compound matters, this option, like many of your other options, is now in the money, and early exercise at $\$ 55$ a share is a potential threat.

In situations such as this, the idea is to take advantage of the temporary slump and not only roll out the option, but also consider increasing the number of contracts involved. You therefore buy back the option for $\$ 603$ a contract and sell one or more LEAP puts on XYZ with expiration dates 20 months away (because the current LEAP put expires in eight months, there will be one that expires in 20 months; two months must pass before LEAPS with 30 -month expiration dates will open). You can be aggressive and write a LEAP put with the same strike price of $\$ 55$, write a slightly out-of-the-money LEAP put with strike $\$ 50$, or be conservative and write a LEAP put with strike $\$ 45$.

For a strike price of $\$ 55$, the premium will be $\$ 8.28$, for which the margin requirement will be $\$ 1,895.50$. For a strike price of $\$ 50$, the premium will be $\$ 5.83$, for which the margin requirement will be $0.20 \times \$ 53.375 \times 100-(\$ 53.375-\$ 50) \times 100+\$ 583$, or $\$ 1,313$. For a strike price of $\$ 45$, the premium will be $\$ 3.84$, for which the margin requirement will be $0.10 \times \$ 53.375 \times 100+\$ 384$, or $\$ 917.75$.

The appropriate decision here depends very much on how critical it is to maintain your margin requirements. If you are still well within your margin limit, you could keep the $\$ 55$ strike price, thus pocketing a net premium of $\$ 828$ less $\$ 603$, or $\$ 225$ per contract, with overall margin increasing from $\$ 1,670$ to $\$ 1,895$. If margin maintenance is of some concern, you could sell five contracts with a strike price of $\$ 50$ for every four you buy back, thus essentially breaking even on the transaction after paying commissions while slightly decreasing margin requirements (\$1,670 margin on each of four contracts is $\$ 6,680$, and $\$ 1,313$ margin on each of five contracts is $\$ 6,565$ ). If margin requirements are of great concern, you might sell three contracts with a strike price of $\$ 45$ for every two you buy back, thus incurring a very small premium shortfall while significantly decreasing margin requirements ( $\$ 1,670$ margin on each of two contracts is $\$ 3,340$, and $\$ 918$ margin on each of three contracts is $\$ 2,754$ ).

Another thing you should consider doing, if reducing margin becomes important, is to close out positions whose premiums have become relatively small. Even in a general market pullback or serious contraction, there will likely be issues still so far out of the money that the associated premiums are negligible. Consider the example of the XYZ Corporation stock that went from $\$ 53.375$ to $\$ 150$ in a little over
a year and that has now perhaps backed off to $\$ 100$. With a strike price of $\$ 55$, the premium is essentially zero, yet the margin required to maintain this position is $\$ 1,000$ per contract (i.e., 10 percent of $\$ 10,000$ ). As previously indicated, many brokers will gladly work with their customers in such circumstances and charge a minimum commission to close out such positions.

## Covered Put Writing

As stated before, margin is required for writing naked puts and uncovered calls. Investors seeking to increase portfolio income routinely use covered calls to do so. A covered call means the investor writes a call while also owning the stock. This is sometimes referred to as a buy-write if the investor writes the call while simultaneously purchasing the stock. In practice, there is no difference between a buy-write and selling a covered call. In either instance, there is no margin requirement, and the potential for unlimited exposure should there be a sharp rise in the price of the underlying equity is thereby eliminated. Does the same sort of thing happen if an investor resorts to covered put writing?

First of all, exactly what does it mean to write a covered put? Incredibly enough, there is no universal agreement as to what is meant by this expression. The latest edition of Understanding Stock Options (April 1996), published by the Options Industry Council (a trade organization composed of the various options exchanges and the Options Clearing Corporation), states that a "put writer is considered to be uncovered if he does not have a corresponding short stock position or has not deposited cash equal to the exercise value of the put." The latest edition of Characteristics and Risks of Standardized Options (February 1994), published by the Options Clearing Corporation, does not use the term covered put as such but refers only to writers of cash-secured puts. In the latest (ninth edition) and earlier editions of the Pass Trak® Series 7, General Securities Representative, published by Dearborn Financial Publishing, Inc., a naked (or uncovered) option is defined as "the position of an options investor who writes a call or a put on a security he does not own." An insert in the ninth edition expanded this definition, stating that "in a cash account, a put is covered and the writer is not required to meet option margin requirements if she deposits into the
account or presents: cash equal to the aggregate exercise price of the put; an escrow agreement in which a bank certifies that it holds on deposit for the writer funds equal to the aggregate exercise price of the put; or money market securities with a current market value equal to or greater than the aggregate exercise price of the put."

As a result, there are people who believe a covered put writer is one who: (a) is long (owns) the stock; (b) is short the stock; or (c) has cash or cash-equivalent funds in an amount equal to the aggregate exercise price of the put. The correct answer, however, is (b) or (c) in a margin account and (c) in a cash account.

Because we are going to be selling puts in a margin account, let's compare the relative risks and rewards of writing uncovered puts versus covered ones, wherein the investor is short the stock. Interestingly, writing a put while simultaneously short the stock can be more risky than writing a naked put. To understand why, remember that when you write a naked put, the theoretical worst-case situation is where the stock plummets to zero for a net loss equal to the exercise price less the premium received. Should the price of the stock increase, the gain is the premium received.

Now suppose you write a put and are simultaneously short the stock. In this situation, the investor is completely protected if the price collapses because any loss on the option as the price of the stock moves below the exercise price is matched dollar for dollar by the gain incurred on the shorted stock. On the other hand, should the price of the stock increase, the potential for loss increases without limit because the unlimited liability on the upside of the short position is mitigated only by the premium received from the sale of the put.

## 5-

## Disposition and Taxes

## Introduction

The tax consequences arising out of option transactions are extremely complex. Options, like stocks, are classified as capital assets, and the disposition of such assets is a taxable event. As with stocks, how long the position has been held determines whether the gain or loss is classified as short- or long-term. Furthermore, how the gain or loss is treated also depends on whether the option contract has been terminated through trade, expiration, or exercise and assignment. Because of this sensitivity to how an option contract is terminated, the first part of this chapter describes all three terminating actions and the corresponding times by which they must be initiated and accomplished. These are especially important in nip-and-tuck situations where the exercise price of an option is very close to the market price as the expiration day approaches.

## Trading

Until June 23, 1997, trading in all equity options, including LEAPS, stopped at 4:10 PM. ${ }^{*}$ Today, however, in order to minimize disruptions in the options market as a result of news announcements and earnings reports made after the regular markets close at 4:00 PM,

* All times in this chapter are Eastern time unless otherwise specified.
trading in equity options now ceases at 4:02 PM. Customers are typically required by brokerage firms to submit requests for option trades by 3:55 PM at the latest because of the time needed for them to process the trade. This entails looking up trading symbols, verifying account numbers, and filling out trading slips and submitting them to trading desks, which must in turn transmit the orders to the trading floor of the appropriate stock exchange in time for verification and confirmation. Requests for option trades submitted by customers between 3:55 PM and the 4:02 PM absolute cutoff time are often accepted and submitted in hopes of beating the deadline, but the customer assumes all risk in such instances. These times apply to expiration Friday ${ }^{*}$ as well.

Although there are no exceptions to the 4:02 PM trading cutoff on expiration Friday, the CBOE now extends this closing time on the final trading day of each quarter to accommodate the particularly large number of transactions submitted by institutional and mutual fund managers on those days. (The other three exchanges that handle options do not do this, however.) For future reference, note that trading in broad-based and international indexes stops at 4:15 PM.

## Exercise

Option exercise ordinarily begins with the option holder notifying his or her brokerage firm that exercise is to take place. ${ }^{* *}$ Through a sequence of steps, notification in turn is given to the appropriate clearinghouse member of the Options Clearing Corporation, the relevant options exchange, and, ultimately, the Options Clearing Corporation itself. Predictably, there are different cutoff times at different points in this chain and they vary from brokerage firm to brokerage firm. At the various option exchanges, the cutoff time for notification is typically 4:30 PM on all days except expiration Friday, when it is 5:30 PM.

* Options expire on the Saturday following the third Friday of the month, but trading stops on the prior business day. If that Friday is a(stock exchange) holiday, trading ends on Thursday.
${ }^{* *}$ As a matter of course, brokerage firms will automatically exercise options expiring in the money by a certain amount unless instructions to the contrary have been received from the customer. This threshold amount is typically one-half or three-quarters of a point.

The 5:30 PM deadline has been known to be extended up to half an hour by options exchanges on the rare occasion when there is a backlog of exercise orders awaiting execution because of jammed communication lines or networking glitches. In any event, the Options Clearing Corporation must receive its notification by 8:00 Рм (7:00 Рм in Chicago, where the OCC is located) on all days, including expiration Friday.

To meet all deadlines and allow enough time for confirmation, brokerage firms typically require customers to submit exercise requests by 4:00 PM on regular days and by $4: 30$ pm or soon thereafter on expiration Friday. Brokerage firms will rarely, if ever, take on the risk of attempting to submit exercise notices after the cutoff time imposed by clearinghouse members or options exchanges. Although options do not formally expire until noon the next day, Saturday morning is used for reconciliation between open and closed orders and the selection of which option writers get assigned.

## Assignment

The assignment of options for which notification has been received in a timely fashion by the Options Clearing Corporation is performed by noon on Saturday. After that time, option rights become absolutely extinguished. However, option writers who did not close their positions will not find out whether the options were exercised against them until some time on the following Monday, when they are notified by their brokerage firms. Surprises do happen in this regard.

Holders of slightly in-the-money options frequently elect not to exercise their rights to buy or sell the underlying equity, and holders of at-the-money or slightly out-of-themoney options will sometimes exercise their options during the last trading day because they do not know where the final closing price will be relative to the strike price. Holders of at-the-money or slightly out-of-the money options have been known to exercise their options simply because they want to put stock to, or call away stock from, the other fellow.

Another surprise that often happens in the final days or hours of trading is that an option writer will instruct his or her broker to buy back the option and close the position only to receive a notice of assignment a business day or so later. If the exercise preceded closing, the option writer is a candidate for assignment notwithstanding the fact
that the writer did not receive notification until after the closing transaction took place.
The real surprise to option writers that occurs from time to time is that options are exercised against them that are significantly out of the money. This typically happens as a result of major news (bad or good) announced immediately after regular trading hours on expiration Friday. Suppose you are the writer of a put on XYZ Corporation with strike price $\$ 40$. You have been monitoring the price of the underlying stock all day long on expiration Friday and are happy to see it close at $4: 00$ PM at $\$ 405 / 8$. Two minutes later, you see the last trades for $\$ 40$ puts on XYZ close out at $1 / 16$. Great, you figure, the premium you collected all those months ago was pure profit, and you can go home and relax for the weekend. At 4:20 pm, however, XYZ Corporation issues an earnings warning, or announces that it has lost its largest client, or issues a press release stating that its latest wonder drug seems to have harmed more people than it helped. The consensus among analysts is that XYZ will open three or more points down when trading commences Monday morning. For the next hour, holders of the $\$ 40$ put option who stuck around after trading stopped are submitting exercise notices to their brokers. On Monday morning, XYZ opens at $\$ 36$ a share, and numerous put writers of the $\$ 40$ strike option who did not close out their positions on Friday wake up to find they are the owners of a $\$ 36$ stock that has just cost them $\$ 40$ plus commission.

In situations like this, only a certain fraction of the out-of-the-money options will have been exercised because many of the option holders will have considered their option worthless and gone home for the weekend by 4:00 Pm. Suppose the open interest in the $\$ 40$ put options totaled 1,000 contracts, of which 200 were exercised at the last minute. Who gets assigned and who does not is determined by a two-step procedure. First, the Options Clearing Corporation allocates the 200 assignments among the various brokerage firms in proportion to the open interest each firm represents. That is, if clients of the ABC Securities Corporation had written 120 of the 1,000 open put options, then 20 percent of 120 , or 24 assignments $(120 \times 200 \div 1,000)$ would be allocated to ABC. Then that firm will select 24 option contracts at random from among the 120 open interest put writers and notify them accordingly. It is thus luck of the draw that determines who gets stuck and who does not in such situations.

To avoid such situations, it is therefore recommended that investors make arrangements with their brokers to close out all option contracts that might have any possibility of taking the option writer by surprise owing to bad news announced after trading ends on expiration Friday. If you had pocketed $\$ 1,000$ in premiums many months before (and earned interest on that amount since then), buying back the option for $1 / 8(\$ 12.50)$ is a relatively small price to pay, and doing this will permit you to leave for the weekend on expiration Friday with complete peace of mind. As stated before, for active participants many brokers will forgo the usual commission on such deals and charge a nominal amount under the circumstances.

## Trading Halts

A frequently asked question on the CBOE bulletin board is exactly what happens to option writers and option holders when trading in the underlying equity is halted. In general, halting the trading in the underlying equity automatically halts the trading of associated options. This restriction applies strictly to trading, so under ordinary situations (i.e., order imbalance, news pending, etc.), option holders are still able to exercise their option rights. Much more tricky is what happens on those occasional instances when the OCC suspends option exercise as well. This situation is particularly worrisome near expiration Friday.

As stated in Characteristics and Risks of Standard Options, the "OCC or an options market may restrict the exercise of an option while trading in an option has been halted, and the restriction may remain in effect until shortly before expiration." So relax-this means that the OCC must lift the exercise restrictions in sufficient time for option holders to exercise their options before such rights are permanently extinguished.

## Recent History of Tax Treatment of Capital Assets

The tax treatment of capital gains and options has undergone several shifts and reversals over the past few years. For a long time prior to 1997, gains and losses on capital assets were classified as being either short- or long-term depending on whether the underlying assets had been held for less than or longer than 12 months.

## The Taxpayers Relief Act of 1997

The Taxpayers Relief Act of 1997 introduced substantial changes in the ways in which gains and losses on capital assets were recognized, treated, and taxed. Gains and losses, previously classified as short-term or long-term, were now classified as being short-term, midterm, or long-term. As before, assets held for under 12 months were classified as short-term; assets held between 12 and 18 months were midterm, and assets held for 18 months and longer were long-term. Short-term assets were taxed at ordinary income rates, which for individuals could be as high as 39.6 percent. Midterm assets were taxed at the flat rate of 28 percent, and long-term assets were taxed at the flat rate of 20 percent. A flat rate of 10 percent was also applicable to individuals in a 15 percent tax bracket. These rates applied to both the regular and alternative minimum taxes as well. The tax rate on long-term gains on collectibles remained at 28 percent, and the long-term rate on real estate investments was 25 percent.

## The IRS Restructuring and Reform Act of 1998

The IRS Restructuring and Reform Act of 1998 eliminated the midterm holding period (and its 28 percent tax rate) and reverted once again to the short- and long-term capital gains classification. Under the IRS Restructuring and Reform Act, a capital gain from the sale of property held more than one year is eligible for the same $10-, 20$-, and 25percent capital gains rates as was provided under the 1997 Act.

## What Lies Ahead

The tax acts of 1997 and 1998 specify that starting in the year 2001, the capital gains tax rates of 20 percent and 10 percent for assets held for five years or more are to be 18 percent and 8 percent, respectively. The 18 percent rate (but not the 8 percent rate), however, is restricted to assets acquired on or after January 1, 2001. Individuals in a 15 percent tax bracket are to have their long-term capital gains taxed at just 8 percent starting in 2001, even on assets acquired before then. Because LEAPS typically have life spans of at most 30 months (although they can by regulation be issued for up to 39 months), the

Table 5.1
Effective Tax Rates on Capital Gains under the Tax Acts of 1997 and 1998

Prior to Jan, 1, 2001

Classification of Gain

Short-term ( $<12$
months)

Long-term ( $>12$
months)

| Long-term (15\% <br> taxpayer) | $10.0 \%$ |
| :--- | :--- |
| Long-term (collectibles) | $28.0 \%$ |
| Long-term (real estate) | $25.0 \%$ |

On and after Jan, 1, 2001

## Classification of Gain

Short-term ( $<12$
months)

Long-term (>12 months)

Long-term (15\% taxpayer)

Long-term (collectibles)

Long-term (real estate)

## Applicable

 Rate$39.6 \%{ }^{*}$
18.0\%
8.0\%
28.0\%
$25.0 \%$
*Maximum tax bracket applicable
special five-year tax rates of 18 percent and 8 percent are of little relevance to option contracts (unless superlong LEAPS are introduced).

The revised rates are summarized in Table 5.1. As you can see, the tax on $\$ 1,000$ of capital gains can range from a maximum of $\$ 396$ down to as little as $\$ 80$, depending on the holding period and tax bracket involved.

## Tax Implications for Option Holders

For call and put buyers who sell their options, the gain or loss is the difference between the net sales price (sales price less commission) and the adjusted cost basis (purchase price plus commission). The gain or loss will be classified as short- or long-term, depending on whether the position was held for less than or equal to 12 months or longer than 12 months. By extension, the capital loss for call and put buyers whose options expire worthless is the adjusted cost basis, and the loss is classified as being short- or long-term based on the period between acquisition and expiration.

For call buyers who exercise their options, the adjusted cost basis of acquiring the stock (strike price plus commission) is increased by the adjusted cost basis of the call. Whether the gain or loss on ultimate sale of the stock is short- or long-term will depend on the
subsequent holding period of the stock alone, without regard to how long the call was held. For put buyers who exercise their options, the net sales proceeds are reduced by the adjusted cost basis of the put. Whether the gain or loss upon delivery is classified as short- or long-term depends solely on how long the stock alone was held, without regard to how long the put was held.As an example, suppose you purchase a LEAP put for $\$ 10$ a share plus a $\$ 30$commission to protect your position on XYZ, a $\$ 50$ stock that you've owned for sixmonths:
Cost Basis ..... \$1,000
Plus: Commission ..... 30
Adjusted Cost Basis ..... \$1,030
Fifteen months later you sell the LEAP put on XYZ for \$2 a share less a $\$ 25$commission:
Sales Proceeds ..... \$ 200
Less: Commission ..... 25
Net Sales Proceeds ..... \$ 175
The capital gain and corresponding tax for this transaction are therefore:
Adjusted Cost Basis ..... \$1,030
Less: Net Sales Proceeds ..... 175
Long-Term Capital Loss ..... \$ 855
Income Tax @ 20\% ..... 171-

The dash indicates a credit that can offset the taxpayer's other tax liability.

## Tax Implications for Option Writers

For call and put writers, premiums received are not treated as immediate income. How and when option writers pay taxes on such premiums depend on the disposition of the option involved. For call and put writers who close out their positions by buying back the options involved, the gain or loss is the difference between the adjusted closeout cost (closeout cost plus commission) and the net premium (premium less commission) originally received. In general, the resultant capital gain or loss is treated as a short-term
gain or loss, irrespective of the period involved.* By extension, if the option expires without exer-

* The one exception to this occurs when an in-the-money call is written on stock already owned for more than 12 months and the call is purchased back at a loss. In this situation the capital loss is treated as a long-term loss.
cise, the net premium (premium less commission) is treated as a short-term capital gain, irrespective of the period involved.

As an example, suppose you write a LEAP put on XYZ for $\$ 10$ a share less a $\$ 30$ commission:
Premium Generated ..... \$1,000
Less: Commission ..... 30
Net Premium ..... \$ 970
Fifteen months later, you buy back that LEAP put for $\$ 2$ a share plus a $\$ 25$ commission:
Closeout Cost ..... \$ 200
Plus: Commission ..... 25
Adjusted Closeout Cost ..... \$ 225

The short-term capital gain and maximum corresponding tax for this transaction are therefore:

Net Premium

Less: Adjusted Closeout
Cost
Short-Term Capital Gain
Income Tax @ 39.6\%
$\$ 970.00$
225.00
$\$ 745.00$
295.02 (maximum)

Notice that the gain is treated as short-term, irrespective of the holding period.
For call writers whose options were exercised against them, the adjusted sales price (strike price plus commission) of the delivered stock is increased by the net premium (premium less commission) originally received. Whether the gain or loss upon delivery of the stock is classified as short- or long-term depends on two things: how long the stock was held, and whether the call at the time it was written was out of the money, in
but near the money, or deep out of the money.
In general, writing out-of-the-money calls or calls on stock already qualifying for longterm treatment has no effect on the holding period. On the other hand, writing in-but-near-the-money calls on stock held less than 12 months can suspend the prior holding period of the stock, while writing deep-out-of-the-money calls on stock held less than 12 months can eliminate the prior holding period of the stock altogether. Whether a call is classified as in but near the money or deep out of the
money depends not only on the relative strike and stock prices involved, but also on the remaining time to expiration. There is no simple formula for all of this, and readers should consult the appropriate tables published by the Internal Revenue Service to determine whether a specific in-the-money call written on stock already owned qualifies for mere suspension versus elimination of the prior holding period.

Covered call writers can elect to use stock they already own or stock they immediately purchase in the open market to deliver, so to that extent they can influence or control the holding period and cost basis of the delivered stock. Such complexities are another reason why I prefer not to utilize covered call writing as part of my investment program.

For put writers whose options were exercised against them, the adjusted purchase price (strike price plus commission) of the acquired stock is decreased by the net premium (premium less commission) originally received. Whether the gain or loss on delivery of the stock is short- or long-term will depend on the subsequent holding period of the stock alone, without regard to when the option was written. As an example, suppose you write a LEAP put with strike price $\$ 50$ on XYZ for $\$ 10$ a share less a $\$ 30$ commission:
Premium Generated ..... \$1,000
Less: Commission ..... 30
Net Premium ..... \$ 970

Fifteen months later the option is exercised against you (because the stock fell to \$40) and you purchase the delivered stock for $\$ 50$ a share plus a $\$ 75$ commission:
Strike Price of Stock ..... \$5,000
Plus: Commission ..... 75
Adjusted Purchase Price ..... \$5,075
Less: Net Premium ..... 970
Adjusted Cost Basis ..... \$4,105

Six months later, you sell your XYZ shares for $\$ 48$ a share less a $\$ 75$ commission:

Less: Commission

Net Sales Proceeds
$\$ 4,725$

The capital gain and maximum corresponding tax for this transaction are therefore:

Net Sales Proceeds
Less: Adjusted Cost Basis
Short-Term Capital Gain
Income Tax @ 39.6\%
\$4,725.00
4,105.00
\$ 620.00
245.52 (maximum)

Notice that the gain is treated as short-term because the holding period is that of the stock, without regard to the length of time the option position was held. Further note that there was a capital gain on ultimate disposition even though you sold the stock at a price $(\$ 48)$ lower than what you paid for it (\$50), a consequence of the premium received 21 months before.

## Other Tax Implications

The tax consequences in the case of spreads, strangles, straddles, and other combinations are much more complicated and are beyond the scope of this book. Indeed, I think an entire book could be written about the tax implications of puts and calls. There are many traps that await the unwary in the options arena. As a simple instance, suppose you purchased a put to protect a stock in your portfolio that was acquired less than one year before that. The tax implications regarding the put itself are as described previously in this chapter. What is not so apparent is that the holding period of the stock being protected is completely eliminated in that instance and will not begin again until the put is disposed of.

As an example, let's go back to our very first example where you purchased a LEAP put on XYZ to protect your position on this $\$ 50$ stock that you had purchased for $\$ 45$ plus a $\$ 75$ commission and had owned for six months. Fifteen months later, you sold 'the LEAP put for a loss of $\$ 855$ and tax credit of $\$ 171$. Suppose you then sold the XYZ stock itself ten months after that for $\$ 80$ a share less an $\$ 85$ commission.

Sales Proceeds

\$8,000

Less: Commission 85
Net Sales Proceeds
$\$ 7,915$
Plus: Commission ..... 75Adjusted Cost Basis\$4,575

The capital gain and maximum corresponding tax for this transaction after you held this stock for 31 months are therefore:

Net Sales Proceeds
Less: Adjusted Cost Basis
Short-Term Capital Gain
Income Tax @ 39.6\%
\$7,915.00
4,575.00
\$3,340.00
1,322.64 (maximum)

This is considerably more than the 20 percent long-term capital gains tax of $\$ 668$ you were expecting to pay because as far as tax law is concerned, you had only held the stock for 10 months. There are ways to avoid this, such as by waiting the requisite 12 months before buying the protective put or by "marrying" the put and the stock; that is, by buying both the stock and the put at the same time with the announced intention of selling the stock by exercising the put. In any case, none of this should scare you away from the use of protective puts as part of your overall asset management program. Rather, it is just to show you that tax law is complex, that as it is applied to options it is even more complex, and that a tax adviser should be consulted before embarking on any extensive options program.

By the way, it is possible to use some of these quirks in the tax law to your advantage in certain situations. For example, suppose you own a stock for close to one year that has tanked badly, but which for one reason or another you do not wish to dispose of immediately. If you do delay the sale, the short-term capital loss will become a long-term loss (and therefore no longer available to offset short-term gains). On the other hand, if you purchase a put or a deep-in-the-money call on that stock, the holding period on the stock is immediately set back to zero, preserving its short-term status. This is true whether you hold the option one minute or one year.

In case you skimmed over it the first time, let me repeat: a tax adviser should be consulted before embarking on any extensive options program.

## PART TWO-

RISK, REWARD, AND SAFETY

## 6-

## Baseline Analysis

## Reaction and Challenge

As I perfected the basic strategy described in the previous chapters, I began to describe the method to friends and fellow investors. Many of them were horrified to hear that I was dealing with uncovered puts. "Too risky," they said; "It's doomed to failure;" "The gains you make on successful deals will be overwhelmed by gigantic losses on your losers." Listening to them would have you convinced I was playing the ponies or gambling in Las Vegas. It's not hard to understand these initial reactions; after all, Characteristics and Risks of Standard Options, a joint publication of the various option exchanges, emphatically states that "as with writing uncovered calls, the risk of writing put options is substantial." This warning is repeated in the companion pamphlet Understanding Stock Options. Few seemed to recall the statement made in the former publication: "The risk of being an option writer may be reduced by the purchase of other options on the same underlying interest-and thereby assuming a spread position-or by acquiring other types of hedging positions in the options markets or other markets."

How could I convince other investors (and myself as well) that what I was doing had the potential to increase the rate of return on my investment portfolio without unnecessary risk? After all, people do invest their funds in uninsured money market funds paying 5 percent a year rather than federally insured passbook savings accounts paying
just 3 percent a year. The added return must bring with it a certain degree of added risk, yet almost everyone is willing to accept the risk/ reward ratio in this situation.

## Methodology

To address this issue, imagine what would have been the outcome if each month over some extended period, one sold an at-the-money (ATM) LEAP put on every company for which LEAPS existed and pocketed the premium. The period selected was the tenyear period ending March 31, 1997. This cutoff date was selected because on that date the Dow Jones Industrial Average stood at 6,583 and the Nasdaq composite index was at 1,222 , both well below their closing values for 1996 and close to their lows of 1997. In that manner, the phenomenal run-up that has taken place in the stock market since then was effectively eliminated.

On that date, LEAPS existed on the 217 equities shown in Table 6.1. Because of mergers, acquisitions, and spin-offs, about three dozen of these companies are no longer independent entities and/or have changed their names since then. These include Air Touch, Amoco, Bay Networks, Borland, Chrysler, Citicorp, Columbia Gas, CUC International, Digital Equipment, DSC Communications, Dun \& Bradstreet, ENSEARCH, First Chicago, General Instrument, HFS, ITT, Marriott International, Mobile Telecommunications, NationsBank, NYNEX, Pacific Telesis, PHP Healthcare, R JR Holdings, Salomon, Signet Bank, SunAmerica, Tambrands, TCI, Telephonos de Brasileras, Travelers, U.S. Robotics, U.S. Surgical, Westinghouse, WMX Technologies, and Woolworth. By the time you read this, other reorganizations will have undoubtedly taken place.

Of course, LEAP puts did not come into being until 1990, and even then they only appeared on just a handful of stocks, so you will have to imagine for the moment that such puts had been in existence for those 217 equities over the ten-year period ending on March 31, 1997. Because LEAPS did not exist for most of these issues over that period, no historical information is available on the premiums that such options would have commanded. What was done instead was to use the daily history of closing stock prices over that decade to compute historical volatility, and from this to use the standard BlackScholes for-
mula for computing the LEAP put premium on a month-to-month basis. So as not to make the modeling process too complex, the risk-free rate of return was kept at 6 percent per year throughout, and all volatility calculations were based on the prior one-year (typically 253 trading days) price history.

In each instance, the at-the-money put selected was the one for which the strike price was equal to or immediately below the market price of the underlying issue in accordance with standard option rules: If the price of the stock was $\$ 23$, the option sold was the one at $\$ 22.50$; if the price was $\$ 44$, the option sold was the one at $\$ 40$; and if the price was $\$ 247$, the option sold was the one at $\$ 240$.

In most instances, there would have been not just one but two such LEAP puts available for sale each month: the one that expired in the January about a year to a year and a half away, and the one that expired in the January about two to two and a half years away. We will call these the near and far LEAPS, for the lack of better terms. If the expiration date of the near LEAP put was less than eight months away, it was not sold, as we want to restrict the study to an analysis of long-term options.

A database containing the ten-year history of daily high, low, and closing prices of the 217 common stocks that had LEAPS on March 31, 1997, was downloaded from the America Online historical price files. Along with the stocks in Table 6.1 are listed their respective ratings by First Call (F/C) and Standard \& Poor's (S\&P) as of March 31, 1997. Also shown are the volatilities calculated for March 31, 1997. The figures range from a low of 0.150 for Amoco Corporation to an unusually high 1.456 for Compania Tele de Chile. Only 10 of the 217 stocks had volatilities greater than 0.65 .

The First Call rating system generates a numerical average determined from the ratings supplied by the industry analysts who follow the stock. An individual analyst's ratings range from 1 (strongest recommendation) to 5 (strong sell). Because of the averaging technique involved, it is rare to see First Call ratings worse than 3.5. The S\&P ratings range from $\mathrm{A}+$ (strongest possible) downward. Just one stock (Pitney Bowes) was not rated by First Call, while 37 stocks were not rated by Standard \& Poor's. Most of the issues not rated by S\&P represented American Depositary Receipts (ADRs) of foreign stocks.

For the 216 issues with First Call ratings, the average is 2.1 , which is slightly better than the average rating of about 2.2 for the universe of stocks rated by First Call. Among the 180 issues with $\mathrm{S} \& \mathrm{P}$ ratings, the average is just under $\mathrm{B}+$. (The $\mathrm{S} \& \mathrm{P}$ average was calculated by letting $\mathrm{A}+=5.0, \mathrm{~A}=4.5, \mathrm{~A}-=4.0, \mathrm{~B}+=3.5, \mathrm{~B}=3.0, \mathrm{~B}-=2.5, \mathrm{C}+=2.0$, and $\mathrm{C}=1.5$. The numerical average calculated on this basis was 3.4.) The average volatility for all 217 issues in Table 6.1 is 0.346 .

## The Simulation Model

After downloading the historical data, I constructed a detailed simulation model that could calculate the effects on each of the 217 issues listed in Table 6.1 of having sold a put each month for the period from January 1987 (or whenever the company came into being) through March 31, 1997. The two extra months (January and February) in 1987 were included to allow more accurate computation of initial volatilities. More important was the fact that I started the analysis with 1987 because I wanted to include one of the worst days ever from the viewpoint of put sellers-the market decline of 22.6 percent on October 19, 1987.

Each data history file contained the daily high, low, and closing prices for the stock from January 1, 1987, onward. It is possible to distort the results if the LEAP puts are consistently taken as being sold at that point each month when the underlying issue achieved its low price (and hence commanded its highest put premium). So as not to bias the results, the assumption was made that all LEAP puts were sold at the closing price on the last day of the month.

It is also possible to distort the results if the LEAP puts are consistently taken as being sold only in the month or months when the underlying issue achieved its low price (and hence commanded its highest put premium). It was for this reason that the assumption was made that LEAP puts were sold on each stock each and every month during the calendar year (subject only to a minimum expiration date of eight months).

Another way to distort the results is to select a cutoff date ending on a sharp upbeat in market prices. As mentioned earlier, it was to minimize this possibility that the cutoff date of March 31, 1997 (close to the low of the year), was selected for the financial simulation rather

Table 6.1
LEAPS Available in March 1997

| Name of | Symbol | F/C | S\&P | Vol. |
| :--- | :--- | :--- | :--- | :--- |
| Underlying <br> Equity |  |  |  |  |


| Abbott Labs | ABT | 2.2 | A+ | 0.230 |
| :--- | :--- | :--- | :--- | :--- |
| Acuson | ACN | 2.2 | B- | 0.449 |
| Adobe Systems | ADBE | 1.7 | B+ | 0.504 |
| Advanced Micro | AMD | 2.5 | B- | 0.537 |
| AirTouch Comm. | ATI | 1.6 | NR | 0.298 |
| Allied Signal | ALD | 1.9 | B+ | 0.203 |
| Allstate | ALL | 1.9 | BR | 0.261 |
| Altera | ALTR | 1.5 | B- | 0.616 |
| ALZA | 2.4 | CA | B+ | 0.246 |
| Amerada Hess | AHC | 2.5 | A+ | 0.214 |
| America Online | AOL | 1.9 | A+ | 0.748 |
| American Express | AXP | 2.4 | 1.6 | 0.252 |
| American Home | AHP | AIG |  |  |
| American | International |  |  | 0.195 |


| Amgen | AMGN | 1.8 | B | 0.311 |
| :--- | :--- | :--- | :--- | :--- |
| Amoco | AN | 2.7 | B+ | 0.150 |
| AMR | AMR | 2.0 | B- | 0.264 |
| Anheuser-Busch | BUD | 2.4 | A | 0.217 |


| Apple Computer | AAPL | 3.1 | B | 0.536 |
| :---: | :---: | :---: | :---: | :---: |
| Applied Materials | AMAT | 1.5 | B | 0.536 |
| ASA Holdings | ASAI | 2.6 | A | 0.341 |
| AT\&T | T | 2.5 | B+ | 0.271 |
| Atlantic Richfield | ARC | 2.7 | B+ | 0.173 |
| Atmel | ATML | 1.7 | B | 0.644 |
| Avon Products | AVP | 1.8 | B+ | 0.237 |
| Baker Hughes | BHI | 2.0 | B | 0.315 |
| BankBoston | BKB | 1.8 | B | 0.229 |
| BankAmerica | BAC | 1.7 | B+ | 0.270 |
| Bankers Trust NY | BT | 2.8 | B | 0.220 |
| Barrick Gold | ABX | 2.4 | A | 0.302 |
| Bay Networks | BAY | 2.6 | B | 0.510 |
| Bell Atlantic | BEL | 2.1 | A- | 0.226 |
| BellSouth | BLS | 2.3 | B+ | 0.291 |
| Best Buy Co. | BBY | 3.1 | B | 0.576 |
| Biogen | BGEN | 1.7 | B- | 0.433 |
| Boeing | BA | 1.5 | B+ | 0.246 |
| Borland International | BORL | 2.7 | C | 0.718 |
| Boston Scientific | BSX | 1.4 | NR | 0.354 |
| Bristol-Myers Squibb | BMY | 2.6 | A | 0,255 |


| Burlington <br> Northern | BNI | 1.6 | NR | 0.208 |
| :--- | :--- | :--- | :--- | :--- |
| Cabletron Systems | CS | 2.0 | B + | 0.497 |
| Campbell Soup | CPB | 2.3 | B+ | 0.209 |
| Caterpillar | CAT | 2.7 | B | 0.247 |
| Centocor | CNTO | 1.8 | C | 0.607 |
| Chase Manhattan | CMB | 1.5 | B | 0.245 |
| Chevron | CHV | 2,7 | B | 0,205 |
| Chiron | CHIR | 2.6 | C | 0.441 |
| Chrysler | C | 2.3 |  | 0.262 |

(Table continued on next page)

Table 6.1
LEAPS Available in March 1997 (Continued)

| Name of | Symbol | F/C | S\&P | Vol. |
| :--- | :--- | :--- | :--- | :--- |
| Underlying <br> Equity |  |  |  |  |


| Chubb | CB | 2.3 | A | 0.257 |
| :--- | :--- | :--- | :--- | :--- |
| Cirrus Logic | CRUS | 2.4 | B- | 0.652 |
| Cisco Systems | CSCO | 1.5 | B | 0.430 |
| Citicorp | CCI | 1.9 | B | 0.237 |
| Coca-Cola | KO | 2.0 | A+ | 0.221 |
| Columbia Gas | CG | 2.5 | NR | 0.203 |
| Compania Tele de <br> Chile | CTC | 2.4 | NR | 1.456 |


| Compaq | CPQ | 1.5 | B | 0.405 |
| :--- | :--- | :--- | :--- | :--- |
| Conseco | CNC | 1.0 | B + | 0.331 |
| Corning | GLW | 1.4 | B + | 0.301 |
| Cracker Barrel | CBRL | 1.8 | A | 0.325 |
| CUC International | CU | 1.5 | B | 0.348 |
| Cypress Semi | CY | 2.5 | B | 0.530 |
| Dayton Hudson | DH | 1.9 | B | 0.314 |
| Dell Computer | DELL | 1.9 | B- | 0.508 |
| Delta Air Lines | DAL | 1.8 | C | 0.247 |
| Digital Equipment | DEC | 3.0 | A | 0.504 |
| Disney (Wait) | DIS | 2.0 |  | 0.221 |


| Dow Chemical | DOW | 2.9 | B | 0.157 |
| :---: | :---: | :---: | :---: | :---: |
| DSC | DIGI | 2.2 | B | 0.628 |
| Communications |  |  |  |  |
| Dun \& Bradstreet | DNB | 2.6 | B+ | 0.990 |
| DuPont (E.I.) de Nemours | DD | 2.1 | B+ | 0.231 |
| Eastman Kodak | EK | 2.0 | B | 0.273 |
| EFII | EFII | 1.3 | NR | 0.529 |
| EMC | EMC | 1.9 | B | 0.436 |
| ENSERCH | ENS | 2.8 | B | 0.317 |
| Equifax | EFX | 2.0 | A- | 0.324 |
| Ericsson <br> Telephone | ERICY | 2.2 | NR | 0.332 |
| Exxon | XON | 2.6 | A- | 0.192 |
| Fannie Mae | FNM | 1.5 | A | 0.340 |
| Federal Express | FDX | 2.4 | B- | 0.249 |
| Federated Stores | FD | 1.7 | NR | 0.287 |
| First Chicago | FCN | 2.3 | NR | 0.274 |
| Ford Motor | F | 1.9 | B- | 0.224 |
| Fruit of the Loom | FTL | 2.3 | B- | 0.268 |
| Gap | GPS | 1.8 | A | 0.393 |
| General Electric | GE | 1.6 | A+ | 0.209 |
| General Instrument | GIC | 2.4 | NR | 0.419 |


| General Mills | GIS | 2.6 | A | 0.179 |
| :--- | :--- | :--- | :--- | :--- |
| General Motors | GM | 2.0 | B | 0.236 |
| Georgia-Pacific | GP | 2.5 | B- | 0.193 |
| Gillette | G | 1.6 | A+ | 0.242 |
| Glaxo Wellcome | GLX | 2.4 | NR | 0.231 |
| Goodyear Tire | GT | 2.3 | BR | 0.189 |
| Grupo Televisa | TV | 2.2 | B+ | 0.373 |
| GTE | GTE | 1.9 | B+ | 0.259 |
| HealthSouth | HRC | 1.6 | A+ | 0.346 |
| Heinz (H.J.) | HNZ | 2.6 |  | 0.211 |

(Table continued on next page)

Table 6.1
LEAPS Available in March 1997 (Continued)

| Name of | Symbol | F/C | S\&P | Vol. |
| :--- | :--- | :--- | :--- | :--- |
| Underlying <br> Equity |  |  |  |  |


| Hewlett-Packard | HWP | 2.2 | A | 0,378 |
| :---: | :---: | :---: | :---: | :---: |
| HFS Inc. | HFS | 1.1 | NR | 0.423 |
| Hi[ton Hotels | HLT | 1.5 | B+ | 0.291 |
| Home Depot | HD | 1.4 | A+ | 0.293 |
| Homestake Mining | HM | 2.7 | B- | 0.330 |
| Household International | HI | 2.1 | B+ | 0.236 |
| IBM | IBM | 1.9 | B- | 0.316 |
| Informix | IFMX | 2.5 | B | 0.810 |
| Intel | INTC | 1.6 | B+ | 0.331 |
| International Game | IGT | 1.5 | B+ | 0.351 |
| International Paper | IP | 2.5 | B | 0.228 |
| ITT | ITT | 2.3 | NR | 0.403 |
| Johnson \& Johnson | JNJ | 1.9 | A+ | 0,242 |
| KMart | KM | 2.5 | B+ | 0.418 |
| Kroger | KR | 1.8 | B+ | 0.245 |
| Limited | LTD | 2.5 | A | 0,298 |
| Liposome | LIPO | 1.7 | C | 0.662 |
| Lowe's | LOW | 1.8 | A- | 0.383 |


| Lucent | LU | 2.0 | NR | 0.354 |
| :--- | :--- | :--- | :--- | :--- |
| Technologies |  |  |  |  |

Madge Netwo
Magna
International

| Marriott | MAR | 1.6 | NR | 0.218 |
| :--- | :--- | :--- | :--- | :--- |
| International |  |  |  |  |


| Maytag | MYG | 2.2 | B- | 0.266 |
| :--- | :--- | :--- | :--- | :--- |
| MBNA | KRB | 1.9 | A- | 0.671 |
| McDonald's | MCD | 2.4 | A+ | 0.210 |
| McGraw-Hill | MHP | 2.5 | NR | 0.192 |
| MCI <br> Communications | MCIC | 2.0 | B | 0,333 |


| MEMC Electronic | WFR | 2.2 | NR | 0.635 |
| :--- | :--- | :--- | :--- | :--- |
| Merck | MRK | 2.2 | A+ | 0.253 |
| Merrill Lynch | MER | 2.7 | B+ | 0.290 |
| Micron <br> Technology | MU | 2.4 | B | 0.644 |
| Microsoft | MSFT | 1.6 | B+ |  |
| Minn, Mining | MUM | 2.9 | A+ | 0.285 |
| Mobil | MOB | 2.3 | NR | 0.214 |
| Mobile Telecomm. | MTEL | 2.8 | B+ | 0.175 |
| Monsanto | MTC | 1.7 | B+ | 0.587 |
| Morgan (J.P.) | JPM | 2.5 | 0.314 |  |


| Motorola | MOT | 2.2 | A+ | 0.354 |
| :--- | :--- | :--- | :--- | :--- |
| National <br> Semiconductor | NSM | 2.1 | B- | 0.478 |
| NationsBank | NB | 2.0 | A- | 0.247 |
| Newbridge <br> Networks | NN | 1.7 | B | 0.509 |
| NEXTEL | NXTL | 1.5 | NR |  |
| NIKE | NKE | 1,9 | B | 0.461 |
| Novell | NOVL | 2.7 | B+ | 0.334 |
| NYNEX | NYN | 2.4 | B- | 0.546 |
| Occidental | OXY | 2.6 | B+ | 0.234 |
| Petroleum | ODP | 1.5 | B | 0.213 |
| Office Depot | ORCL |  |  | 0.614 |
| Oracle |  |  |  |  |

(Table continued on next page)

Table 6.1
LEAPS Available in March 1997 (Continued)

| Name of <br> Underlying <br> Equity | Symbol | F/C | S\&P | Vol. |
| :--- | :--- | :--- | :--- | :--- |


| Pacific Telesis | PAC | 2.6 | B | 0.279 |
| :--- | :--- | :--- | :--- | :--- |
| PepsiCo | PEP | 2.0 | A | 0.264 |
| Pfizer | PFE | 2.0 | A- | 0.258 |
|  <br> Upjohn | PNU | 2.7 | NR | 0.284 |


| Phelps Dodge | PD | 2.5 | B + | 0.231 |
| :--- | :--- | :--- | :--- | :--- |
| Philip Morris | MO | 1.5 | A+ | 0.289 |
| PHP Healthcare | PPH | 3.0 | B- | 0.662 |
| Pitney Bowes | PBI | NR | A+ | 0.223 |
| Placer Dome | PDG | 2.3 | B- | 0.308 |
| Polaroid | PRD | 2.9 | B+ | 0.217 |
| Potash <br> Saskatchewan | POT | 2.3 | NR | 0.277 |


| PPG Industries | PPG | 2.7 | A- | 0.177 |
| :--- | :--- | :--- | :--- | :--- |
| Procter \& Gamble | PG | 1.7 | A | 0.210 |
| Quaker Oats | OAT | 2.9 | B+ | 0.241 |
| Qualcomm | QCOM | 1.6 | B- | 0.549 |
| Reebok <br> International | RBK | 2.4 | B+ | 0.311 |
| R JR Nabisco | RN | 1.7 |  |  |


| Safeway | SWY | 1.9 | B | 0.295 |
| :---: | :---: | :---: | :---: | :---: |
| Salomon Bros. | SB | 2.3 | B+ | 0.270 |
| Sara Lee | SLE | 2.3 | A | 0.214 |
| SBC <br> Communications | SBC | 2.2 | A | 0.209 |
| Schering-Plough | SGP | 2.3 | A+ | 0.258 |
| Schlumberger | SLB | 2.0 | B+ | 0.261 |
| Schwab | SCH | 2.5 | B+ | 0.402 |
| Seagate <br> Technology | SEG | 1.7 | B | 0.477 |
| Sears, Roebuck | S | 2.0 | B | 0.296 |
| Signet Banking | SBK | 2.4 | B | 0.264 |
| SmithKline Beecham | SBH | 1.9 | NR | 0.215 |
| Southwest Air | LUV | 2.2 | A- | 0.350 |
| Sprint | FON | 2.2 | B + | 0.267 |
| Storage <br> Technology | STK | 2.0 | B- | 0.479 |
| Sun Microsystems | SUNW | 1.6 | B | 0.464 |
| SunAmerica | SAI | 1.5 | A | 0.369 |
| Sybase | SYBS | 2.7 | C | 0.562 |
| Tambrands | TMB | 2.8 | B | 0.237 |
| TCI | TCOMA | 1.6 | NR | 0.403 |
| Tele. Argentina | TAR | 2.1 | NR | 0.329 |


| Tele. Brasileiras | TBR | 1.3 | NR | 0.304 |
| :--- | :--- | :--- | :--- | :--- |
| Tele. Mexico | TMX | 2.3 | NR | 0.256 |
| Tenneco | TEN | 2.5 | B | 0.224 |
| Texaco | TX | 2.5 | B | 0.204 |
| Texas Instruments | TXN | 2.1 | B | 0.425 |
| 3Corn | COMS | 2.0 | B- | 0.603 |
| Tiffany \& | TIF | 1.9 | B- | 0.377 |
| Time Warner | TWX | 2.0 | B+ | 0.266 |
| Toys "R" Us | TOY | 2.2 | NR | 0.325 |
| TWA | TWA | 2.0 | A | 0.682 |
| Travelers | TRV | 1.8 | 0.320 |  |

(Table continued on next page)

Table 6.1
LEAPS Available in March 1997 (Continued)

| Name of | Symbol | F/C | S\&P | Vol. |
| :--- | :--- | :--- | :--- | :--- |
| Underlying <br> Equity |  |  |  |  |


| Triton Energy | OIL | 2.0 | B- | 0.297 |
| :--- | :--- | :--- | :--- | :--- |
| U.S. Robotics | USRX | 2.3 | B+ | 0.655 |
| UAL | UAL | 1,9 | B- | 0,356 |
| Union Carbide | UK | 2.5 | NR | 0.230 |
| Unisys | UIS | 3.0 | C | 0.498 |
| United HealthCare | UNH | 1.8 | B+ | 0.513 |
| United   <br> Technologies UTX 2.0 | B | 0.214 |  |  |


| Unocal | UCL | 2.6 | $\mathrm{~B}+$ | 0.257 |
| :--- | :--- | :--- | :--- | :--- |
| US Surgical | USS | 1.9 | $\mathrm{~B}+$ | 0.417 |
| US WEST Comm. | USW | 2.4 | $\mathrm{~B}+$ | 0.229 |
| US WEST Media | UMG | 1.5 | NR | 0.283 |
| USAir Group | U | 2.4 | $\mathrm{~B}-$ | 0.431 |
| USX-Marathon | MRO | 2.4 | NR | 0.283 |
| USX-U.S. Steep | X | 2.2 | NR | 0.239 |
| Viacom | VIA.B | 1.8 | $\mathrm{~A}+$ | 0.304 |
| Wal-Mart | WMT | 2.1 | $\mathrm{~A}-$ | 0.285 |
| Warner-Lambert | WLA | 1.8 | $\mathrm{~B}+$ | 0.271 |
| Wells Fargo | WFC | 2,2 | 0,191 |  |


| Wendy's <br> International | WEN | 1.9 | A- | 0.286 |
| :--- | :--- | :--- | :--- | :--- |
| Westinghouse | WX | 2.6 | B- | 0.304 |
| WMX |  |  |  |  |
| Technologies | WMX | 2.3 | B | 0.255 |
| Woolworth | Z | 1.7 | C |  |
| WorldCom | WCOM | 1.8 | B | 0.318 |
| Xerox | XRX | 1.6 | B- | 0.431 |
| YPF Anonima | YPF | 1.9 | NR | 0.310 |

than some later point in time during the market's rapid ascent to current levels. Finally, there is the selection of the option-pricing formula. As I describe in Chapters 14 and 15, the effect of dividends and the early exercise provisions of American-style options is to increase the price of puts. To adopt as conservative an approach as possible, all premiums were calculated by ignoring dividends and early exercise (i.e., European-style options).

Adopting these procedures I have outlined effectively eliminated any attempt to maximum LEAP premiums by timing the market or influence the results by selecting a good year to start or a market peak at which to evaluate the final outcomes. All other baseline assumptions and specific output results are summarized in the sequence of tables that follow.

## The Results

Table 6.2 shows that by the end of March 1997, a total of 21,976 near-term and 23,914 far-term LEAP puts would have been written, or 45,890 in all. The number of near-term puts sold is less than the number of far-term puts because of the minimum eight-month expiration period that was imposed on the process. Of the 21,976 near-term puts sold, 20,022 of them would have reached their expiration dates prior to the end of the simulation on March 31, 1997. Of the 23,914 far-term puts sold, 19,383 of them would have reached their expiration dates. The remaining 1,954 near-term active LEAP puts and 4,531 far-term active LEAP puts represent open interest and are investigated as well.

Of the 20,022 near-term LEAP puts that expired, 15,178 , or 75.8 percent, expired out-ofthe money (OTM), with no financial exposure to the put writer.* This left 4,844, or 24.2 percent, of the near-term LEAP puts to expire in the money (ITM). In a similar manner, of the 19,383 far-term LEAP puts that expired, 15,457 , or 79.7 percent, expired out of the money, and 3,926 , or 20.3 percent, expired in the money. The percentage of the farterm puts that expired in the money is thus smaller than that of the near-term puts (20.3 percent versus 24.2 percent). This is a result of the additional year that the underlying stock had to recover from any financial difficulties encountered along the way, as well as of the natural growth of earnings during that time frame.

Table 6.3 shows the premiums collected and the corresponding financial exposure incurred during the study period for the LEAP puts that expired prior to March 31, 1997. The premiums collected were $\$ 3.8$ million on the near-term LEAP puts and $\$ 4.5$ million on the far-term LEAP puts. The total of almost $\$ 8.4$ million in premiums shown is just for the 39,405 LEAP puts that expired, not for the total number of 45,890 written.

So as to establish a baseline of the premiums received and financial exposure encountered, no hedging strategies whatsoever were adopted

* This ignores the possibility of early exercise when the option might have been in the money; however, as many if not most puts are purchased as insurance against market decline, in-themoney puts are ordinarily not exercised until close to expiration.
on this initial run. The premiums received in this baseline run were presumed to be immediately invested in money market funds earning a risk-free rate of return of 6 percent. Such funds, if left on deposit and compounded to the end of the simulation run on March 31, 1997, would be substantial. To focus on the underlying mechanics of the overall process, Table 6.3 considers the effects of interest earned on the premiums only between the time the premium was received and the expiration date of the corresponding LEAP put. The combined total amount of the LEAP premium and the interest earned through expiration is called the forward value of the premium, and is seen to be $\$ 4.1$ million for the near-term LEAPS and $\$ 5.1$ million for the far-term LEAP puts. It is the forward value of the premiums that is then used to cover the financial exposure incurred by various LEAP puts that expired in the money.

Financial exposure is the difference between the stock price and the strike price at expiration, if the latter is greater. For the 4,844 near-term LEAP puts expiring in the money, the financial exposure is $\$ 2.7$ million, which is equivalent to an average potential loss of $\$ 558$ per contract. For the 3,926 far-term LEAP puts expiring in the money, it is $\$ 2.9$ million for an average potential loss of $\$ 743$ per contract. Why is the average loss on the far-term ITM LEAP puts greater than the average loss on the near-term ITM LEAP puts? The reason is that the universe of 217 stocks includes several lower-rated issues that fared very poorly over the ten-year period investigated. Because of the virtually downhill price histories of these particular issues, the longer the term of the LEAP put, the greater the financial exposure encountered.

On the other hand, the higher premium associated with far-term LEAP puts often more than offsets the higher level of financial risk involved. To see this, note that the realized gain on the near-term LEAP puts is calculated as the $\$ 4,081,004$ forward value of the premiums less the $\$ 2,701,176$ in financial exposure involved, or $\$ 1,379,828$. This realized gain as a percentage of the $\$ 3,828,194$ in premiums collected on the near-term LEAP puts is 36 percent, and is referred to as the retention rate in Table 6.3. For the farterm LEAP puts, the retention rate is 48.1 percent. So while the average loss on the farterm ITM LEAP puts is higher, so is their retention rate. The overall retention rate is 42.6 percent.

Table 6.4 shows what's happening with the 6,485 active LEAP puts that had not yet expired by the cutoff date of the simulation. The premiums collected on the 1,954 active near-term LEAP puts totaled $\$ 698,972$. When invested at 6 percent per year (compounded monthly), they were worth $\$ 712,791$ on March 31, 1997. These active near-term LEAP puts had a residual value of $\$ 652,565$ on that date, for an unrealized gain of $\$ 60,226$. In a similar manner, the unrealized gain on the 4,531 active far-term LEAP puts was $\$ 266,175$. The total unrealized gain was thus $\$ 326,401$ on March 31, 1997. The number of active far-term LEAP puts is going to be much larger than the number of near-term LEAP puts because there are that many more of them whose expiration date is later than March 31, 1997.

Table 6.5 brings together the financial results on the 39,405 expired and 6,485 active LEAP puts. This table shows the effect of leaving the net realized gains on deposit to compound at 6 percent interest from expiration through the end of the study period on March 31, 1997. A total of $\$ 10,836,330$ in premiums would have been received over the ten-year study period on the 45,890 LEAP puts written, including both expired and stillactive LEAP puts. By March 31, 1997, the total realized gain and interest earned from the sale of the expired LEAP puts would have been $\$ 4,471,186$. Combining this with the unrealized gain of $\$ 326,401$ on the active puts yields an overall account value on March 31, 1997 of $\$ 4,797,587$.

As a final, overall figure of merit, we note that the account value of close to $\$ 4.8$ million on March 31,1997 , is 44.3 percent of the $\$ 10,836,330$ in premiums generated over the course of the run. It is to be emphasized that it is not the account value of $\$ 4.8$ million nor the $\$ 10.8$ million in premiums that is important here but rather the ratio of the two. Obviously, no one is going to sell one or more LEAP puts each month on every one of the possible stocks for which LEAPS are available. What we have established is that if you had sold a random number of at-the-money LEAP puts on a random number of stocks on a random schedule throughout each year over the past ten years, and invested the net premiums in money market funds, the expected value of your account balance at the end would be about 44 percent of the total premiums ever collected.

The realized and unrealized gains determined here ignore the effect of taxation and all transaction costs, fees, and commissions. These can be significant because irrespective of the holding period involved, the gains on puts that expire worthless are treated as shortterm capital gains. On this basis, after-tax results on a net commission basis would be somewhat smaller than those shown in the tables.

Of course, this isn't the real problem associated with the above results. The real problem is the high level of financial exposure relative to the premiums collected. Although only 22.3 percent of the LEAP puts will expire in the money, their effect is to force the return of 58.4 percent of the forward values of the premiums received (the complement of the 42.6 percent retention rate in Table 6.3).

In view of this, maybe my friends were correct in saying that "the gains you make on successful deals will be overwhelmed by gigantic losses on your losers." On the other hand, surely one could decrease one's financial exposure by being more discriminating about what stocks to select for selling LEAP puts on, as well as by adopting appropriate hedging strategies, such as the use of spreads and rollouts and the selling of out-of-the money puts. Each of these techniques will be considered in the chapters that follow.

## RUN NUMBER 1

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below the ATM Strike 0 Price:

Minimum No. of Months till Expiration:
8

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 5.0

Minimum Standard \& Poor's Rating: None

No. of Stocks Meeting Either Criterion: 217

Table 6.2
LEAP OTM and ITM Rates

|  | LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM Rate | Expired <br> ITM | ITM Rate | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 21,976 | 20,022 | 15,178 | $75.8 \%$ | 4,844 | $24.2 \%$ | 1,954 |
| Far: | 23,914 | 19,383 | 15,457 | $79.7 \%$ | 3,926 | $20.3 \%$ | 4,531 |
| Total: | 45,890 | 39,405 | 30,635 | $77.7 \%$ | 8,770 | $22.3 \%$ | 6,485 |

Table 6.3
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 20,022 | $\$ 3,828,194$ | $\$ 4,081,004$ | $\$ 2,701,176$ | $\$ 1,379,828$ | $36.0 \%$ |
| Far: | 19,383 | $\$ 4,526,083$ | $\$ 5,097,433$ | $\$ 2,918,755$ | $\$ 2,178,678$ | $48.1 \%$ |
| Total: | 39,405 | $\$ 8,354,277$ | $\$ 9,178,437$ | $\$ 5,619,931$ | $\$ 3,558,506$ | $42.6 \%$ |

Table 6.4
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,954 | $\$ 698,972$ | $\$ 712,791$ | $\$ 652,565$ | $\$ 60,226$ |
| Far: | 4,531 | $\$ 1,783,085$ | $\$ 1,865,301$ | $\$ 1,599,126$ | $\$ 266,175$ |
| Total: | 6,485 | $\$ 2,482,057$ | $\$ 2,578,092$ | $\$ 2,251,691$ | $\$ 326,401$ |

Table 6.5
Premiums Collected and Account Values

| Original | Premiums | Compound | Unrealized | Account <br> Contracts | Collected <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- | | Gain |
| :--- |


| Near: | 21,976 | $\$ 4,527,167$ | $\$ 1,727,337$ | $\$ 60,226$ | $\$ 1,787,564$ | $39.5 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 23,914 | $\$ 6,309,168$ | $\$ 2,743,849$ | $\$ 266,175$ | $\$ 3,010,023$ | $47.7 \%$ |
| Total: | 45,890 | $\$ 10,836,330$ | $\$ 4,471,186$ | $\$ 326,401$ | $\$ 4,797,587$ | $44.3 \%$ |

## 7-

## Eliminating Dogs

## Introduction

So far, I have considered the effect of selling at-the-money puts on the entire universe of 217 stocks that had LEAPS on March 31, 1997. You saw that 77.7 percent of the time, the stock closed out of the money, and for every $\$ 8,354$ received in premiums and interest on expired LEAPS, the net amount retained was $\$ 3,559$. The remaining portion of the premiums and interest, $\$ 5,620$, was needed to close out losing positions. Because of the longer expiration time involved, the net amount retained on the far-term LEAPS averaged out to 48.1 percent, while on the near-term LEAPS the net amount retained averaged out to just 36 percent. Finally, the account balance at the end of the ten-year period was 44.3 percent of the total premiums ever collected.

Such results are hardly worth boasting about. One way to improve them might be to restrict the sale of LEAP puts to better-quality issues. In this chapter, I'll investigate what would have happened if I had sold LEAP puts only on those issues whose underlying stocks were rated 2 or better by First Call or were rated B or better by Standard \& Poor's. We use or rather than and because the 37 stocks appearing in Table 6.1 that were not rated by Standard \& Poor's would automatically have been eliminated on that account alone. I will conduct this investigation in three phases.

In the first phase, the universe will consist of those issues whose underlying stocks were rated 2 or better by First Call or were rated B
or better by Standard \& Poor's. In the second phase, the universe will be restricted even further to those issues whose underlying stocks were rated 1.6 or better by First Call or B+ or better by Standard \& Poor's. And in the third phase, the universe will be restricted to those issues whose underlying stocks were rated 1.2 or better by First Call or A- or better by Standard \& Poor's. For lack of better nomenclature, we will refer to these populations as the "B minimum," "B+ minimum," and "A- minimum" universes.

## The B Minimum Universe

The method used in the previous chapter was first applied to those LEAPS whose underlying stocks were rated 2 or better by First Call or B or better by Standard \& Poor's. To be precise, the above criteria ought to be applied on a month-by-month basis to each stock over the ten-year history studied. But because there is no readily available history file of First Call ratings, what was done instead was to include or exclude issues on the basis of their First Call and S\&P ratings of March 31, 1997. On that basis, LEAP puts would have been sold on 178 of the 217 stocks listed in Table 6.1. As is discussed below, the elimination of the lowest-rated 39 issues substantially improved the results.

As shown in Table 7.1, the number of LEAP contracts written over the ten-year simulation decreases to 38,637 . Of these, 33,312 expired and 5,325 were still active on the cutoff date of March 31, 1997. The percentage of options expiring out of the money is now 80 percent. Although this represents an increase of just 2.4 percentage points in the OTM rate from the base level of 77.7 percent in Run No. 1, the impact on overall retention rates is significant. Table 7.2 shows that the overall retention rate grows from 42.6 percent in Run No. 1 to 54.3 percent, an increase of 11.7 percentage points. This premium retention rate is now 46.6 percent on the near-term LEAPS and 60.9 percent on the far-term LEAPS.

From Table 7.4, we see that the account value on March 31, 1997, resulting from the net premiums, accrued interest, and unrealized gains will be $\$ 5,117,983$. This figure is 57.5 percent of the $\$ 8,895,368$ in premiums ever generated.

## The B+ Minimum Universe

Suppose I had discriminated even further and restricted the sale of LEAP puts to stocks that had a First Call rating of 1.6 or better or an S\&P rating of B+ or better on March 31, 1997. The number of issues qualifying would now be just 115, with dramatically improved results.

As shown in Table 7.5, the number of LEAP contracts written decreases to 25,302 , with 21,858 having expired and 3,444 still active on March 31, 1997. The percentage of options expiring out of the money would have increased even further to 84 percent. Table 7.6 shows that the overall retention rate is now 66.2 percent, an increase of 23.6 percentage points from the baseline level of 42.6 percent in Run No. 1. The premium retention rate is now 57.8 percent on the near-term LEAPS and 73.4 percent on the farterm LEAPS.

From Table 7.8, we see that the account value on March 31, 1997, resulting from the net premiums, accrued interest, and unrealized gains will be $\$ 3,697,495$. This figure is 69.7 percent of the $\$ 5,303,771$ in premiums ever generated.

## The A- Minimum Universe

Now suppose I further restricted the sale of LEAP puts to stocks that had a First Call rating of 1.2 or better or an S\&P rating of A- or better on March 31, 1997. The number of issues qualifying would have fallen to just 50 , representing the highest-quality issues having LEAP options.

As shown in Table 7.9, the number of LEAP contracts written decreases to 11,520, with 10,018 having expired and 1,502 still active on March 31, 1997. The percentage of options expiring out of the money would have increased further still to 87.1 percent. Table 7.10 shows that the overall retention rate is now 79.9 percent, an increase of 37.3 percentage points from the base level of 42.6 percent in Run No. 1. The premium retention rate is now 71.8 percent on the near-term LEAPS and 86.8 percent on the farterm LEAPS.

From Table 7.12, we see that account value on March 31, 1997, resulting from the net premiums, accrued interest, and unrealized gains will be $\$ 1,611,512$. This figure is 84.9 percent of the $\$ 1,898,748$ in premiums ever generated.

## RUN NUMBER 2

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 0 Price:

Minimum No. of Months till Expiration:
8
Premium Reinvestment Rate: $6.0 \%$

Minimum First Call Rating: 2.0
Minimum Standard \& Poor's Rating: B
No. of Stocks Meeting Either Criterion: 178

Table 7.1
LEAP OTM and ITM Rates

|  | LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM Rate | Expired <br> ITM | ITM Rate | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 18,501 | 16,898 | 13,180 | $78.0 \%$ | 3,718 | $22.0 \%$ | 1,603 |
| Far: | 20,136 | 16,414 | 13,465 | $82.0 \%$ | 2,949 | $18.0 \%$ | 3,722 |
| Total: | 38,637 | 33,312 | 26,645 | $80.0 \%$ | 6,667 | $20.0 \%$ | 5,325 |

Table 7.2
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 16,898 | $\$ 3,117,588$ | $\$ 3,323,413$ | $\$ 1,871,962$ | $\$ 1,451,451$ | $46.6 \%$ |
| Far: | 16,414 | $\$ 3,686,137$ | $\$ 4,151,508$ | $\$ 1,907,776$ | $\$ 2,243,732$ | $60.9 \%$ |
| Total: | 33,312 | $\$ 6,803,725$ | $\$ 7,474,921$ | $\$ 3,779,739$ | $\$ 3,695,183$ | $54.3 \%$ |

Table 7.3
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,603 | $\$ 602,343$ | $\$ 614,183$ | $\$ 524,708$ | $\$ 89,474$ |
| Far: | 3,722 | $\$ 1,489,300$ | $\$ 1,556,507$ | $\$ 1,184,486$ | $\$ 372,020$ |
| Total: | 5,325 | $\$ 2,091,643$ | $\$ 2,170,689$ | $\$ 1,709,195$ | $\$ 461,495$ |

Table 7.4
Premiums Collected and Account Values
Original

Contracts \begin{tabular}{l}
Premiums <br>
Collected

$\quad$

Compound <br>
Gain

$\quad$

Unrealized <br>
Value

 

Account <br>
Value

$\quad$

Value <br>
Ratio
\end{tabular}

| Near: | 18,501 | $\$ 3,719,931$ | $\$ 1,817,314$ | $\$ 89,474$ | $\$ 1,906,788$ | $51.3 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 20,136 | $\$ 5,175,437$ | $\$ 2,839,175$ | $\$ 372,020$ | $\$ 3,211,195$ | $62.0 \%$ |
| Total: | 38,637 | $\$ 8,895,368$ | $\$ 4,656,489$ | $\$ 461,495$ | $\$ 5,117,983$ | $57.5 \%$ |

## RUN NUMBER 3

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 0 Price:

Minimum No. of Months till Expiration:
8

Premium Reinvestment Rate: $6.0 \%$

Minimum First Call Rating: 1.6

Minimum Standard \& Poor's Rating: B+
No. of Stocks Meeting Either Criterion: 115

Table 7.5
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired | OTM Rate | Expired | ITM Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | LEAPS


| Near: | 12,116 | 11,080 | 9,055 | $81.7 \%$ | 2,025 | $18.3 \%$ | 1,036 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | 10,778 | 9,299 | $86.3 \%$ | 1,479 | $13.7 \%$ | 2,408 |
| Total: | 25,302 | 21,858 | 18,354 | $84.0 \%$ | 3,504 | $16.0 \%$ | 3,444 |

Table 7.6
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 11,080 | $\$ 1,835,915$ | $\$ 1,957,072$ | $\$ 895,583$ | $\$ 1,061,489$ | $57.8 \%$ |
| Far: | 10,778 | $\$ 2,156,467$ | $\$ 2,428,733$ | $\$ 1,846,840$ | $\$ 1,581,893$ | $73.4 \%$ |

Total: $\quad 21,858 \quad \$ 3,992,382 \quad \$ 4,385,805 \quad \$ 1,742,423 \quad \$ 2,643,382 \quad 66.2 \%$

Table 7.7
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,036 | $\$ 386,048$ | $\$ 393,551$ | $\$ 330,773$ | $\$ 62,778$ |
| Far: | 2,408 | $\$ 1,925,341$ | $\$ 1,966,239$ | $\$ 1,689,007$ | $\$ 277,233$ |
| Total: | 3,444 | $\$ 1,311,389$ | $\$ 1,359,790$ | $\$ 1,019,779$ | $\$ 340,010$ |

Table 7.8
Premiums Collected and Account Values

| Original | Premiums | Compound <br> Contracts | Unrealized <br> Collected | Account <br> Gain | Value |
| :--- | :--- | :--- | :--- | :--- | :--- |


| Near: | 12,116 | $\$ 2,221,964$ | $\$ 1,340,532$ | $\$ 62,778$ | $\$ 1,403,309$ | $63.2 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | $\$ 3,081,807$ | $\$ 2,016,953$ | $. \$ 277,233$ | $\$ 2,294,186$ | $74.4 \%$ |
| Total: | 25,302 | $\$ 5,303,771$ | $\$ 3,357,485$ | $\$ 340,010$ | $\$ 3,697,495$ | $69.7 \%$ |

## RUN NUMBER 4

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 0 Price:

Minimum No. of Months till Expiration:
8

Premium Reinvestment Rate: $6.0 \%$

Minimum First Call Rating:
1.2

Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 7.9
LEAP OTM and ITM Rates

|  | LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM Rate | Expired <br> ITM | ITM Rate | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,516 | 5,065 | 4,292 | $84.7 \%$ | 773 | $15.3 \%$ | 451 |
| Far: | 16,004 | 14,953 | 4,435 | $89.5 \%$ | , 1518 | $10.5 \%$ | 1,051 |
| Total: | 11,520 | 10,018 | 8,727 | $87.1 \%$ | 1,291 | $12.9 \%$ | 1,502 |

Table 7.10
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,065 | $\$ 656,632$ | $\$ 700,038$ | $\$ 228,728$ | $\$ 471,310$ | $71.8 \%$ |
| Far: | 14,953 | $\$, 1783,524$ | $\$, 1882,534$ | $\$ 202,719$ | $\$, 1679,815$ | $86.8 \%$ |
| Total: | 10,018 | $\$ 1,440,155$ | $\$ 1,582,571$ | $\$ 431,447$ | $\$ 1,151,125$ | $79.9 \%$ |

Table 7.11
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | Active |  | Value | Value |  |
| Far: | 1,051 | $\$ 138,639$ | $\$ 141,294$ | $\$ 116,837$ | $\$ 24,457$ |
| Total: | 1,502 | $\$ 319,954$ | $\$ 333,714$ | $\$ 218,707$ | $\$ 115,007$ |
|  |  | $\$ 458,593$ | $\$ 475,008$ | $\$ 335,544$ | $\$ 139,464$ |

Table 7.12
Premiums Collected and Account Values

| Original | Premiums <br> Contracts | Compound <br> Gain | Unrealized <br> Gain | Account | Value |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  | Value | Ratio |  |


| Near: | 5,516 | $\$ 795,270$ | $\$ 603,605$ | $\$ 24,457$ | $\$ 628,062$ | $79.0 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | $\$ 1,103,477$ | $\$, 1868,443$ | $\$ 115,007$ | $\$, 1983,450$ | $89.1 \%$ |
| Total: | 11,520 | $\$ 1,898,748$ | $\$ 1,472,048$ | $\$ 139,464$ | $\$ 1,611,512$ | $84.9 \%$ |

## Summary of Results

As a way of comparing the results obtained so far, let's tabulate the OTM rates, retention rates, and overall ten-year value ratios for the four cases investigated.

Table 7.13
Figures of Merit as a Function of Stock Rating

| Run No. | No. of | Steady-State | Steady-State <br> Retention Rate | Ten-Year <br> Value Ratio |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1. | Universe | Issues | OTM Rate |  |  |
| 2. | All | 217 | $77.7 \%$ | $42.6 \%$ | $44.3 \%$ |
| 3. | B min | 178 | 80.0 | 54.3 | 57.5 |
| 4. | B+ min | 115 | 84.0 | 66.2 | 69.7 |

As Table 7.13 clearly shows, as the quality of the underlying stocks increases, the greater the chance that the options will expire out of the money, the greater the percentage of premiums retained, and the greater the account balance as a percentage of premiums collected.

I do not mean to imply that investors should limit the sale of LEAP puts strictly to highquality companies rated $\mathrm{B}+$ or better. Situations will arise from time to time where it is financially advantageous to sell options on companies with lesser-quality issues, especially in those instances involving reorganizations, turnarounds, takeovers, and mergers.

## 8 -

## Out-of-the-Money LEAPS

## Introduction

We saw in the previous chapter that restricting the sale of at-the-money LEAP puts to better stocks could significantly increase the proportion of LEAPS that would expire worthless, thereby reducing financial risk and increasing retention rates and ultimate profitability. Another way to reduce risk while maintaining adequate retention rates is to sell LEAP puts that are one or more steps below the at-the-money exercise price. However, although writing out-of-the-money puts is certainly safer than writing at-themoney puts, the premiums will be correspondingly smaller because of the reduced level of risk involved. Whether such a strategy is cost effective is the subject of this chapter.

My study employs two series of computer runs. In the first series, I repeat the simulations performed in Runs No. 3 and 4, but this time all of the strike prices are set one step below the at-the-money exercise prices used earlier. Recall that strike price intervals for LEAP (and standard) options are set in increments of $\$ 2.50$ when the stock price is between $\$ 5$ and $\$ 25$, in increments of $\$ 5$ when the stock price is between $\$ 25$ and $\$ 200$, and in increments of $\$ 10$ when the strike price is over $\$ 200$. For a stock price of $\$ 21$, for example, the at-the-money strike price is taken as $\$ 20$, so the one-step out-of-the-money strike price is going to be $\$ 17.50$.

In the second series, we repeat the simulations, but this time with all of the strike prices set two steps below the at-the-money exercise prices used before.

## One-Step OTM LEAPS on the B+ Minimum Universe

Run No. 5 is the analog of Run No. 3, in which the sale of LEAP puts was restricted to the 115 stocks in the $\mathrm{B}+$ minimum universe, but this time the strike prices are set one step out of the money. As shown in Table 8.1, the number of LEAP contracts written is again 25,302 , with 21,858 contracts expired and 3,444 still active on March 31, 1997. The percentage of options expiring out of the money increases from 84 percent in Run No. 3 to 92.5 percent.

Setting the exercise price one step below the ATM strike price reduces risk significantly but heavily impacts the premiums received. This can be readily observed by comparing the $\$ 2,066,174$ in premiums collected for the expired LEAP puts in Table 8.2 against the $\$ 3,992,382$ in premiums shown in Table 7.6. On the other hand, the overall retention increases from 66.2 percent in Table 7.6 to 70.4 percent in Table 8.2. Account value as a percentage of total premiums collected is up from 69.7 percent in Table 7.8 to 72.6 percent in Table 8.4.

## One-Step OTM LEAPS on the A- Minimum Universe

Run No. 6 is the analog of Run No. 4, in which the sale of LEAP puts was restricted to the 50 stocks in the A- minimum universe, but this time with the strike prices set at one step out of the money. As shown in Table 8.5, the number of LEAP contracts written is again 11,520, with 10,018 contracts expired and 1,502 still active on March 31, 1997. The percentage of options expiring out of the money increases from 87.1 percent in Run No. 4 to 95.1 percent.

Setting the exercise price one step below the ATM strike price again reduces risk significantly and again heavily impacts the premiums received: compare the \$649,621 in premiums collected for the expired LEAP puts in Table 8.6 against the $\$ 1,440,155$ in premiums in Table 7.10. And again, the overall retention rate increases from 79.9 percent in Table 7.10 to 90 percent in Table 8.6. Account value as a
percentage of total premiums collected is now 91.6 percent (Table 8.8), well ahead of the 84.9 percent figure seen in Table 7.12.

## Two-Step OTM LEAPS on the B+ Minimum Universe

Run No. 7 is the analog of Run No. 3, in which the sale of LEAP puts was restricted to the 115 stocks in the $\mathrm{B}+$ minimum universe but this time with the strike prices set at two steps out of the money. As shown in Table 8.9, the number of LEAP contracts written is again 25,302 , with 21,858 contracts expired and 3,444 still active on March 31, 1997. The percentage of options expiring out of the money increases from 84 percent in Run No. 3 to 95.6 percent.

As you might predict, setting the exercise price two steps below the ATM strike price greatly reduces risk but also impacts the premiums received even more dramatically. Compare the $\$ 1,136,869$ in premiums collected for expired LEAP puts in Table 8.10 against the $\$ 3,992,382$ shown in Table 7.6. The overall retention rate in Table 8.10 increases to 71.1 percent from the 66.2 percent figure seen in Table 7.6. Account value as a percentage of total premiums collected in Table 8.12 is now 73.6 percent, up from 69.7 percent in Table 7.8.

## Two-Step OTM LEAPS on the A- Minimum Universe

Run No. 8 is the analog of Run No. 4, in which the sale of LEAP puts was restricted to the 50 stocks in the A-minimum universe but now with the strike prices set at two steps out of the money. As shown in Table 8.13, the number of LEAP contracts written is again 11,520, with 10,018 contracts expired and 1,502 still active on March 31, 1997. The percentage of options expiring out of the money increases from 87.1 percent in Run No. 4 to 97.1 percent.

The other results are entirely predictable. Premiums collected for the expired LEAP puts total $\$ 330,155$ in Table 8.14 compared with the $\$ 1,440,155$ in Table 7.10. The overall retention rate increases from 79.9 percent in Table 7.10 to 95.7 percent, and account value as a percentage of total premiums collected is now 98.3 percent in Table 8.16, well ahead of the 84.9 percent seen in Table 7.12.

## RUN NUMBER 5

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 1 Price:

Minimum No. of Months till Expiration:
8

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.6
Minimum Standard \& Poor's Rating: B+
No. of Stocks Meeting Either Criterion: 115

Table 8.1
LEAP OTM and ITM Rates

| LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM Rate | Expired <br> ITM | ITM | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 12,116 | 11,080 | 10,177 | $91.9 \%$ | 903 | $8.1 \%$ | 1,036 |
| 13,186 | 10,778 | 10,040 | $93.2 \%$ | 1,738 | $6.8 \%$ | 2,408 |
| 25,302 | 21,858 | 20,217 | $92.5 \%$ | 1,641 | $7.5 \%$ | 3,444 |

Table 8.2
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 11,080 | $\$ 870,704$ | $\$ 929,123$ | $\$ 393,369$ | $\$ 535,754$ | $61.5 \%$ |
| Far: | 10,778 | $\$ 1,195,471$ | $\$ 1,347,097$ | $\$ 429,109$ | $\$ 1,917,989$ | $76.8 \%$ |

Total: $21,858 \quad \$ 2,066,174 \quad \$ 2,276,221 \quad \$ 822,478 \quad \$ 1,453,743 \quad 70.4 \%$

Table 8.3
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual <br> Value | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 1,036 | $\$ 232,269$ | $\$ 236,786$ | $\$ 194,803$ | $\$ 41,982$ |
| Far: | 2,408 | $\$ 593,555$ | $\$ 618,822$ | $\$ 444,505$ | $\$ 174,317$ |
| Total: | 3,444 | $\$ 825,824$ | $\$ 855,608$ | $\$ 639,308$ | $\$ 216,300$ |

Table 8.4
Premiums Collected and Account Values

| Original | Premiums | Compound <br> Contracts | Unrealized <br> Collected | Account <br> Gain | Value |
| :--- | :--- | :--- | :--- | :--- | ---: |


| Near: | 12,116 | $\$ 1,102,973$ | $\$ 690,495$ | $\$ 41,982$ | $\$ 732,477$ | $66.4 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | $\$ 1,789,026$ | $\$ 1,191,361$ | $\$ 174,317$ | $\$ 1,365,678$ | $76.3 \%$ |
| Total: | 25,302 | $\$ 2,891,998$ | $\$ 1,881,855$ | $\$ 216,300$ | $\$ 2,098,155$ | $72.6 \%$ |

## RUN NUMBER 6

ATM Strike Price Is the High, Low, or Closing ..... C
Stock Price:
No. of Steps LEAP Put Is below ATM Strike ..... 1
Price:
Minimum No. of Months till Expiration: ..... 8
Premium Reinvestment Rate: ..... 6.0\%
Minimum First Call Rating: ..... 1.2
Minimum Standard \& Poor's Rating: ..... A-
No. of Stocks Meeting Either Criterion: ..... 50

Table 8.5
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired | OTM Rate | Expired | ITM |
| :--- | :--- | :--- | :--- | :--- | :--- | | LEAPS |
| :--- |
| Written | Expired | OTM |  | ITM |
| :--- | :--- | :--- |


| Near: | 5,516 | 5,065 | 4,800 | $94.8 \%$ | 265 | $5.2 \%$ | 451 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | 14,953 | 4,729 | $95.5 \%$ | 224 | $4.5 \%$ | 1,051 |
| Total: | 11,520 | 10,018 | 9,529 | $95.1 \%$ | 489 | $4.9 \%$ | 1,502 |

Table 8.6
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS <br> Expired | Premiums <br> Collected | Forward | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 5,065 | $\$ 264,349$ | $\$ 282,199$ | $\$ 65,498$ | $\$ 216,701$ | $82.0 \%$ |
| 14,953 | $\$ 385,272$ | $\$ 434,226$ | $\$ 166,443$ | $\$ 367,784$ | $95.5 \%$ |

Total: $\quad 10,018 \quad \$ 649,621 \quad \$ 716,426 \quad \$ 131,940 \quad \$ 584,485 \quad 90.0 \%$

Table 8.7
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | Active | Value | Value |  |  |
| Far: | 1,051 | $\$ 76,630$ | $\$ 78,093$ | $\$ 63,358$ | $\$ 14,735$ |
| Total: | 1,502 | $\$ 269,212$ | $\$ 196,907$ | $\$ 128,283$ | $\$ 68,623$ |
|  |  | $\$ 275,000$ | $\$ 191,641$ | $\$ 83,359$ |  |

Table 8.8
Premiums Collected and Account Values

| Original | Premiums | Compound <br> Contracts | Unrealized <br> Collected | Account <br> Gain | Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |


| Near: | 5,516 | $\$ 340,979$ | $\$ 280,707$ | $\$ 14,735$ | $\$ 295,443$ | $86.6 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | $\$ 574,484$ | $\$ 474,186$ | $\$ 68,623$. | $\$ 542,809$ | $94.5 \%$ |
| Total: | 11,520 | $\$ 915,463$ | $\$ 754,893$ | $\$ 83,359$ | $\$ 838,252$ | $91.6 \%$ |

## RUN NUMBER 7

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 2 Price:

Minimum No. of Months till Expiration: 8
Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.6
Minimum Standard \& Poor's Rating: B+

No. of Stocks Meeting Either Criterion: 115

Table 8.9
LEAP OTM and ITM Rates

| LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM Rate | Expired <br> ITM | ITM | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 12,116 | 11,080 | 10,547 | $95.2 \%$ | 533 | $4.8 \%$ | 1,036 |
| 13,186 | 10,778 | 10,343 | $96.0 \%$ | 435 | $4.0 \%$ | 2,408 |
| 25,302 | 21,858 | 20,890 | $95.6 \%$ | 968 | $4.4 \%$ | 3,444 |

Table 8.10
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 11,080 | $\$ 447,303$ | $\$ 477,653$ | $\$ 208,363$ | $\$ 269,291$ | $60.2 \%$ |
| Far: | 10,778 | $\$ 1,689,566$ | $\$ 1,777,415$ | $\$ 237,967$ | $\$ 539,448$ | $78.2 \%$ |

Total: 21,858 \$1,136,869 \$1,255,068 \$446,329 \$808,739 71.1\%

Table 8.11
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,036 | $\$ 133,071$ | $\$ 135,651$ | $\$ 111,068$ | $\$ 24,583$ |
| Far: | 2,408 | $\$ 364,184$ | $\$ 379,020$ | $\$ 280,836$ | $\$ 198,184$ |
| Total: | 3,444 | $\$ 497,255$ | $\$ 514,671$ | $\$ 391,904$ | $\$ 122,767$ |

Table 8.12
Premiums Collected and Account Values
Original

Contracts \begin{tabular}{ll}
Premiums <br>
Collected

$\quad$

Compound <br>
Gain

$\quad$

Unrealized <br>
Gain

 Account 

Value <br>
\end{tabular}

| Near: | 12,116 | $\$ 580,374$ | $\$ 360,255$ | $\$ 24,583$ | $\$ 384,837$ | $66.3 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | $\$ 1,053,750$ | $\$ 1,720,099$ | $\$ 198,184$ | $\$ 1,818,283$ | $77.7 \%$ |
| Total: | 25,302 | $\$ 1,634,124$ | $\$ 1,080,354$ | $\$ 122,767$ | $\$ 1,203,120$ | $73.6 \%$ |

## RUN NUMBER 8

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 2 Price:

Minimum No. of Months till Expiration: 8
Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.2
Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 8.13
LEAP OTM and ITM Rates
LEAPS

Written \begin{tabular}{lllll}
LEAPS <br>
Expired

 

Expired <br>
OTM

$\quad$ OTM $\quad$

Expired <br>
ITM

$\quad$

ITM

 

LEAPS <br>
Active
\end{tabular}

Table 8.14
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,065 | $\$ 123,882$ | $\$ 132,344$ | $\$ 28,160$ | $\$ 104,184$ | $84.1 \%$ |
| Far: | 14,953 | $\$ 206,272$ | $\$ 232,609$ | $\$ 20,686$ | $\$ 211,922$ | $102.7 \%$ |

Total: 10,018 $\$ 330,155 \quad \$ 364,952 \quad \$ 48,846 \quad \$ 316,106 \quad 95.7 \%$

Table 8.15
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual <br> Value | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 451 | $\$ 39,263$ | $\$ 40,008$ | $\$ 32,289$ | $\$ 7,719$ |
| Far: | 1,051 | $\$ 104,640$ | $\$ 108,597$ | $\$ 172,106$ | $\$ 36,491$ |
| Total: | 1,502 | $\$ 143,903$ | $\$ 148,605$ | $\$ 104,395$ | $\$ 44,210$ |

Table 8.16
Premiums Collected and Account Values

| Original | Premiums | Compound | Unrealized | Account | Value |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Contracts | Collected | Gain $>$ | Gain | Value | Ratio |


| Near: | 5,516 | $\$ 163,146$ | $\$ 140,287$ | $\$ 7,719$ | $\$ 148,006$ | $90.7 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | $\$ 310,912$ | $\$ 281,540$ | $\$ 36,491$ | $\$ 318,031$ | $102.3 \%$ |
| Total: | 11,520 | $\$ 474,058$ | $\$ 421,826$ | $\$ 44,210$ | $\$ 466,037$ | $98.3 \%$ |

## Summary of Results

To compare the results obtained, let's again tabulate the OTM rate, the retention rate, and the overall ten-year value ratio for the runs done so far.

Table 8.17
Figure of Merit Comparisons

| Run No. | Universe | No. of Issues | Steps below ATM | Steady-State OTM Rate | Steady-State <br> Retention <br> Rate | Ten-Year <br> Account <br> Ratio |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | All | 217 | 0 | 77.7\% | 42.6\% | 44.3\% |
| 2. | B min | 178 | 0 | 80.0 | 54.3 | 57.5 |
| 3. | $B+\min$ | 115 | 0 | 84.0 | 66.2 | 69.7 |
| 4. | A- min | 50 | 0 | 87.1 | 79.9 | 84.9 |
| 5. | B+ rain | 115 | 1 | 92.5 | 70.4 | 72.6 |
| 6. | A- min | 50 | 1 | 95.1 | 90.0 | 91.6 |
| 7. | $B+\min$ | 115 | 2 | 95.6 | 71.1 | 73.6 |
| 8. | A- min | 50 | 2 | 97.1 | 95.7 | 98.3 |

As seen in Table 8.17, for the B+ minimum universe of 115 stocks, the proportion of LEAPS expiring worthless is seen to rise from a low of 84 percent to 92.5 percent to 95.6 percent as exercise prices are moved further out of the money. The corresponding retention rates and account ratios improve somewhat: retention rates move from 66.2 percent to 70.4 percent to 71.1 percent, and account ratios move from 69.7 percent to 72.6 percent to 73.6 percent.

For the A- minimum universe of 50 stocks, the proportion of LEAPS expiring worthless is seen to rise from a low of 87.1 percent to 95.1 percent to 97.1 percent as exercise prices are moved further out of the money. This time, however, the corresponding retention rates and account ratios improve significantly, the former going from 79.9 percent to 90 percent to 95.7 percent, the latter moving from 84.9 percent to 91.6 percent to 98.3 percent.

What all this tells us is that by writing out-of-the-money LEAP puts on better-quality stocks, it is possible to bring up the proportion of LEAPS expiring worthless to levels well over 95 percent and achieve premium retention rates of 90 percent or more, with account ratios as high as 98 percent of the total premiums collected. Mind you,
these results are calculated from the sale of a random number of out-of-the-money LEAP puts on a random number of these better-quality stocks on a random schedule throughout each year over a ten-year period. As such, they do not reflect any tactical decision making or any involvement on the part of the investor other than his or her investing the net premiums in money market funds.

The next chapter investigates the extent to which the above results can be improved by using a simple recovery-and-repair strategy in those situations where LEAP contracts appear to be expiring in the money as their expiration dates approach.

## 9 -

## Roll 'Em Out

## Introduction

The previous chapter demonstrated that by writing LEAP puts on higher-quality issues one or two steps below the at-the-money market price, it is possible to increase the rate at which the options expire out of the money to levels ranging from 92 percent to 97 percent. An impressive result, to be sure, but more impressive results can be achieved by rolling out any LEAP puts that appear to be winding up in the money as expiration approaches. This entails a two-step process of (1) buying back the LEAP puts shortly before the expiration date (thus closing out those positions), and (2) writing an equivalent number of LEAP puts with expiration dates either one or two years away.

You saw in Chapter 3 that there are numerous ways to carry out this type of mitigation strategy. Besides selecting the expiration date, you can also choose an appropriate strike price. Suppose an at-the-money LEAP put had been sold on a stock with a volatility of 0.40 and the price was $\$ 100$ a share with 25 months to expiration. From Table 2.1, you see that the (European-style) option premium is very close to $\$ 1,600$ per contract. Now suppose that some two years later the stock is, unfortunately, down to $\$ 90$. To close out the position, you buy back the option for close to its intrinsic value* of $\$ 1,000$, a strategy that by

* The intrinsic value of an in-the-money put or call option is the difference between the strike price and stock price.
itself would ensure an overall profit of $\$ 600$ per contract, even after commissions (remember that the premium has been earning interest for a year and a half).

What happens next is that you roll out the option. Because the month is January (that's when all LEAPS expire), there will be two replacement LEAPS available: the near-term LEAP put expiring the following January and the far-term LEAP put expiring the January two years away. There will, of course, be a range of strike prices available to you-S $95, \$ 90, \$ 85$, and so on; most likely, the original $\$ 100$ price will be available and perhaps an $\$ 80$ strike as well. With two expiration dates (near and far) and, say, five strike prices at or near the money, there are as many as ten viable alternatives open to you. Which of these to select will depend on how long you feel will be required before the company resumes its earnings growth, regains market share lost, or otherwise recovers its former price levels. The more rapid and certain the recovery, the higher the strike price and shorter the term you can afford to select. The weaker the prospects of recovery, the lower the strike price and longer the term you should select. If the company has really faltered, your best course of action may well be to limit further financial exposure and not perform the second leg of the procedure.

## Procedure

To investigate the extent to which the use of rollovers can mitigate financial exposure and thereby enhance overall performance, the following two assumptions were made in all instances where a LEAP put wound up in the money as expiration approached: (1) the in-the-money LEAP put was purchased for its intrinsic value (the difference between stock and exercise prices at expiration), and (2) a single LEAP put was then sold at a strike price and expiration date that reflected the same philosophy as that governing the original LEAP put. That is, if the original LEAP put was a near-term one, the replacement LEAP put sold was also near-term (with an expiration date one year away); if the original LEAP put was a far-term one, the replacement LEAP put sold was also far-term (with an expiration date two years away).

Similarly, if the original LEAP put was out of the money, at the money, or in the money at the time it was sold, a correspondingly conservative, neutral, or aggressive stance was adopted for the replacement

LEAP put sold. That is, LEAP puts originally one step out of the money were replaced by one-step out-of-the-money puts. These strike prices are relative to the stock price at the time, so in the example cited previously, the at-the-money LEAP put of $\$ 100$ would be replaced by an at-the-money $\$ 90$ LEAP put with an expiration date two years away.

With this approach in mind, six computer simulations were conducted in order to determine the impact of rollovers on the bottom line. These simulations were run for the at-the-money LEAPS, one-step out-of-the-money LEAPS, and two-step out-of-themoney LEAPS, in each case for both the $\mathrm{B}+$ minimum and $\mathrm{A}-$ minimum stock universes.

## Rolling At-the-Money LEAPS

Run No. 9 is the analog of Run No. 3 and shows the effect of adopting a rollover strategy for any issues winding up in the money from among the 115 stocks in the $\mathrm{B}+$ minimum universe. As a result of rollovers, the total number of LEAP contracts written increases from 25,302 to 29,292 . The net effect of rollovers is to reduce the ITM exposure of $\$ 3,174,423$ in Run No. 3 to $\$ 1,249,983$ (using the premiums received from the additional LEAP contracts for that purpose). As a result, the retention rate on the premiums received from the sale of the expired LEAP contracts increases from 66.2 percent in Run No. 3 to the 78.5 percent shown in Table 9.2. From Table 9.4 you see that the account value on March 31, 1997, will have grown to $\$ 4,360,099$. This sum is 80.3 percent of the total premiums collected over the ten-year period and is significantly higher than the 69.7 percent without rollovers seen in Run No. 3.

Run No. 10 is the analog of Run No. 4 and shows the effect of adopting a rollover strategy for any stocks winding up in the money from among the 50 issues in the Aminimum universe. As a result of rollovers, the total number of LEAP contracts written increases from 11,520 to 12,932 . The net effect of rollovers is to reduce the ITM exposure of $\$ 431,447$ in Run No. 4 to $\$ 247,180$ (again using the premiums received from the additional LEAP contracts for that purpose). As a result, the retention rate on the premiums received from the sale of the expired LEAP contracts increases from 79.9 percent in Run No. 4 to 92.7 percent, as shown in Table 9.6. From Table 9.8, we see that the account value on March 31, 1997, will have grown to $\$ 1,849,570$. This
sum is 95.9 percent of the total premiums collected over the ten-year period and is significantly higher than the 84.9 percent without rollovers seen in Run No. 4.

## Rolling One-Step Out-of-the-Money LEAPS

Run No. 11 is the analog of Run No. 5 and shows the effect of adopting a rollover strategy for any stocks winding up in the money from among the 115 issues in the $\mathrm{B}+$ minimum universe. As a result of rollovers, the total number of LEAP contracts written increases from 25,302 to 27,074 . Yet again, the net effect of rollovers is to reduce the ITM exposure of $\$ 822,478$ in Run No. 5 to $\$ 686,414$. The retention rate on the premiums received from the sale of the expired LEAP contracts increases from 70.4 percent in Run No. 5 to 76.9 percent, as shown in Table 9.10. From Table 9.12, you see that the account value on March 31, 1997, will have grown to $\$ 2,284,359$. This sum is 77.9 percent of the total premiums collected over the ten-year period and is significantly higher than the 72.6 percent without rollovers seen in Run No. 5.

Run No. 12 is the analog of Run No. 6 and shows the effect of adopting a rollover strategy for any stocks winding up in the money from among the 50 issues in the Aminimum universe. As a result of rollovers, the total number of LEAP contracts written increases from 11,520 to 12,010 . The net effect of rollovers is to reduce the ITM exposure of $\$ 131,940$ in Run No. 6 to $\$ 91,637$. The retention rate on the premiums received from the sale of the expired LEAP contracts increases from 90 percent to 96.2 percent, as shown in Table 9.14, and from Table 9.16 you see that the account value on March 31, 1997, will have grown to $\$ 891,361$. This is 96.8 percent of the total premiums collected over the ten-year period and is significantly higher than the 91.6 percent without rollovers seen in Run No. 6.

Note that the retention rate for the far-term LEAPS is 101.8 percent. Retention rates greater than 100 percent can be achieved as a result of the interest earned between the sale of options and their corresponding expiration dates.

## Rolling Two-Step Out-of-the-Money LEASPS

Run No. 13 is the analog of Run No. 7 and shows the effect of adopting a rollover strategy for the 115 issues in the $\mathrm{B}+$ minimum universe. As a result of rollovers, the total number of LEAP contracts written increases from 25,302 to 26,306 . The rollovers reduce the ITM exposure from $\$ 446,329$ in Run No. 7 to $\$ 390,194$. The retention rate on the premiums received increases from 71.1 percent to 76.1 percent, as shown in Table 9.18. From Table 9.20, you see that the account value on March 31, 1997, will have grown to $\$ 1,281,850$, which is 77.5 percent of the total premiums collected over the ten-year period and which is significantly higher than the 73.6 percent without rollovers seen in Run No. 7.

Run No. 14 is the analog of Run No. 8 and shows the effect of adopting a rollover strategy for any stocks winding up in the money for the 50 issues in the A- minimum universe. As a result of rollovers, the total number of LEAP contracts written goes from 11,520 to 11,815 . The rollovers reduce the ITM exposure from $\$ 48,846$ in Run No. 8 to $\$ 32,351$, and the retention rate on the premiums received increases from 95.7 percent to 100.7 percent, as shown in Table 9.22. From Table 9.24, you see that the account value on March 31, 1997, will have grown to $\$ 490,331$, which is 103.2 percent of the total premiums collected over the ten-year period and is higher than the 98.3 percent without rollovers seen in Run No. 8. As you saw in Run No. 12, retention rates greater than 100 percent can be achieved as a result of the interest earned between the sale of options and their corresponding expiration dates.

## RUN NUMBER 9

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 0 Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y
ITM Far-Term LEAPS Are Rolled Over: Y

Premium Reinvestment Rate: $6.0 \%$

Minimum First Call Rating: 1.6

Minimum Standard \& Poor's Rating: B+

No. of Stocks Meeting Either Criterion: 115

Table 9.1
LEAP OTM and Rollout Rates

| LEAPS | LEAPS | Expired <br> Written | Expired | OTM | LEAPS | Rollout |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | | LEAPS |
| :--- |
| OTM |


| Near: | 14,496 | 13,321 | 10,941 | $82.1 \%$ | 2,380 | $17.9 \%$ | 1,175 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 14,796 | 12,076 | 10,466 | $86.7 \%$ | 1,610 | $13.3 \%$ | 2,720 |
| Total: | 29,292 | 25,397 | 21,407 | $84.3 \%$ | 3,990 | $15.7 \%$ | 3,895 |

Table 9.2
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums | Forward | ITM | Realized | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Expired | Collected | Value | Exposure | Gain | Rate |


| Near: | 13,321 | $\$ 1,835,915$ | $\$ 1,957,072$ | $\$ 654,353$ | $\$ 1,302,719$ | $71.0 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 12,076 | $\$ 2,156,467$ | $\$ 2,428,733$ | $\$ 1,595,630$ | $\$ 1,833,103$ | $85.0 \%$ |
| Total: | 25,397 | $\$ 3,992,382$ | $\$ 4,385,805$ | $\$ 1,249,983$ | $\$ 3,135,821$ | $78.5 \%$ |

Table 9.3
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual <br> Value | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 1,175 | $\$ 427,669$ | $\$ 435,578$ | $\$ 376,392$ | $\$ 59,186$ |
| Far: | 2,720 | $\$ 1,010,901$ | $\$ 1,054,817$ | $\$ 1,750,400$ | $\$ 304,417$ |
| Total: | 3,895 | $\$ 1,438,571$ | $\$ 1,490,395$ | $\$ 1,126,792$ | $\$ 363,603$ |

Table 9.4
Premiums Collected and Account Values

| Original | Premiums <br> Contracts | Compound <br> Collected | Unrealized | Account <br> Gain | Galue |
| :--- | :--- | :--- | :--- | :--- | :--- |


| Near: | 12,116 | $\$ 2,263,585$ | $\$ 1,661,559$ | $\$ 59,186$ | $\$ 1,720,745$ | $76.0 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | $\$ 3,167,368$ | $\$ 2,334,938$ | $\$ 304,417$ | $\$ 2,639,354$ | $83.3 \%$ |
| Total: | 25,302 | $\$ 5,430,953$ | $\$ 3,996,497$ | $\$ 363,603$ | $\$ 4,360,099$ | $80.3 \%$ |

## RUN NUMBER 10

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 0 Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y
ITM Far-Term LEAPS Are Rolled Over: Y

Premium Reinvestment Rate: $6.0 \%$

Minimum First Call Rating: 1.2

Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 9.5
LEAP OTM and Rollout Rates

| LEAPS Written | LEAPS <br> Expired | Expired OTM | OTM | LEAPS Rolled | Rollout Rate | LEAPS <br> Active |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Rate |  |  |  |
| 6,396 | 5,899 | 5,019 | 85.1\% | 880 | 14.9\% | 497 |
| 16,536 | 15,383 | 4,851 | 90.1\% | 1,532 | 19.9\% | 1,153 |
| 12,932 | 11,282 | 9,870 | 87.5\% | 1,412 | 12.5\% | 1,650 |

Table 9.6
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums | Forward | ITM | Realized | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Expired | Collected | Value | Exposure | Gain | Rate |


| Near: | 5,899 | $\$ 656,632$ | $\$ 700,038$ | $\$ 134,574$ | $\$ 565,464$ | $86.1 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 15,383 | $\$, 1783,524$ | $\$, 1882,534$ | $\$ 112,606$ | $\$, 1769,927$ | $98.3 \%$ |
| Total: | 11,282 | $\$ 1,440,155$ | $\$ 1,582,571$ | $\$ 247,180$ | $\$ 1,335,392$ | $92.7 \%$ |

Table 9.7
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual <br> Value | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 497 | $\$ 147,675$ | $\$ 150,418$ | $\$ 126,012$ | $\$ 24,407$ |
| Far: | 1,153 | $\$ 341,495$ | $\$ 356,386$ | $\$ 299,944$ | $\$ 126,443$ |
| Total: | 1,650 | $\$ 489,170$ | $\$ 506,805$ | $\$ 355,955$ | $\$ 150,849$ |

Table 9.8
Premiums Collected and Account Values
Original

Contracts \begin{tabular}{l}
Premiums <br>
Collected

$\quad$

Compound <br>
Gain

$\quad$

Unrealized <br>
Gain

 Account 

Value <br>
\end{tabular}

| Near: | 5,516 | $\$ 804,306$ | $\$ 722,905$ | $\$ 24,407$ | $\$ 747,312$ | $92.9 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | $\$ 1,125,019$ | $\$, 1975,816$ | $\$ 126,443$ | $\$ 1,102,259$ | $98.0 \%$ |
| Total: | 11,520 | $\$ 1,929,325$ | $\$ 1,698,721$ | $\$ 150,849$ | $\$ 1,849,570$ | $95.9 \%$ |

## RUN NUMBER 11

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 1 Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y
ITM Far-Term LEAPS Are Rolled Over: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.6

Minimum Standard \& Poor's Rating: B+

No. of Stocks Meeting Either Criterion: 115

Table 9.9
LEAP OTM and Rollout Rates

|  | LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM Rate | LEAPS <br> Rolled | Rollout <br> Rate | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 13,109 | 12,017 | 11,024 | $91.7 \%$ | 993 | $8.3 \%$ | 1,092 |
| Far: | 13,965 | 11,400 | 10,621 | $93.2 \%$ | 1,779 | $6.8 \%$ | 2,565 |
| Total: | 27,074 | 23,417 | 21,645 | $92.4 \%$ | 1,772 | $7.6 \%$ | 3,657 |

Table 9.10
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Expired |  |  |  |  |  |


| Near: | 12,017 | $\$ 870,704$ | $\$ 929,123$ | $\$ 340,533$ | $\$ 588,590$ | $67.6 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 11,400 | $\$ 1,195,471$ | $\$ 1,347,097$ | $\$ 345,880$ | $\$ 1,001,217$ | $83.8 \%$ |
| Total: | 23,417 | $\$ 2,066,174$ | $\$ 2,276,221$ | $\$ 686,414$ | $\$ 1,589,807$ | $76.9 \%$ |

Table 9.11
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 1,092 | $\$ 247,335$ | $\$ 251,999$ | $\$ 210,567$ | $\$ 41,432$ |
| Far: | 2,565 | $\$ 619,244$ | $\$ 645,502$ | $\$ 459,968$ | $\$ 185,535$ |
| Total: | 3,657 | $\$ 866,579$ | $\$ 897,502$ | $\$ 670,535$ | $\$ 226,967$ |

Table 9.12
Premiums Collected and Account Values

| Original | Premiums | Compound | Unrealized | Account <br> Contracts | Collected |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Gain | Gain | Value |  |  |  |


| Near: | 12,116 | $\$ 1,118,039$ | $\$ 763,604$ | $\$ 41,432$ | $\$ 805,036$ | $72.0 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | $\$ 1,814,714$ | $\$ 1,293,789$ | $\$ 185,535$ | $\$ 1,479,323$ | $81.5 \%$ |
| Total: | 25,302 | $\$ 2,932,753$ | $\$ 2,057,392$ | $\$ 226,967$ | $\$ 2,284,359$ | $77.9 \%$ |

## RUN NUMBER 12

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Put Is below ATM Strike 1 Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y
ITM Far-Term LEAPS Are Rolled Over: Y

Premium Reinvestment Rate: $6.0 \%$

Minimum First Call Rating: 1.2

Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 9.13
LEAP OTM and Rollout Rates

| LEAPS | LEAPS | Expired | OTM | LEAPS | Rollout | LEAPS |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Written | Expired | OTM |  | Rolled | Rate | Active |


| Near: | 5,782 | 5,325 | 5,059 | $95.0 \%$ | 266 | $5.0 \%$ | 457 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,228 | 15,139 | 4,915 | 95.6 | 224 | 4.4 | 1,089 |
| Total: | 12,010 | 10,464 | 9,974 | $95.3 \%$ | 490 | $4.7 \%$ | 1,546 |

Table 9.14
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums | Forward | ITM | Realized | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Expired | Collected | Value | Exposure | Gain | Rate |


| Near: | 5,325 | $\$ 264,349$ | $\$ 282,199$ | $\$ 49,438$ | $\$ 232,761$ | $88.1 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 15,139 | $\$ 385,272$ | $\$ 434,226$ | $\$ 42,199$ | $\$ 392,027$ | 101.8 |
| Total: | 10,464 | $\$ 649,621$ | $\$ 716,426$ | $\$ 91,637$ | $\$ 624,789$ | $96.2 \%$ |

Table 9.15
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 457 | $\$ 77,516$ | $\$ 78,989$ | $\$ 64,648$ | $\$ 14,341$ |
| Far: | 1,089 | $\$ 194,114$ | $\$ 202,127$ | $\$ 129,501$ | $\$ 72,626$ |
| Total: | 1,546 | $\$ 271,630$ | $\$ 281,116$ | $\$ 194,149$ | $\$ 86,967$ |

Table 9.16
Premiums Collected and Account Values

| Original | Premiums | Compound | Unrealized | Account | Value |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Contracts | Collected | Gain | Gain | Value |  |


| Near: | 5,516 | $\$ 341,865$ | $\$ 301,311$ | $\$ 14,341$ | $\$ 315,652$ | $92.3 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | $\$ 579,386$ | $\$ 503,083$ | $\$ 72,626$ | $\$ 575,709$ | $99.4 \%$ |
| Total: | 11,520 | $\$ 921,251$ | $\$ 804,394$ | $\$ 86,967$ | $\$ 891,361$ | $96.8 \%$ |

## RUN NUMBER 13

ATM Strike Price Is the High, Low, or Closing C Stock Price:
No. of Steps LEAP Put Is below ATM Strike 2 Price:
Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y
ITM Far-Term LEAPS Are Rolled Over: Y
Premium Reinvestment Rate: $\quad 6.0 \%$
Minimum First Call Rating: 1.6
Minimum Standard \& Poor's Rating: B+
No. of Stocks Meeting Either Criterion: 115

Table 9.17
LEAP OTM and Rollout Rates

| LEAPS | LEAPS | Expired | OTM Rate | LEAPS | Rollout <br> Rote | LEAPS <br> Written |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Expired | OTM |  | Rolled | Rate | Active |  |


| Near: | 12,678 | 11,616 | 11,054 | $95.2 \%$ | 562 | $4.8 \%$ | 1,062 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,628 | 11,144 | 10,702 | $96.0 \%$ | 1,442 | $4.0 \%$ | 2,484 |
| Total: | 26,306 | 22,760 | 21,756 | $95.6 \%$ | 1,004 | $4.4 \%$ | 3,546 |

Table 9.18
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 11,616 | $\$ 447,303$ | $\$ 477,653$ | $\$ 190,971$ | $\$ 286,682$ | $64.1 \%$ |


| Far: | 11,144 | $\$ 1,689,566$ | $\$ 1,777,415$ | $\$ 199,223$ | $\$ 578,192$ | $83.8 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Total: | 22,760 | $\$ 1,136,869$ | $\$ 1,255,068$ | $\$ 390,194$ | $\$ 864,874$ | $76.1 \%$ |

Table 9.19
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | Active |  | Value | Value | Gain |
| Far: | 1,062 | $\$ 140,761$ | $\$ 143,416$ | $\$ 117,980$ | $\$ 25,436$ |
| Total: | 2,484 | $\$ 376,759$ | $\$ 391,969$ | $\$ 288,840$ | $\$ 103,129$ |
|  | 3,546 | $\$ 517,520$ | $\$ 535,385$ | $\$ 406,820$ | $\$ 128,565$ |

Table 9.20
Premiums Collected and Account Values
Original

Contracts \begin{tabular}{llll}
Premiums <br>
Collected

$\quad$

Compound <br>
Gain

$\quad$

Unrealized <br>
Gain

 

Account <br>
Value

$\quad$

Value <br>
Ratio
\end{tabular}

| Near: | 12,116 | $\$ 588,065$ | $\$ 385,946$ | $\$ 25,436$ | $\$ 411,383$ | $70.0 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | $\$ 1,066,325$ | $\$ 1,767,338$ | $\$ 103,129$ | $\$ 1,870,467$ | $81.6 \%$ |
| Total: | 25,302 | $\$ 1,654,389$ | $\$ 1,153,285$ | $\$ 128,565$ | $\$ 1,281,850$ | $77.5 \%$ |

## RUN NUMBER 14

| ATM Strike Price Is the High, Low, or Closing | C |
| :--- | :--- |
| Stock Price: |  |
| No. of Steps LEAP Put Is below ATM Strike <br> Price: | 2 |
| Minimum No. of Months till Expiration: | 8 |
| ITM Near-Term LEAPS Are Rolled Over: | Y |
| ITM Far-Term LEAPS Are Rolled Over: | Y |
| Premium Reinvestment Rate: | $6.0 \%$ |
| Minimum First Call Rating: | 1.2 |
| Minimum Standard \& Poor's Rating: | A- |
| No. of Stocks Meeting Either Criterion: | 50 |

Table 9.21
LEAP OTM and Rollout Rates

| LEAPS | LEAPS | Expired | OTM | LEAPS | Rollout | LEAPS |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Written | Expired | OTM |  | Rolled | Rate | Active |


| Near: | 5,705 | 5,254 | 5,065 | $96.4 \%$ | 189 | $3.6 \%$ | 451 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,110 | 15,046 | 14,940 | $97.9 \%$ | 106 | $2.1 \%$ | 1,064 |
| Total: | 11,815 | 10,300 | 10,005 | $97.1 \%$ | 295 | $2.9 \%$ | 1,515 |

Table 9.22
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums | Forward | ITM | Realized | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Expired | Collected | Value | Exposure | Gain | Rate |


| Near: | 5,254 | $\$ 123,882$ | $\$ 132,344$ | $\$ 19,707$ | $\$ 112,636$ | $90.9 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 15,046 | $\$ 206,272$ | $\$ 232,609$ | $\$ 12,643$ | $\$ 219,965$ | $106.6 \%$ |
| Total: | 10,300 | $\$ 330,155$ | $\$ 364,952$ | $\$ 32,351$ | $\$ 332,602$ | $100.7 \%$ |

Table 9.23
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual <br> Value | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 451 | $\$ 39,263$ | $\$ 40,008$ | $\$ 32,289$ | $\$ 7,719$ |
| Far: | 1,064 | $\$ 105,885$ | $\$ 109,929$ | $\$ 172,180$ | $\$ 37,749$ |
| Total: | 1,515 | $\$ 145,148$ | $\$ 149,937$ | $\$ 104,469$ | $\$ 45,468$ |

Table 9.24
Premiums Collected and Account Values

| Original | Premiums | Compound <br> Contracts | Unrealized <br> Collected | Account <br> Gain | Gain |
| :--- | :--- | :--- | :--- | :--- | :--- | | Value |
| :---: |


| Near: | 5,516 | $\$ 163,146$ | $\$ 152,879$ | $\$ 7,719$ | $\$ 160,598$ | $98.4 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | $\$ 312,157$ | $\$ 291,985$ | $\$ 37,749$ | $\$ 329,733$ | $105.6 \%$ |
| Total: | 11,520 | $\$ 475,303$ | $\$ 444,863$ | $\$ 45,468$ | $\$ 490,331$ | $103.2 \%$ |

## Summary of Results

To compare the results obtained, I will again tabulate the OTM rate, the retention rate, and the overall ten-year value ratio for all runs done so far.

Table 9.25
Figure of Merit Comparisons


As you can readily see from Table 9.25 , adopting a rollover strategy to mitigate potential financial exposure can substantially improve both retention rates and long-term account values.

## At-the-Money Results.

For the $\mathrm{B}+$ minimum universe of 115 stocks, the retention rate progressively increases from 66.2 percent without relievers in Run No. 3 to 78.5 percent with relievers in Run No. 9 , with a corresponding increase in account ratio from 69.7 percent to 80.3 percent. For the A- minimum universe of 50 stocks, the retention rate progressively increases from 79.9 percent without relievers in Run No. 4 to 92.7 percent with relievers in Run No. 10, with a corresponding increase in account ratio from 84.9 percent to 95.9 percent.

## One-Step Out-of-the-Money Results.

For the $\mathrm{B}+$ minimum universe of 115 stocks the retention rate progressively increases from
70.4 percent without rollovers in Run No. 5 to 76.9 percent with roll-overs in Run No. 11, with a corresponding increase in account ratio from 72.6 percent to 77.9 percent. For the A- minimum universe of 50 stocks, the retention rate progressively increases from 90 percent without rollovers in Run No. 6 to 96.2 percent with rollovers in Run No. 12, with a corresponding increase in account ratio from 91.6 percent to 96.8 percent.

## Two-Step Out-of-the-Money Results.

For the $\mathrm{B}+$ minimum universe of 115 stocks, the retention rate progressively increases from 71.1 percent without rollovers in Run No. 7 to 76.1 percent with roll-overs in Run No. 13, with a corresponding increase in account ratio from 73.6 percent to 77.5 percent. For the A- minimum universe of 50 stocks, the retention rate progressively increases from 95.7 percent without rollovers in Run No. 8 to 100.7 percent with rollovers in Run No. 14, with a corresponding increase in account ratio from 98.3 percent to 103.2 percent.

## 10-

## Buy 'Em Out

## Introduction

What I've hopefully established by now is that selling LEAP puts can be controlled for risk, thus reducing financial exposure to levels well within acceptable limits. So far, the only thing we've done with the premiums generated has been to invest them in money market funds and watch them grow at 6 percent a year. But as the title of this book suggests, I have in mind a better use of the premiums received, which is to use them to acquire additional shares of stock in my favorite companies.

Your list of favorite companies is certainly not going to coincide with my list; in fact, it is safe to say that no two people reading this book will have the same set of pet stocks. In view of this, what I propose to do is to take the premiums generated and use them to cover the costs of any high-quality stocks from among the list of companies in Table 6.1 that were assigned because the LEAP puts wound up in the money by the expiration date.

## Procedure

To be conservative, the premiums generated from the sale of LEAP puts are placed into a money market account until the puts expire out of the money and worthless. This approach has the twofold advantage of terminating any financial obligation associated with the expiring LEAP
put and of eliminating the maintenance margin requirement (as described in Chapter 4). As the premiums build up in this manner, you can purchase stock and add it to your equity portfolio.

You can also use the accumulated premiums to purchase stock that was assigned to you because of option positions that expired in the money. The procedure detailed in this chapter consists of accepting the exercise and assignment of any stocks whose far-term LEAP puts expired in the money but rolling out any near-term LEAP puts that did so. The reason the far-term in-the-money LEAP puts are accepted for assignment and the near-term LEAP puts are rolled out (rather than the reverse) is to delay stock purchase long enough for the premiums received to build up ahead of the monetary requirements for stock acquisition.

In practice, you would be free to accept exercise and assignment of any stock you believed was worthwhile, assuming you had the dollars to acquire it. As we want to concentrate on the effects of stock acquisition, the computer runs in this chapter will be restricted to the universe of 115 stocks rated $\mathrm{B}+$ or better and the universe of 50 stocks rated A - or better. For each universe, three runs will be made, ranging from the conservative sale of at-the-money LEAP puts to the very conservative sale of LEAP puts two steps out of the money.

In each instance, any near-term LEAPS that appear to be winding up in the money will be rolled in much the same manner as in the previous chapter. For any far-term LEAPS that expire in the money, the procedure followed is to purchase the assigned stock.

## At-the-Money LEAPS on the B+ Minimum Universe

Run No. 15 is the analog of Run No. 3 but where the in-the-money near-term LEAPS are rolled out and the in-the-money far-term LEAPS are accepted for assignment from among the total universe of 115 stocks rated $\mathrm{B}+$ or better and for which the original strike price was at the money.

All line items for the near-term LEAPS are identical to those in Run No. 9 (which is Run No. 3 with rollovers). On the other hand, the 1,479 far-term LEAPS in Table 10.1 that expired in the money are all accepted for assignment. The ITM exposure for the far-term LEAPS in

Table 10.2 is $\$ 3,899,612$ and represents the funding required to finance the acquisition of the 147,900 shares so assigned.

The realized gain in Table 10.2 is again the difference between the forward value and ITM exposure. It is a negative $\$ 1,470,879$ for the far-term LEAPS, because the cost basis of $\$ 3.9$ million is greater than the $\$ 2.4$ million available from the far-term premiums alone. However, when the near-term LEAP premiums are used to pay for the acquired stock, the additional capital needed from external sources over the ten-year period is just a little over $\$ 168,000$, an almost breakeven situation. Table 10.3 shows the unrealized gain for the 3,583 active but unexpired LEAPS.

Table 10.4 shows the premiums collected and the account values resulting at the end of the ten-year study period. The account value for the far-term LEAPS includes the close to $\$ 7.9$ million in the new column marked stock value. The overall investment account on March 31, 1997, is just shy of $\$ 8$ million. This sum is close to 150 percent of the $\$ 5,345,392$ in total premiums collected over the ten-year period and is substantially higher than the 69.7 percent account ratio (without roll-overs) in Run No. 3 or the 80.3 percent account ratio (with rollovers) in Run No. 9. Table 10.5 details the portfolio of 147,900 shares of stock acquired in 93 different companies as a result of exercise and assignment. The names these companies were known by are those of March 31, 1997, and do not reflect any mergers, acquisitions or spin-offs that have occurred since then.

## At-the-Money LEAPS on the A- Minimum Universe

Run No. 16 is the analog of Run No. 4 but where the in-the-money near-term LEAPS are rolled out and the in-the-money far-term LEAPS are accepted for assignment from among the total universe of 50 stocks rated A- or better and for which the original strike price was at the money.

The ITM exposure of $\$ 1,241,101$ in Table 10.7 represents the funding required to finance the acquisition of the 51,800 shares of stock resulting from the 518 far-term option contracts that expired in the money and were assigned. The realized gain in Table 10.7 is $\$ 565,464$ for the near-term LEAPS and a negative $\$ 358,568$ for the far-term LEAPS. The combined realized gain is this time a relatively large pos-
itive amount, signifying that the total premiums received were more than enough to cover the ITM exposure of the near-term LEAPS as well as pay for the stock acquired through assignment of the far-term LEAPS that expired in the money. As a result, the account value of $\$ 2,941,554$ at the end of the ten-year period includes stock valued at close to $\$ 2.5$ million. The account value is 154.2 percent of the premiums collected over the ten-year period and is substantially higher than the 95.9 percent account ratio (with rollovers) seen in Run No. 10. Table 10.10 details the portfolio of 51,800 shares of stock acquired in 40 different companies as a result of exercise and assignment.

## One-Step OTM LEAPS on the B+ Minimum Universe

Run No. 17 is the analog of Run No. 5 but where the in-the-money near-term LEAPS are rolled out and the in-the-money far-term LEAPS are accepted for assignment from among the total universe of 115 stocks rated $\mathrm{B}+$ or better and for which the original strike price was one step out of the money. The ITM exposure of $\$ 1,759,423$ in Table 10.12 represents the funding required to finance the acquisition of the 73,800 shares of stock resulting from the 738 far-term option contracts that expired in the money and were assigned. The realized gain in Table 10.12 is $\$ 588,590$ for the near-term LEAPS and a negative $\$ 412,326$ for the far-term LEAPS. The combined realized gain of $\$ 176,264$ is a positive amount, signifying that the total premiums received are enough to cover the ITM exposure of the near-term LEAPS as well as pay for the stock acquired through assignment of the far-term LEAPS that expired in the money. As a result, the account value of $\$ 4,334,794$ at the end of the ten-year period includes stock valued at close to $\$ 3.9$ million. The account value is 149.1 percent of the premiums collected over the ten-year period and is substantially higher than the 77.9 percent account ratio (with rollovers) seen in Run No. 11. Table 10.15 details the portfolio of 73,800 shares of stock acquired in 66 different companies as a result of exercise and assignment.

## One-Step OTM LEAPS on the A- Minimum Universe

Run No. 18 is the analog of Run No. 6 but where the in-the-money near-term LEAPS are rolled out and the in-the-money far-term LEAPS
are accepted for assignment, from among the total universe of 50 stocks rated A - or better and for which the original strike price was one step out of the money.

The ITM exposure of $\$ 511,671$ in Table 10.17 represents the funding required to finance the acquisition of the 22,400 shares of stock resulting from the 224 far-term option contracts that expired in the money and were assigned. The realized gain in Table 10.17 is $\$ 232,761$ for the near-term LEAPS and a negative $\$ 77,444$ for the far-term LEAPS. The combined realized gain is again positive, signifying that the total premiums received were enough to cover the ITM exposure of the near-term LEAPS as well as pay for the stock acquired through assignment of the far-term LEAPS that expired in the money. As a result, the account value of $\$ 1,326,217$ at the end of the ten-year period includes stock valued at just over $\$ 1$ million. The account value is 144.7 percent of the premiums collected over the ten-year period and is again substantially higher than the 96.8 percent account ratio (with rollovers) seen in Run No. 12. Table 10.20 details the portfolio of 22,400 shares of stock acquired in 24 different companies as a result of exercise and assignment.

## Two-Step OTM LEAPS on the B+ Minimum Universe

Run No. 19 is the analog of Run No. 7 but where the in-the-money near-term LEAPS are rolled out and the in-the-money far-term LEAPS are accepted for assignment from among the total universe of 115 stocks rated $\mathrm{B}+$ or better and for which the original strike price was two steps out of the money.

The ITM exposure of $\$ 768,734$ in Table 10.22 represents the funding required to finance the acquisition of the 43,500 shares of stock resulting from the 435 far-term option contracts that expired in the money and were assigned. The realized gain in Table 10.22 is $\$ 286,682$ for the near-term LEAPS and a positive $\$ 8,680$ for the far-term LEAPS. In this situation, the premiums received from sale of the far-term LEAPS alone were enough to cover the cost of the stock acquired through assignment of the far-term LEAPS that expired in the money. As a result, the account value of $\$ 2,522,336$ at the end of the ten-year period includes stock valued at close to $\$ 2$ million. The account value is 153.6 percent of the premiums collected over the ten-
year period and is substantially higher than the 77.5 percent account ratio (with rollovers) seen in Run No. 13. Table 10.25 details the portfolio of 43,500 shares of stock acquired in 49 different companies as a result of exercise and assignment.

## Two-Step OTM LEAPS on the A- Minimum Universe

Run No. 20 is the analog of Run No. 8 but where the in-the-money near-term LEAPS are rolled out and the in-the-money far-term LEAPS are accepted for assignment from among the total universe of 50 stocks rated A- or better and for which the original strike price was two steps out of the money.

The ITM exposure of $\$ 190,502$ in Table 10.27 represents the funding required to finance the acquisition of the 10,600 shares of stock resulting from the 106 far-term option contracts that expired in the money and were assigned. The realized gain in Table 10.27 is $\$ 112,636$ for the near-term LEAPS and a positive $\$ 42,107$ for the far-term LEAPS. In this situation, the premiums received from sale of the far-term LEAPS was more than enough to cover the cost of the stock acquired through assignment of the far-term LEAPS that expired in the money. As a result, the account value of $\$ 730,440$ at the end of the ten-year period includes stock valued at $\$ 462,413$. The account value is 154.1 percent of the premiums collected over the ten-year period and is substantially higher than the 103.2 percent account ratio (with roll-overs) seen in Run No. 14. Table 10.30 details the portfolio of 10,600 shares of stock acquired in 16 different companies as a result of exercise and assignment.

## RUN NUMBER 15

ATM Strike Price is the High, Low, or Closing C Stock Price:

No. of Steps Near-Term LEAP Put Is below ATM 0 Strike Price:

No. of Steps Far-Term LEAP Put Is below ATM 0 Strike Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y

Stocks of ITM Far-Term LEAPS Are Purchased: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.6
Minimum Standard \& Poor's Rating: B+

No. of Stocks Meeting Either Criterion: 11

Table 10.1
LEAP OTM and ITM Rates

|  | LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM | Expired <br> ITM | ITM <br> Rate | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 14,496 | 13,321 | 10,941 | $82.1 \%$ | 2,380 | $17.9 \%$ | 1,175 |
| Far: | 13,186 | 10,778 | 19,299 | $86.3 \%$ | 1,479 | $13.7 \%$ | 2,408 |
| Total: | 27,682 | 24,099 | 20,240 | $84.0 \%$ | 3,859 | $16.0 \%$ | 3,583 |

Table 10.2
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 13,321 | $\$ 1,835,915$ | $\$ 1,957,072$ | $\$ 654,353$ | $\$ 1,302,719$ | $71.0 \%$ |
| Far: | 10,778 | $\$ 2,156,467$ | $\$ 2,428,733$ | $\$ 3,899,612$ | $-\$ 1,470,879$ | $-68.2 \%$ |
| Total: | 24,099 | $\$ 3,992,382$ | $\$ 4,385,805$ | $\$ 4,553,966$ | $-\$ 168,161$ | $-4.2 \%$ |

Table 10.3
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,175 | $\$ 427,669$ | $\$ 435,578$ | $\$ 376,392$ | $\$ 59,186$ |
| Far: | 2,408 | $\$ 3,925,341$ | $\$ 1,966,239$ | $\$ 1,689,007$ | $\$ 277,233$ |
| Total: | 3,583 | $\$ 1,353,010$ | $\$ 1,401,817$ | $\$ 1,065,399$ | $\$ 336,419$ |

Table 10.4
Premiums Collected and Account Values

|  | Original <br> Contracts | Premiums <br> Collected | Compound <br> Gain | Unrealized <br> Gain | Stock | Account <br> Value | Value <br> Ratio |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 12,116 | $\$ 2,263,585$ | $\$ 1,661,559$ | $\$ 59,186$ | $\$ 0$ | $\$ 1,720,745$ | $76.0 \%$ |
| Far: | 13,186 | $\$ 3,081,807$ | - | $\$ 277,233$ | $\$ 7,857,106$ | $\$ 6,275,718$ | $203.6 \%$ |
|  |  |  | $\$ 1,858,621$ |  |  |  |  |
| Total: | 25,302 | $\$ 5,345,392$ | $-\$ 197,062$ | $\$ 336,419$ | $\$ 7,857,106$ | $\$ 7,996,463$ | $149.6 \%$ |

Table 10.5
List of Stocks Purchased

| Name of | Trading Symbol | No. of <br> Company |  | Cost <br> Basis |
| :--- | :--- | :--- | :--- | :--- |


| Abbott Labs | ABT | 1,200 | \$ 25,050 | \$ 67,350 |
| :---: | :---: | :---: | :---: | :---: |
| Adobe Systems | ADBE | 1,000 | 29,238 | 40,125 |
| Allied Signal | ALD | 2,200 | 34,625 | 156,750 |
| American Express | AXP | 3,500 | 73,565 | 209,563 |
| American Home | AHP | 900 | 28,575 | 54,000 |
| Amoco | AN | 1,400 | 64,925 | 121,275 |
| Anheuser-Busch | BUD | 1,200 | 29,400 | 50,550 |
| ASA Holdings | ASAI | 2,300 | 42,088 | 47,725 |
| AT\&T | T | 2,100 | 66,937 | 72,975 |
| Atlantic Richfield | ARC | 3,500 | 383,275 | 472,500 |
| Avon Products | AVP | 1,300 | 20,470 | 68,250 |
| BankAmerica | BAC | 800 | 34,500 | 80,700 |
| Barrick Gold | ABX | 300 | 5,963 | 7,125 |
| Bell Atlantic | BEL | 700 | 34,725 | 42,700 |
| BellSouth | BLS | 1,200 | 29,549 | 50,550 |
| Boeing | BA | 2,000 | 77,663 | 197,250 |
| Boston Scientific | BSX | 500 | 8,925 | 30,875 |
| Bristol-Myers Squibb | BUY | 2,400 | 69,200 | 141,600 |


| Burlington Northern | BNI | 400 | 19,000 | 29,600 |
| :---: | :---: | :---: | :---: | :---: |
| Cabletron Systems | CS | 200 | 3,800 | 5,900 |
| Campbell Soup | CPB | 200 | 3,875 | 9,275 |
| Chase Manhattan | CMB | 3,100 | 75,150 | 290,238 |
| Chubb | CB | 300 | 9,615 | 16,163 |
| Compaq | CPQ | 1,800 | 22,167 | 137,925 |
| Conseco | CNC | 1,300 | 9,077 | 46,313 |
| Corning | GLW | 1,600 | 50,700 | 71,000 |
| Cracker Barrel | CBRL | 2,200 | 45,550 | 57,475 |
| CUC International | CU | 1,700 | 3,097 | 38,250 |
| Dayton Hudson | DH | 1,700 | 35,986 | 70,975 |
| Dun \& Bradstreet | DNB | 5,300 | 227,925 | 134,488 |
| DuPont (E.I.) de Nemours | DD | 600 | 21,125 | 63,600 |
| Equifax | EFX | 300 | 2,259 | 8,175 |
| Exxon | XON | 400 | 25,000 | 43,100 |
| Fannie Mae | FNM | 100 | 1,788 | 3,613 |
| Gap | GPS | 1,500 | 17,757 | 50,250 |
| General Electric | GE | 600 | 14,519 | 59,550 |
| General Mills | GIS | 2,400 | 115,073 | 149,100 |
| GTE | GTE | 600 | 20,088 | 27,975 |
| HealthSouth | HRC | 900 | 2,936 | 17,213 |


| Heinz (H.J.) | HNZ | 1,000 | 23,182 | 39,500 |
| :--- | :--- | :---: | :---: | :---: |
| Hewlett-Packard | HWP | 2,500 | 26,835 | 133,125 |
| Hilton Hotels | HLT | 2,300 | 22,700 | 55,775 |
| Home Depot | HD | 100 | 4,675 | 5,350 |
| Household | HI | 2,000 | 41,750 | 172,250 |
| International |  | 100 |  | 13,913 |
| Intel | INTC | 2,600 | 34,325 | 41,925 |
| International Game | IGT | 1,300 | 27,793 | 68,738 |

(Table continued on next page)

Table 10.5
List of Stocks Purchased (Continued)

| Name of Company | Trading Symbol | No. of Shares | Cost <br> Basis | Stock <br> Value |
| :---: | :---: | :---: | :---: | :---: |
| KMart | KM | 6,400 | \$ 86,172 | \$ 77,600 |
| Kroger | KR | 400 | 27,000 | 20,400 |
| Limited | LTD | 5,400 | 90,811 | 99,225 |
| Lowe's | LOW | 900 | 24,126 | 33,638 |
| Magna <br> International | MGA | 3,300 | 32,861 | 163,763 |
| Merck | MRK | 1,500 | 55,875 | 126,375 |
| Merrill Lynch | MER | 2,300 | 31,775 | 197,513 |
| Minn. Mining | MUM | 400 | 17,778 | 33,800 |
| Mobil | MOB | 400 | 23,925 | 52,250 |
| Monsanto | MTC | 200 | 2,131 | 7,650 |
| Morgan (J.P.) | JPM | 1,500 | 70,500 | 147,375 |
| Motorola | MOT | 800 | 11,067 | 48,300 |
| NationsBank | NB | 1,700 | 33,256 | 94,350 |
| NEXTEL | NXTL | 2,900 | 35,738 | 38,788 |
| NIKE | NKE | 900 | 12,825 | 55,688 |
| NYNEX | NYN | 2,100 | 80,939 | 95,813 |
| Office Depot | ODP | 2,400 | 44,457 | 48,900 |
| Oracle | ORCL | 1,500 | 4,060 | 57,844 |


| PepsiCo | PEP | 400 | 7,379 | 13,050 |
| :---: | :---: | :---: | :---: | :---: |
| Pfizer | PFE | 1,500 | 34,686 | 126,188 |
| Philip Morris | MO | 2,100 | 126,075 | 240,188 |
| Pitney Bowes | PBI | 1,600 | 43,914 | 94,000 |
| Polaroid | PRD | 2,800 | 76,875 | 111,300 |
| PPG Industries | PPG | 600 | 11,925 | 32,400 |
| Quaker Oats | OAT | 900 | 30,156 | 32,850 |
| Reebok International | RBK | 1,700 | 33,413 | 76,288 |
| Salomon | SB | 3,000 | 89,613 | 149,625 |
| Sara Lee | SLE | 1,100 | 25,613 | 44,550 |
| Schlumberger | SLB | 3,200 | 171,800 | 343,200 |
| Schwab | SCH | 100 | 200 | 3,188 |
| Southwest Air | LUV | 2,100 | 49,138 | 46,463 |
| Sprint | FON | 2,200 | 45,621 | 99,825 |
| Sun Microsystems | SUNW | 700 | 4,263 | 20,213 |
| SunAmerica | SAI | 400 | 927 | 15,050 |
| TCI | TCOMA | 2,400 | 33,038 | 28,800 |
| Toys "R" Us | TOY | 3,000 | 76,500 | 84,000 |
| Travelers | TRV | 200 | 1,308 | 9,575 |
| United HealthCare | UNH | 800 | 15,266 | 38,100 |
| Unocal | UCL | 1,700 | 39,088 | 64,813 |


| US Surgical | USS | 2,500 | 68,525 | 76,250 |
| :--- | :--- | :---: | :---: | :---: |
| US WEST Comm. | USW | 600 | 13,893 | 20,325 |
| Warner-Lambert | WLA | 1,000 | 32,790 | 86,500 |
| Wells Fargo | WFC | 2,100 | 130,350 | 596,663 |
| Wendy's | WEN | 1,800 | 8,475 | 37,125 |
| International |  | 2,100 | 37,394 | 119,438 |
| Xerox | XRX | 147,900 | $\$ 3,899,610$ | $\$ 7,857,106$ |

## RUN NUMBER 16

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps Near-Term LEAP Put Is below ATM 0 Strike Price:

No. of Steps Far-Term LEAP Put Is below ATM 0 Strike Price:

Minimum 1No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y

Stocks of ITM Far-Term LEAPS Are Purchased: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.2

Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 10.6
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired | OTM Rate | Expired | ITM |
| :--- | :--- | :--- | :--- | :--- | :--- | | LEAPS |
| :--- |
| Written | | Expired | OTM |
| :--- | :--- |


| Near: | 6,396 | 5,899 | 5,019 | $85.1 \%$ | 880 | $14.9 \%$ | 497 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | 14,953 | 4,435 | $89.5 \%$ | 1,518 | $10.5 \%$ | 1,051 |
| Total: | 12,400 | 10,852 | 9,454 | $87.1 \%$ | 1,398 | $12.9 \%$ | 1,548 |

Table 10.7
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,899 | $\$ 656,632$ | $\$ 700,038$ | $\$ 134,574$ | $\$ 565,464$ | $86.1 \%$ |
| Far: | 14,953 | $\$ 1,783,524$ | $\$ 1,882,534$ | $\$ 1,241,101$ | $-\$ 358,568$ | $-45.8 \%$ |
| Total: | 10,852 | $\$ 1,440,155$ | $\$ 1,582,571$ | $\$ 1,375,675$ | $\$ 206,896$ | $14.4 \%$ |

Table 10.8
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 497 | $\$ 147,675$ | $\$ 150,418$ | $\$ 126,012$ | $\$ 24,407$ |
| Far: | 1,051 | $\$ 319,954$ | $\$ 333,714$ | $\$ 218,707$ | $\$ 115,007$ |
| Total: | 1,548 | $\$ 467,629$ | $\$ 484,132$ | $\$ 344,719$ | $\$ 139,413$ |

Table 10.9
Premiums Collected and Account Values

|  | Original <br> Contracts | Premiums <br> Collected | Compound <br> Gain | Unrealized Stock <br> Gain | Account <br> Value | Value <br> Ratio |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,516 | $\$ 804,306$ | $\$ 722,905$ | 24,407 | $\$ 0$ | $\$ 747,312$ | $92.9 \%$ |
| Far: | 16,004 | $\$ 1,103,477$ | $-\$ 394,965$ | $\$ 115,007$ | $\$ 2,474,200$ | $\$ 2,194,242$ | $198.8 \%$ |
| Total: | 11,520 | $\$ 1,907,784$ | $\$ 327,941$ | $\$ 139,413$ | $\$ 2,474,200$ | $\$ 2,941,554$ | $154.2 \%$ |

Table 10.10
List of Stocks Purchased

| Name of Company | Trading Symbol | No. of Shares | Cost <br> Basis | Stock <br> Value |
| :---: | :---: | :---: | :---: | :---: |
| Abbott Labs | ABT | 1,200 | \$ 25,050 | \$ 67,350 |
| American Home | AHP | 900 | 28,575 | 54,000 |
| Anheuser-Busch | BUD | 1,200 | 29,400 | 50,550 |
| ASA Holdings | ASAI | 2,300 | 42,088 | 7,725 |
| Barrick Gold | ABX | 300 | 5,963 | 7,125 |
| Bell Atlantic | BEL | 700 | 34,725 | 42,700 |
| Bristol-Myers Squibb | BUY | 2,400 | 69,200 | 141,600 |
| Chubb | CB | 300 | 9,615 | 16,163 |
| Conseco | CNC | 1,300 | 9,077 | 46,313 |
| Cracker Barrel | CBRL | 2,200 | 45,550 | 57,475 |
| Dayton Hudson | DH | 1,700 | 35,986 | 70,975 |
| Equifax | EFX | 300 | 2,259 | 8,175 |
| Exxon | XON | 400 | 25,000 | 43,100 |
| Fannie Mae | FNM | 100 | 1,788 | 3,613 |
| Gap | GPS | 1,500 | 17,757 | 50,250 |
| General Electric | GE | 600 | 14,519 | 59,550 |
| General Mills | GIS | 2,400 | 115,073 | 149,100 |
| Heinz (H.J.) | HNZ | 1,000 | 23,182 | 39,500 |


| Hewlett-Packard | HWP | 2,500 | 26,835 | 133,125 |
| :---: | :---: | :---: | :---: | :---: |
| Home Depot | HD | 100 | 4,675 | 5,350 |
| Johnson \& Johnson | JNJ | 1,300 | 27,793 | 68,738 |
| Limited | LTD | 5,400 | 90,811 | 99,225 |
| Lowe's | LOW | 900 | 24,126 | 33,638 |
| Merck | MRK | 1,500 | 55,875 | 126,375 |
| Minn. Mining | MMM | 400 | 17,778 | 33,800 |
| Motorola | MOT | 800 | 11,067 | 48,300 |
| NationsBank | NB | 1,700 | 33,256 | 94,350 |
| NIKE | NKE | 900 | 12,825 | 55,688 |
| Pepsi Co | PEP | 400 | 7,379 | 13,050 |
| Pfizer | PFE | 1,500 | 34,686 | 126,188 |
| Phi lip Morris | MO | 2,100 | 126,075 | 240,188 |
| Pitney Bowes | PBI | 1,600 | 43,914 | 94,000 |
| PPG Industries | PPG | 600 | 11,925 | 32,400 |
| Sara Lee | SLE | 1,100 | 25,613 | 44,550 |
| Southwest Air | LUV | 2,100 | 49,138 | 46,463 |
| SunAmerica | SAI | 400 | 927 | 15,050 |
| Travelers | TRV | 200 | 1,308 | 9,575 |
| Wal-Mart | WMT | 2,700 | 59,025 | 75,263 |
| Warner-Lambert | WLA | 1,000 | 32,790 | 86,500 |
| Wendy's | WEN | 1,800 | 8,475 | 37,125 |

International

Totals
51,800
$\$ 1,241,100$
\$2,474,200

## RUN NUMBER 17

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps Near-Term LEAP Put Is below ATM 1 Strike Price:

No. of Steps Far-Term LEAP Put is below ATM 1 Strike Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y

Stocks of ITM Far-Term LEAPS Are Purchased: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.6
Minimum Standard \& Poor's Rating: B+
No. of Stocks Meeting Either Criterion: 115

Table 10.11
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired | OTM | Expired | ITM | LEAPS |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Written | Expired | OTM |  | ITM |  | Active |


| Near: | 13,109 | 12,017 | 11,024 | $91.7 \%$ | 993 | $8.3 \%$ | 1,092 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | 10,778 | 10,040 | $93.2 \%$ | 1,738 | $6.8 \%$ | 2,408 |
| Total: | 26,295 | 22,795 | 21,064 | $92.4 \%$ | 1,731 | $7.6 \%$ | 3,500 |

Table 10.12
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 12,017 | $\$ 870,704$ | $\$ 929,123$ | $\$ 340,533$ | $\$ 588,590$ | $67.6 \%$ |
| Far: | 10,778 | $\$ 1,195,471$ | $\$ 1,347,097$ | $\$ 1,759,423$ | $\$ 412,326$ | $-34.5 \%$ |
| Total: | 22,795 | $\$ 2,066,174$ | $\$ 2,276,221$ | $\$ 2,099,956$ | $\$ 176,26$ | $48.5 \%$ |

Table 10.13
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 1,092 | $\$ 247,335$ | $\$ 251,999$ | $\$ 210,567$ | $\$ 41,432$ |
| Far: | 2,408 | $\$ 593,555$ | $\$ 618,822$ | $\$ 444,505$ | $\$ 174,317$ |
| Total: | 3,500 | $\$ 840,890$ | $\$ 870,821$ | $\$ 655,072$ | $\$ 215,750$ |

Table 10.14
Premiums Collected and Account Values

| Original | Premiums | Compound | Unrealized | Stock | Account | Value |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Contracts | Collected | Gain | Gain | Value | Value | Ratio |

Near: $12,116 \quad \$ 1,118,039 \quad \$ 763,604 \quad \$ 41,432 \quad \$ 0 \quad \$ 805,036 \quad 72.0 \%$
Far: $\quad 13,186 \quad \$ 1,789,026 \quad-\$ 502,215 \quad \$ 174,317 \quad \$ 3,857,656 \quad \$ 3,529,758 \quad 197.3 \%$

Total: $\quad 25,302 \quad \$ 2,907,065 \quad \$ 261,388 \quad \$ 215,750 \quad \$ 3,857,656 \quad \$ 4,334,794 \quad 149.1 \%$

Table 10.15
List of Stocks Purchased

| Name of Company | Trading <br> Symbol | No. of Shares | Cost <br> Basis | Stock <br> Value |
| :---: | :---: | :---: | :---: | :---: |
| Abbott Labs | ABT | 400 | \$ 4,900 | \$ 22,450 |
| Adobe Systems | ADBE | 400 | 15,150 | 16,050 |
| Allied Signal | ALD | 1,100 | 18,425 | 78,375 |
| Altera | ALTR | 500 | 1,955 | 21,500 |
| American Express | AXP | 1,200 | 21,860 | 71,850 |
| American Home | AHP | 100 | 3,175 | 6,000 |
| Anheuser-Busch | BUD | 100 | 2,450 | 4,213 |
| Applied Materials | AMAT | 700 | 2,439 | 32,463 |
| ASA Holdings | ASAI | 2,600 | 37,946 | 53,950 |
| AT\&T | T | 200 | 7,481 | 6,950 |
| Atlantic Richfield | ARC | 2,200 | 240,650 | 297,000 |
| Avon Products | AVP | 500 | 5,531 | 26,250 |
| BankAmerica | BAC | 300 | 12,938 | 30,263 |
| Barrick Gold | ABX | 200 | 3,975 | 4,750 |
| Bell Atlantic | BEL | 100 | 4,613 | 6,100 |
| Boeing | BA | 1,100 | 40,375 | 108,488 |
| Boston Scientific | BSX | 100 | 1,850 | 6,175 |
| Bristol-Myers Squibb | BUY | 1,600 | 46,769 | 94,400 |


| Burlington Northern | BNI | 100 | 4,750 | 7,400 |
| :---: | :---: | :---: | :---: | :---: |
| Chase Manhattan | CUB | 2,400 | 51,375 | 224,700 |
| Compaq | CPQ | 1,500 | 17,057 | 114,938 |
| Conseco | CNC | 900 | 3,967 | 32,063 |
| Cracker Barrel | CBRL | 1,500 | 30,150 | 39,188 |
| CUC International | CU | 1,700 | 3,097 | 38,250 |
| Dun \& Bradstreet | DNB | 2,200 | 74,525 | 55,825 |
| Gap | GPS | 200 | 925 | 6,700 |
| General Mills | GIS | 1,300 | 61,762 | 80,763 |
| HealthSouth | HRC | 700 | 1,523 | 13,388 |
| Hewlett-Packard | HWP | 1,500 | 15,449 | 79,875 |
| Hilton Hotels | HLT | 1,600 | 15,850 | 38,800 |
| Household International | HI | 1,200 | 22,650 | 103,350 |
| International Game | IGT | 2,500 | 32,538 | 40,313 |
| KMart | KM | 4,000 | 50,500 | 48,500 |
| Kroger | KR | 100 | 1,750 | 5,100 |
| Limited | LTD | 4,100 | 68,704 | 75,338 |
| Magna International | MGA | 2,500 | 17,636 | 124,063 |
| Merck | MRK | 1,000 | 36,875 | 84,250 |
| Merrill Lynch | MER | 800 | 10,570 | 68,700 |


| Morgan (J.P.) | JPM | 600 | 21,750 | 58,950 |
| :--- | :--- | :---: | :---: | :---: |
| NationsBank | NB | 400 | 5,625 | 22,200 |
| NEXTEL | NXTL | 2,400 | 30,350 | 32,100 |
| NIKE | NKE | 300 | 3,750 | 18,563 |
| NY N EX | NYN | 400 | 15,606 | 18,250 |
| Office Depot | ODP | 600 | 9,872 | 12,225 |
| Oracle | ORC | 1,500 | 4,060 | 57,844 |
| Pfizer | PFE | 500 | 8,992 | 42,063 |
| Philip Morris | MO | 1,800 | 108,050 | 205,875 |

(Table continued on next page)

Table 10.15
List of Stocks Purchased (Continued)

| Name of Company | Trading <br> Symbol | No. of Shares | Cost <br> Basis | Stock <br> Value |
| :---: | :---: | :---: | :---: | :---: |
| Pitney Bowes | PBI | 600 | \$ 18,525 | \$ 35,250 |
| Polaroid | PRD | 2,500 | 67,800 | 99,375 |
| PPG Industries | PPG | 400 | 7,950 | 21,600 |
| Reebok International | RBK | 700 | 9,050 | 31,413 |
| Salomon | SB | 1,700 | 56,675 | 84,788 |
| Schlumberger | SLB | 1,500 | 81,275 | 160,875 |
| Schwab | SCH | 100 | 200 | 3,188 |
| Southwest Air | LUV | 1,000 | 18,468 | 22,125 |
| Sprint | FON | 1,200 | 23,700 | 54,450 |
| SunAmerica | SAI | 400 | 927 | 15,050 |
| TCI | TCOMA | 400 | 5,236 | 4,800 |
| Toys "R" Us | TOY | 2,800 | 71,500 | 78,400 |
| United HealthCare | UNH | 500 | 641 | 23,813 |
| Unocal | UCL | 200 | 4,350 | 7,625 |
| US Surgical | USS | 2,400 | 66,200 | 73,200 |
| Wal-Mart | WMT | 600 | 13,725 | 16,725 |
| Wells Fargo | WFC | 1,500 | 93,450 | 426,188 |
| Wendy's | WEN | 800 | 4,000 | 16,500 |

International

| Xerox | XRX | 800 | 13,563 | 45,500 |
| :--- | ---: | ---: | ---: | ---: |
| Totals |  | 73,800 | $\$ 1,759,424$ | $\$ 3,857,656$ |

## RUN NUMBER 18

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps Near-Term LEAP Put Is below ATM 1 Strike Price:

No. of Steps Far-Term LEAP Put Is below ATM 1 Strike Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y

Stocks of ITM Far-Term LEAPS Are Purchased: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.2

Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 10.16
LEAP OTM and ITM Rates

|  | LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM | Expired <br> ITM | ITM | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,782 | 5,325 | 5,059 | $95.0 \%$ | 266 | $5.0 \%$ | 457 |
| Far: | 16,004 | 14,953 | 4,729 | $95.5 \%$ | 224 | $4.5 \%$ | 1,051 |
| Total: | 11,786 | 10,278 | 9,788 | $95.2 \%$ | 490 | $4.8 \%$ | 1,508 |

Table 10.17
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,325 | $\$ 264,349$ | $\$ 282,199$ | $\$ 49,438$ | $\$ 232,761$ | $88.1 \%$ |
| Far: | 14,953 | $\$ 385,272$ | $\$ 434,226$ | $\$ 511,671$ | $-\$ 177,444$ | $-20.1 \%$ |
| Total: | 10,278 | $\$ 649,621$ | $\$ 716,426$ | $\$ 561,109$ | $\$ 155,317$ | $23.9 \%$ |

Table 10.18
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 457 | $\$ 77,516$ | $\$ 78,989$ | $\$ 64,648$ | $\$ 14,341$ |
| Far: | 1,051 | $\$ 189,212$ | $\$ 196,907$ | $\$ 128,283$ | $\$ 68,623$ |
| Total: | 1,508 | $\$ 266,728$ | $\$ 275,895$ | $\$ 192,931$ | $\$ 82,964$ |

Table 10.19
Premiums Collected and Account Values

| Original <br> Contracts | Premiums <br> Collected | Compound <br> Gain | Unrealized Stock <br> Gain | Account <br> Value | Value |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 5,516 | $\$ 341,865$ | $\$ 301,311$ | $\$ 14,341$ | $\$ 0$ | $\$ 315,652$ | $92.3 \%$ |
| 16,004 | $\$ 574,484$ | $-\$ 164,046$ | $\$ 68,623$ | $\$ 1,005,988$ | $\$ 1,010,565$ | $175.9 \%$ |
| 11,520 | $\$ 916,350$ | $\$ 237,266$ | $\$ 82,964$ | $\$ 1,005,988$ | $\$ 1,326,217$ | $144.7 \%$ |

Table 10.20
List of Stocks Purchased

| Name of Company | Trading <br> Symbol | No. of Shares | Cost <br> Basis | Stock <br> Value |
| :---: | :---: | :---: | :---: | :---: |
| Abbott Labs | ABT | 400 | \$ 4,900 | \$ 22,450 |
| American Home | AHP | 100 | 3,175 | 6,000 |
| Anheuser-Busch | BUD | 100 | 2,450 | 4,213 |
| ASA Holdings | ASAI | 2,600 | 37,946 | 53,950 |
| Barrick Gold | ABX | 200 | 3,975 | 4,750 |
| Bell Atlantic | BEL | 100 | 4,613 | 6,100 |
| Bristol-Myers Squibb | BUY | 1,600 | 46,769 | 94,400 |
| Conseco | CNC | 900 | 3,967 | 32,063 |
| Cracker Barrel | CBRL | 1,500 | 30,150 | 39,188 |
| Gap | GPS | 200 | 925 | 6,700 |
| General Mills | GIS | 1,300 | 61,762 | 80,763 |
| Hewlett-Packard | HWP | 1,500 | 15,449 | 79,875 |
| Limited | LTD | 4,100 | 68,704 | 75,338 |
| Merck | MRK | 1,000 | 36,875 | 84,250 |
| NationsBank | NB | 400 | 5,625 | 22,200 |
| NIKE | NKE | 300 | 3,750 | 18,563 |
| Pfizer | PFE | 500 | 8,992 | 42,063 |
| Philip Morris | MO | 1,800 | 108,050 | 205,875 |


| Pitney Bowes | PBI | 600 | 18,525 | 35,250 |
| :--- | :--- | :---: | :---: | :---: |
| PPG Industries | PPG | 400 | 7,950 | 21,600 |
| Southwest Air | LUV | 1,000 | 18,468 | 22,125 |
| SunAmerica | SAI | 400 | 927 | 15,050 |
| Wal-Mart | WMT | 600 | 13,725 | 16,725 |
| Wendy's | WEN | 800 | 4,000 | 16,500 |
| International |  |  |  | $\$ 1,005,988$ |

## RUN NUMBER 19

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps Near-Term LEAP Put Is below ATM 2 Strike Price:

No. of Steps Far-Term LEAP Put Is below ATM 2 Strike Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y

Stocks of ITM Far-Term LEAPS Are Purchased: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.6
Minimum Standard \& Poor's Rating: B+

No. of Stocks Meeting Either Criterion: 115

Table 10.21
LEAP OTM and ITM Rates

|  | LEAPS <br> Written | LEAPS <br> Expired | Expired <br> OTM | OTM Rate | Expired <br> ITM | ITM Rate | LEAPS <br> Active |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 12,678 | 11,616 | 11,054 | $95.2 \%$ | 562 | $4.8 \%$ | 1,062 |
| Far: | 13,186 | 10,778 | 10,343 | $96.0 \%$ | 435 | $4.0 \%$ | 2,408 |
| Total: | 25,864 | 22,394 | 21,397 | $95.5 \%$ | 997 | $4.5 \%$ | 3,470 |

Table 10.22
Premiums Collected and Realized Gain for Expired LEAPS

|  | Expired | Collected | Value | Exposure | Gain | Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 11,616 | $\$ 447,303$ | $\$ 477,653$ | $\$ 190,971$ | $\$ 286,682$ | $64.1 \%$ |
| Far: | 10,778 | $\$ 1,689,566$ | $\$ 1,777,415$ | $\$ 768,734$ | $\$ 128,680$ | $221.3 \%$ |
| Total: | 22,394 | $\$ 1,136,869$ | $\$ 1,255,068$ | $\$ 959,706$ | $\$ 295,36$ | $226.0 \%$ |

Table 10.23
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | Active | 1,062 | $\$ 140,761$ | $\$ 143,416$ | $\$ 117,980$ |

Table 10.24
Premiums Collected and Account Values

|  | Original <br> Contracts | Premiums <br> Collected | Compound <br> Gain | Unrealized <br> Gain | Stock <br> Value | Account <br> Value | Value <br> Ratio |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 12,116 | $\$ 588,065$ | $\$ 385,946$ | $\$ 25,436$ | $\$ 0$ | $\$ 411,383$ | $70.0 \%$ |
| Far: | 13,186 | $\$ 1,053,750$ | $\$ 235,031$ | $\$ 298,184$ | $\$ 1,977,738$ | $\$ 2,110,953$ | $200.3 \%$ |
| Total: | 25,302 | $\$ 1,641,814$ | $\$ 420,978$ | $\$ 123,621$ | $\$ 1,977,738$ | $\$ 2,522,336$ | $153.6 \%$ |

Table 10.25
List of Stocks Purchased

| Name of Company | Trading Symbol | No. of Shares | Cost Basis | Stock <br> Value |
| :---: | :---: | :---: | :---: | :---: |
| Adobe Systems | ADBE | 300 | \$ 11,363 | \$ 12,038 |
| Allied Signal | ALD | 500 | 8,613 | 35,625 |
| Altera | ALTR | 500 | 1,955 | 21,500 |
| American Express | AXP | 600 | 10,930 | 35,925 |
| Applied Materials | AMAT | 700 | 2,439 | 32,463 |
| ASA Holdings | ASAI | 1,900 | 25,212 | 39,425 |
| Atlantic Richfield | ARC | 700 | 78,750 | 94,500 |
| Boeing | BA | 100 | 3,525 | 9,863 |
| Bristol-Myers Squibb | BUY | 700 | 20,350 | 41,300 |
| Chase Manhattan | CMB | 1,600 | 27,625 | 149,800 |
| Compaq | CPQ | 800 | 9,380 | 61,300 |
| Conseco | CNC | 600 | 499 | 21,375 |
| CUC International | CU | 1,700 | 3,097 | 38,250 |
| Dun \& Bradstreet | DNB | 1,600 | 46,550 | 40,600 |
| Equifax | EFX | 200 | 1,439 | 5,450 |
| Gap | GPS | 400 | 1,850 | 13,400 |
| General Mills | GIS | 100 | 4,909 | 6,213 |
| Health South | HRC | 1,100 | 3,563 | 21,038 |


| Hewlett-Packard | HWP | 100 | 1,116 | 5,325 |
| :--- | :--- | :---: | :---: | :---: |
| Hilton Hotels | HLT | 900 | 9,169 | 21,825 |
| Household | HI | 400 | 7,550 | 34,450 |
| International |  |  |  |  |
| Intel | INTC | 300 | 1,950 | 41,738 |
| International Game | IGT | 2,200 | 28,000 | 35,475 |
| KMart | KM | 2,600 | 26,175 | 31,525 |
| Limited | LTD | 1,500 | 24,147 | 27,563 |
| Lowe's | 500 | 2,960 | 18,688 |  |
| Magna | MGA | 2,100 | 11,098 | 104,213 |
| International |  |  |  | 3, |
| Merck | MRK | 400 | 14,600 | 3,700 |
| Merrill Lynch | MER | 600 | 7,848 | 51,525 |
| NationsBank | NB | 200 | 2,813 | 11,100 |

(Table continued on next page)

Table 10.25
List of Stocks Purchased (Continued)

| Name of Company | Trading Symbol | No. of Shares | Cost <br> Basis | Stock <br> Value |
| :---: | :---: | :---: | :---: | :---: |
| NEXTEL | NXTL | 2,000 | \$ 24,200 | \$ 26,750 |
| Office Depot | ODP | 300 | 1,304 | 6,113 |
| Oracle | ORCL | 2,000 | 6,121 | 77,125 |
| Philip Morris | MO | 1,300 | 77,975 | 148,688 |
| Polaroid | PRD | 1,700 | 47,013 | 67,575 |
| Reebok <br> International | RBK | 500 | 5,875 | 22,438 |
| Salomon | SB | 300 | 9,750 | 14,963 |
| Schlumberger | SLB | 600 | 32,975 | 64,350 |
| Schwab | SCH | 100 | 200 | 3,188 |
| Southwest Air | LUV | 300 | 1,433 | 6,638 |
| Sprint | FON | 1,100 | 21,725 | 49,913 |
| Sun Microsystems | SUNW | 600 | 3,600 | 17,325 |
| SunAmerica | SAI | 400 | 927 | 15,050 |
| Toys "R" Us | TOY | 1,200 | 28,575 | 33,600 |
| Travelers | TRV | 1,000 | 6,147 | 47,875 |
| United HealthCare | UNH | 500 | 641 | 23,813 |
| US Surgical | USS | 2,100 | 59,175 | 64,050 |
| Wells Fargo | WFC | 600 | 37,500 | 170,475 |

Wendy's
WEN
International

Totals
43,500
1,000
4,125
(43,500

## RUN NUMBER 20

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps Near-Term LEAP Put Is below ATM 2 Strike Price:

No. of Steps Far-Term LEAP Put Is below ATM 2 Strike Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y

Stocks of ITM Far-Term LEAPS Are Purchased: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.2

Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 10.26
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired <br> Written | Oxpired | OTM Rate | Expired |
| :--- | :--- | :--- | :---: | :--- | :--- |
| OTM |  |  |  |  |  |$\quad$ ITM $\quad$| LEAPS |
| :--- |
| ITM |


| Near: | 5,705 | 5,254 | 5,065 | $96.4 \%$ | 189 | $3.6 \%$ | 451 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | 14,953 | 4,847 | $97.9 \%$ | 106 | $2.1 \%$ | 1,051 |
| Total: | 11,709 | 10,207 | 9,912 | $97.1 \%$ | 295 | $2.9 \%$ | 1,502 |

Table 10.27
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,254 | $\$ 123,882$ | $\$ 132,344$ | $\$ 19,707$ | $\$ 112,636$ | $90.9 \%$ |
| Far: | 14,953 | $\$ 206,272$ | $\$ 232,609$ | $\$ 190,502$ | $\$ 142,107$ | $20.4 \%$ |
| Total: | 10,207 | $\$ 330,155$ | $\$ 364,952$ | $\$ 210,209$ | $\$ 154,743$ | $46.9 \%$ |

Table 10.28
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS Active | Premiums <br> Collected | Forward <br> Value | Residual <br> Value | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 451 | $\$ 39,263$ | $\$ 40,008$ | $\$ 32,289$ | $\$ 7,719$ |
| Far: | 1,051 | $\$ 104,640$ | $\$ 108,597$ | $\$ 172,106$ | $\$ 36,491$ |
| Total: | 1,502 | $\$ 143,903$ | $\$ 148,605$ | $\$ 104,395$ | $\$ 44,210$ |

Table 10.29
Premiums Collected and Account Values

|  | Original <br> Contracts | Premiums <br> Collected | Compound <br> Gain | Unrealized <br> Gain | Stock <br> Value | Account <br> Value | Value <br> Ratio |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 5,516 | $\$ 163,146$ | $\$ 152,879$ | $\$ 7,719$ | $\$ 0$ | $\$ 160,598$ | $98.4 \%$ |
| Far: | 16,004 | $\$ 310,912$ | $\$ 170,938$ | $\$ 36,491$ | $\$ 462,413$ | $\$ 569,842$ | $183.3 \%$ |
| Total: | 11,520 | $\$ 474,058$ | $\$ 223,817$ | $\$ 44,210$ | $\$ 462,413$ | $\$ 730,440$ | $154.1 \%$ |

Table 10.30
List of Stocks Purchased

| Name of Company | Trading | No. of Shares | Cost <br> Basis |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Symbol |  |  | Value |
| ASA Holdings | ASAI | 1,900 | \$ 25,212 | \$ 39,425 |
| Bristol-Myers Squibb | BMY | 700 | 20,350 | 41,300 |
| Conseco | CNC | 600 | 499 | 21,375 |
| Equifax | EFX | 200 | 1,439 | 5,450 |
| Gap | GPS | 400 | 850 | 13,400 |
| General Mills | GIS | 100 | 4,909 | 6,213 |
| Hewlett-Packard | HWP | 100 | 1,116 | 5,325 |
| Limited | LTD | 1,500 | 24,147 | 27,563 |
| Lowe's | LOW | 500 | 2,960 | 18,688 |
| Merck | MRK | 400 | 14,600 | 33,700 |
| NationsBank | NB | 200 | 2,813 | 11,100 |
| Philip Morris | MO | 1,300 | 77,975 | 148,688 |
| Southwest Air | LUV | 300 | 1,433 | 6,638 |
| SunAmerica | SAI | 400 | 927 | 15,050 |
| Travelers | TRV | 1,000 | 6,147 | 47,875 |
| Wendy's International | WEN | 1,000 | 4,125 | 20,625 |
| Totals |  | 10,600 | \$190,502 | \$462,413 |

## Summary

Table 10.31 compares the overall ten-year value ratios for the $\mathrm{B}+$ and A - minimum universes for the three independent situations in which LEAPS winding up in the money are not rolled out, are rolled out, and are both rolled out (near-term) and assigned (farterm).

Table 10.31
Figure of Merit Comparisons

| Run |  | Steps |  |  | Steady- <br> State <br> Retention <br> Rate | Ten-Year <br> Account <br> Ratio |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | No. of | below | Steady- <br> State |  |  |
| No. | Universe | Issues | ATM | OTM Rate |  |  |
| 1. | All | 217 | 0 | 77.7\% | 42.6\% | 44.3\% |
| 2. | B min | 178 | 0 | 80.0 | 54.3 | 57.5 |
| 3. | $B+\min$ | 115 | 0 | 84.0 | 66.2 | 69.7 |
| 4. | A- min | 50 | 0 | 87.1 | 79.9 | 84.9 |
| 5. | $B+\min$ | 115 | 1 | 92.5 | 90.4 | 72.6 |
| 6. | A- min | 50 | 1 | 95.1 | 90.0 | 91.6 |
| 7. | $B+\min$ | 115 | 2 | 95.6 | 71.1 | 73.6 |
| 8. | A- min | 50 | 2 | 97.1 | 95.7 | 98.3 |
| 9. | $\mathrm{B}+\mathrm{min}$ | 115 | 0 | 84.3 | 78.5 | 80.3 |
| 10. | A- min | 50 | 0 | 87.5 | 92.7 | 95.9 |
| 11. | $\mathrm{B}+\mathrm{min}$ | 115 | 1 | 92.4 | 76.9 | 77.9 |
| 12. | A- min | 50 | 1 | 95.3 | 96.2 | 96.8 |
| 13. | $B+\min$ | 115 | 2 | 95.6 | 76.1 | 77.5 |
| 14. | A- min | 50 | 2 | 97.1 | 100.7 | 103.2 |
| 15. | $B+\min$ | 115 | 0 | 84.0 | -4.2 | 149.6 |
| 16. | A- min | 50 | 0 | 87.1 | 14.4 | 154.2 |
| 17. | $\mathrm{B}+\mathrm{min}$ | 115 | 1 | 92.4 | 8.5 | 149.1 |


| 18. | A- $\min$ | 50 | 1 | 95.2 | 23.9 | 144.7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 19. | B $+\min$ | 115 | 2 | 95.5 | 26.0 | 153.6 |
| 20. | A- $\min$ | 50 | 2 | 97.1 | 46.9 | 154.1 |

As you can see from Tables 10.31, adopting the combined rollover and stock acquisition strategy can substantially improve long-term account values.

## At-the-Money Results

For the $\mathrm{B}+$ minimum universe of 115 stocks with at-the-money LEAPS, the account ratio progressively increases from 66.7 percent without rollovers in Run No. 3 to 80.3 percent with rollovers in Run No. 9 to 149.6 percent with the combined rollover/acquisition strategy in Run No. 15.

For the A- minimum universe of 50 stocks, the account ratio progressively increases from 84.9 percent without rollovers in Run No. 4 to 95.9 percent with rollovers in Run No. 10 to 154.2 percent with the combined rollover/acquisition strategy in Run No. 16.

## One-Step Out-of-the-Money Results

For the $\mathrm{B}+$ minimum universe of 115 stocks with one-step out-of-the-money LEAPS, the account ratio progressively increases from 72.6 percent without rollovers in Run No. 5 to 77.9 percent with roll-overs in Run No. 11 to 149.1 percent with the combined rollover/ acquisition strategy in Run No. 17.

For the A- minimum universe of 50 stocks, the account ratio progressively increases from 91.6 percent without rollovers in Run No. 6 to 96.8 percent with rollovers in Run No. 12 to 144.7 percent with the combined rollover/acquisition strategy in Run No. 18.

## Two-Step Out-of-the-Money Results

For the $\mathrm{B}+$ minimum universe of 115 stocks with two-step out-of-the-money LEAPS, the account ratio progressively increases from 73.6 percent without rollovers in Run No. 7 to 77.5 percent with roll-overs in Run No. 13 to 153.6 percent with the combined rollover/ acquisition strategy in Run No. 19.

For the A- minimum universe of 50 stocks, the account ratio progressively increases from 98.3 percent without rollovers in Run No. 8 to 103.2 percent with rollovers in Run No. 14 to 154.1 percent with the combined rollover/acquisition strategy in Run No. 20.

## 11-

## Advanced Strategies

## Introduction

The strategies thus far investigated barely begin to cover the many ways to acquire stock using the premiums received from the sale of LEAP puts. One method that I especially like is to divide the potential universe of higher-rated issues having LEAPs into three categories: (1) stocks that I favor highly, currently hold in portfolio, and want to acquire more of; (2) stocks that I would like to acquire for my portfolio at below-market prices; and (3) stocks that I am more or less neutral about, but would not mind acquiring for my portfolio at prices substantially below today's market prices. In keeping with this "triage" approach, I sell into-the-money LEAP puts on stocks in the first category, at-the-money LEAP puts on the second category, and out-of-the-money puts on the third category. I use the term into-the-money rather than in-the-money to signify the use of exercise prices not more than one or at most two strikes above the current market price.

As a variation on this theme, you could take the 50 or so stocks classified as A- or better and sell into-the-money LEAP puts on the ones rated A+, at-the-money puts on the ones rated A , and out-of-the-money puts on the ones rated A -. Once you acquire proficiency and experience, you could start including B+ rated stocks in this last group as well.

There are so many variations possible on this strategy that as a practical matter I decided to limit the analysis to just two variations, both of which are examined in this chapter. The first method considered is to restrict the sale of LEAP puts to far-term LEAPS and not deal with near-term LEAPS at all. The second method is a mix-and-match approach, in which puts are simultaneously sold on both higher-quality, far-term LEAPS and broader-quality, near-term LEAPS.

## Far-Term LEAPS Alone Strategy

The computer simulations conducted thus far have clearly demonstrated that far-term LEAPS are consistently more profitable and safer than near-term LEAPS. The reasons for this include the fact that standard option-pricing formulas do not take into account the long-term growth rates of the underlying issue and the quite reasonable assumption that over the long term, stock prices of better-quality issues move inexorably upwards.

The effect of restricting the sale of puts to far-term LEAPS can be seen by extracting the relevant line items from the 20 computer simulations already performed. The combined rollover and acquisition strategy is the equivalent of selling two far-term LEAPS on each issue every month. Should any such pair of LEAP puts appear to be winding up in the money as expiration approaches, one of them is rolled out while the other is used to acquire stock as a result of exercise and assignment. When this strategy is employed, the summary chart for far-term LEAPS appears as shown in Table 11.1.

Comparing the results for the far-term LEAPS alone in Table 11.1 with those for the mixed near-term/far-term LEAPS in Table 10.31 clearly shows the improvement in the steady-state out-of-the-money and retention rates obtainable. Although the account value ratios are roughly the same, in terms of absolute dollars the ten-year account values for the far-term LEAPS alone are much larger because the base of premiums collected to which those percentages are applied is so much larger.

The list of stocks acquired is the same as shown for Runs No. 15 through 20 in the previous chapter.

Table 11.1
Figure of Merit Comparisons

|  |  |  | Steps |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Run No. | Universe | No of Issues | below <br> ATM | Steady- <br> State <br> OTM Rate | Steady- <br> State <br> Retention <br> Rate | Ten-Year <br> Account <br> Ratio |
| 1. | All | 217 | 0 | 77.7\% | 42.6\% | 44.3\% |
| 2. | B min | 178 | 0 | 80.0 | 54.3 | 57.5 |
| 3. | $\mathrm{B}+\mathrm{min}$ | 115 | 0 | 84. | 66.2 | 69.7 |
| 4. | A- min | 50 | 0 | 87.1 | 79.9 | 84.9 |
| 5. | $\mathrm{B}+\mathrm{min}$ | 115 | 1 | 92.5 | 70.4 | 72.6 |
| 6. | A- min | 50 | 1 | 95.1 | 90.0 | 91.6 |
| 7. | $\mathrm{B}+\mathrm{min}$ | 115 | 2 | 95.6 | 71.1 | 73.6 |
| 8. | A- min | 50 | 2 | 97.1 | 95.7 | 98.3 |
| 9. | $\mathrm{B}+\mathrm{min}$ | 115 | 0 | 84.3 | 78.5 | 80.3 |
| 10. | A- min | 50 | 0 | 87.5 | 92.7 | 95.9 |
| 11. | $\mathrm{B}+\mathrm{min}$ | 115 | 1 | 92.4 | 76.9 | 77.9 |
| 12. | A- min | 50 | 1 | 95.3 | 96.2 | 96.8 |
| 13. | $B+$ min | 115 | 2 | 95.6 | 76.1 | 77.5 |
| 14. | A- min | 50 | 2 | 97.1 | 100.7 | 103.2 |
| 9/15 | $B+$ min | 115 | 0 | 86.5 | 8.4 | 142.7 |
| 10/16 | A- min | 50 | 0 | 89.8 | 26.3 | 147.9 |
| 11/17 | $B+\min$ | 115 | 1 | 93.2 | 24.6 | 139.0 |


| $12 / 18$ | A- $\min$ | 50 | 1 | 95.6 | 40.8 | 137.5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $13 / 19$ | B $+\min$ | 115 | 2 | 96.0 | 42.6 | 140.6 |
| 1420 | A- $\min$ | 50 | 2 | 97.9 | 63.5 | 144.4 |

## Mix-and-Match Strategies

Another strategy is to sell far-term LEAP puts on the higher-quality, A- minimum universe of 50 stocks while at the same time selling near-term LEAP puts on the broader-quality $\mathrm{B}+$ minimum universe of 115 stocks. The near-term B+ LEAP puts would be rolled over if they wind up in the money as expiration approaches, while the far-term A-LEAP puts would be used for stock acquisition. Because of the higher financial exposure and potential risk of assignment of the near-term B+ LEAPS, the strike prices selected for them will be one step below the level selected for the far-term A- LEAP puts. Two such mix-and-match combinations have been selected to illustrate the approach, ranging from the most conservative to the most aggressive.

## Conservative Mix-and-Match Strategy

Run No. 21 shows the results of selling far-term LEAPS that are one step out of the money on the A- minimum universe of 50 stocks while simultaneously selling near-term LEAPS that are two steps out of the money on the B+ minimum universe of 115 stocks. The results shown are stronger than those obtained in Run No. 18, for which the far-term LEAP universe was also the A- minimum universe of 50 stocks. In particular, collecting premiums from the larger universe of 115 near-term LEAPS has the net effect of lowering overall risk with only a moderate reduction of overall benefits. Although the account value is 122.3 percent of the total premiums collected-down from the 144.7 percent figure seen in Run No. 18-it is applied to a larger base. The list of acquired stocks for this mix-and-match strategy is the same as the one for Run No. 18.

## Moderate Mix-and-Match Strategy

Run No. 22 shows the results of selling far-term LEAPS that are at the money on the Aminimum universe of 50 stocks while simultaneously selling near-term LEAPS that are one step out of the money on the $\mathrm{B}+$ minimum universe of 115 stocks. The results shown are stronger than those obtained in Run No. 16, for which the far-term LEAP universe was also the A- minimum universe of 50 stocks. In particular, collecting premiums from the larger universe of 115 near-term LEAPS has the net effect of lowering overall risk, again with only a moderate reduction of overall benefits. And as with the conservative strategy, although the account value is 135 percent of the total premiums collecteddown from the 154.2 percent figure seen in Run No. 16-it is applied to a larger base. The list of acquired stocks for this mix-and-match strategy is the same as the one for Run No. 16.

## RUN NUMBER 21

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps Near-Term LEAP Put Is below ATM 2 Strike Price:

No. of Steps Far-Term LEAP Put Is below ATM 1 Strike Price:

Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y

Stocks of ITM Far-Term LEAPS Are Purchased: Y

Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum Near-Term First Call Rating: 1.6
Minimum Near-Term Standard \& Poor's Rating: B+

No. of Stocks Meeting Either Criterion: 115

Minimum Far-Term First Call Rating: 1.2

Minimum Far-Term Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 11.2
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired | OTM | Expired | ITM | LEAPS |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Written | Expired | OTM | Rate | ITM | Rate | Active |


| Near: | 12,678 | 11,616 | 11,054 | $95.2 \%$ | 562 | $4.8 \%$ | 1,062 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | 14,953 | 14,729 | $95.5 \%$ | 224 | $4.5 \%$ | 1,051 |

Total:
18,682
16,569
15,783
95.3\%
786
4.7\%
2,113

Table 11.3
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 11,616 | $\$ 447,303$ | $\$ 477,653$ | $\$ 190,971$ | $\$ 286,682$ | $64.1 \%$ |
| Far: | 14,953 | $\$ 385,272$ | $\$ 434,226$ | $\$ 511,671$ | $-\$ 77,444$ | $-20.1 \%$ |
| Total: | 16,569 | $\$ 832,576$ | $\$ 911,880$ | $\$ 702,642$ | $\$ 209,238$ | $25.1 \% \mathrm{z}$ |

Table 11.4
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,062 | $\$ 140,761$ | $\$ 143,416$ | $\$ 117,980$ | $\$ 25,436$ |
| Far: | 1,051 | $\$ 189,212$ | $\$ 196,907$ | $\$ 128,283$ | $\$ 68,623$ |
| Total: | 2,113 | $\$ 329,973$ | $\$ 340,323$ | $\$ 246,263$ | $\$ 94,060$ |

Table 11.5
Premiums Collected and Account Values

|  | Original <br> Contracts | Premiums <br> Collected | Compound <br> Gain | Unrealized <br> Gain | Stock <br> Value | Account <br> Value | Value <br> Ratio |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 12,116 | $\$ 588,065$ | $\$ 385,946$ | $\$ 25,436$ | $\$ 0$ | $\$ 411,383$ | $70.0 \%$ |
| Far: | 16,004 | $\$ 1,574,484$ | $-\$ 164,046$ | $\$ 68,623$ | $\$ 1,005,988$ | $\$ 1,010,565$ | $175.9 \%$ |
| Total: | 18,120 | $\$ 1,162,549$ | $\$ 321,901$ | $\$ 94,060$ | $\$ 1,005,988$ | $\$ 1,421,948$ | $122.3 \%$ |

## RUN NUMBER 22

ATM Strike Price Is the High, Low, or Closing C Stock Price:
No. of Steps Near-Term LEAP Put Is below ATM 1 Strike Price:
No. of Steps Far-Term LEAP Put Is below ATM 0 Strike Price:
Minimum No. of Months till Expiration: 8
ITM Near-Term LEAPS Are Rolled Over: Y
Stocks of ITM Far-Term LEAPS Are Purchased: Y
Premium Reinvestment Rate: $\quad 6.0 \%$
Minimum Near-Term First Call Rating: 1.6
Minimum Near-Term Standard \& Poor's Rating: B+
No. of Stocks Meeting Either Criterion: 115
Minimum Far-Term First Call Rating: 1.2
Minimum Far-Term Standard \& Poor's Rating: A-
No. of Stocks Meeting Either Criterion: 50

Table 11.6
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired | OTM | Expired | ITM | LEAPS |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Written | Expired | OTM |  | ITM |  | Active |


| Near: | 13,109 | 12,017 | 11,024 | $91.7 \%$ | 993 | $8.3 \%$ | 1,092 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | 14,953 | 14,435 | $89.5 \%$ | 1,518 | $10.5 \%$ | 1,051 |

$\begin{array}{llllllll}\text { Total: } & 19,113 & 16,970 & 15,459 & 91.1 \% & 1,511 & 8.9 \% & 2,143\end{array}$

Table 11.7
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 12,017 | $\$ 870,704$ | $\$ 929,123$ | $\$ 340,533$ | $\$ 588,590$ | $67.6 \%$ |
| Far: | 14,953 | $\$ 1,783,524$ | $\$ 1,882,534$ | $\$ 1,241,101$ | $-\$ 358,568$ | $-45.8 \%$ |
| Total: | 16,970 | $\$ 1,654,227$ | $\$ 1,811,657$ | $\$ 1,581,635$ | $\$ 230,023$ | $13.9 \%$ |

Table 11.8
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized <br> Gain |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | Active |  | Value | Value |  |
| Far: | 1,092 | $\$ 247,335$ | $\$ 251,999$ | $\$ 210,567$ | $\$ 41,432$ |
| Total: | 1,051 | $\$ 319,954$ | $\$ 333,714$ | $\$ 218,707$ | $\$ 115,007$ |

Table 11.9
Premiums Collected and Account Values

|  | Original <br> Contracts | Premiums <br> Collected | Compound <br> Gain | Unrealized <br> Gain | Stock <br> Value | Account <br> Value | Value <br> Ratio |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 12,116 | $\$ 1,118,039$ | $\$ 763,604$ | $\$ 41,432$ | $\$ 0$ | $\$ 805,036$ | $72.0 \%$ |
| Far: | 16,004 | $\$ 1,103,477$ | $-\$ 394,965$ | $\$ 115,007$ | $\$ 2,474,200$ | $\$ 2,194,242$ | $198.8 \%$ |
| Total: | 18,120 | $\$ 2,221,516$ | $\$ 368,639$ | $\$ 156,439$ | $\$ 2,474,200$ | $\$ 2,999,278$ | $135.0 \%$ |

## A Word of Caution

With enough time and experience, some investors may feel inclined to take on higher levels of risk by selling far-term LEAP puts that are deeply into the money and/or nearterm LEAP puts that are at the money. Fight the urge to do so, for adopting too aggressive an approach can leave you especially vulnerable to a sudden downturn in the market. How to protect oneself against such a downturn is the subject of the next chapter.

## 12-

## Hedging for Disaster

## Introduction

Each LEAP put in the previous chapters was sold as a "pure play," without any attempt to hedge against an unexpected downturn in the market. As described in Chapter 3, it is possible to lessen potential losses by buying a deep out-of-the-money LEAP put at the same time the primary, near-the-money LEAP put is sold. This type of hedging strategy is particularly useful if you are going to sell LEAP puts on lower-rated companies or on stocks known to be highly volatile. What this does is reduce potential profits while simultaneously reducing potential loss. Profit is reduced because the net premium generated is the difference between the premium received from the sale of the higherstrike LEAP put and the premium paid for the purchase of the lower-strike LEAP put.* On the other hand, the maximum amount of financial exposure is reduced from that of the strike price of the LEAP put sold to that of the difference between the two strike prices involved. Should the stock price fall below the strike price of the insurance put, the incremental financial exposure on the primary put is exactly counterbalanced by the incremental increase in value of the insurance put.

For example, suppose you sold an at-the-money LEAP put on a $\$ 100$ stock with a volatility 0.50 and with 24 months till expiration. From Table 2.1 (or Table A. 5 in Appendix A), you would expect to

[^4]receive a contract premium of $\$ 2,077.40$ for it. Suppose now that you had simultaneously purchased a LEAP put with strike price of $\$ 85$ on the same stock with the same expiration date. As indicated in Table A.8, you would expect to pay $\$ 1,374.10$ for it. Your net premium is therefore $\$ 2,077.40$ less $\$ 1,374.10$, or $\$ 703.30$. On the other hand, the maximum financial exposure is limited to $\$ 15$ a share, or $\$ 1,500$ per contract, no matter how low the price of the underlying issue at expiration.

## Procedure

For analysis purposes, suppose the strike price of the insurance put to be three steps below the strike price of the primary, at-the-money put. To what extent is the purchase of such disaster insurance worth it? To answer this question, I repeat Runs No. 1 through 4 but where, for each at-the-money LEAP put sold, a corresponding LEAP put three steps out of the money is simultaneously purchased for insurance purposes.

If the primary at-the-money LEAP put sold winds up out of the money at expiration, the net profit is the premium received on the at-the-money put less the price paid for the lower-strike insurance put. If the at-the-money LEAP put winds up in the money but above the strike price of the insurance put, the net profit or loss is calculated as the net premium received on the at-the-money LEAP and insurance puts less the financial exposure incurred at expiration on the at-the-money LEAP put. If the stock price at expiration is below the strike price of the insurance put, the overall financial exposure is the difference between the two strike prices involved offset by net premium received on the at-the-money LEAP and insurance puts.

## The Full Universe

Run No. 23 shows the effect of taking the full universe of 217 stocks considered in Run No. 1 and combining the same set of LEAP puts sold with the purchase of insurance puts at a strike price three steps out of the money. By comparing Table 12.1 with Table 6.3, we see that the premiums collected on expired LEAPS have fallen from $\$ 8,354,277$ to $\$ 6,494,411$, with the difference of $\$ 1,859,866$ being the cost of the insurance puts purchased. On the other hand, the financial exposure from puts expiring in the money falls from \$5,619,931 to
$\$ 4,325,249$, a reduction of $\$ 1,294,682$. Of the 39,405 expired LEAP contracts, 8,770 expired in the money, and it turns out that in just 2,541 of these instances was the stock price at expiration below the strike price of the insurance put.

What the computer simulation thus revealed was that in only 2,541 instances out of 39,405 expired LEAPS ( 6.4 percent) was the insurance protection of any value. The retention rate barely increased from 42.6 percent in Run No. 1 to 43.1 percent in Run No. 23 , while the account value at the end of the ten-year period barely increased from 44.3 percent in Run No. 1 to 44.9 percent in Run No. 23.

## The B Minimum Universe

Run No. 24 shows the effect of taking the B minimum universe of 178 stocks considered in Run No. 2 and combining the same set of LEAP puts sold with the purchase of insurance puts at a strike price three steps out of the money. By comparing Table 12.6 with Table 7.2, we see that the premiums collected on expired LEAPS have fallen from $\$ 6,803,725$ to $\$ 5,334,626$, with the difference of $\$ 1,469,099$ being the cost of the insurance puts purchased. On the other hand, the financial exposure from puts expiring in the money falls from $\$ 3,779,739$ to $\$ 3,043,533$, a reduction of $\$ 736,206$. Of the 33,312 expired LEAP contracts, 6,667 expired in the money, and in just 1,851 of these instances was the stock price at expiration below the strike price of the insurance put.

Thus, in only 1,851 instances out of 33,312 expired LEAPS ( 5.6 percent) was the insurance protection of any value. The retention rate decreased from 54.3 percent in Run No. 2 to 52.7 percent in Run No. 24, while the account value at the end of the ten-year period decreased from 57.5 percent in Run No. 2 to 55.2 percent in Run No. 24.

## The B+ Minimum Universe

Run No. 25 shows the effect of taking the B+ minimum universe of 115 stocks considered in Run No. 3 and combining the same set of LEAP puts sold with the purchase of insurance puts at a strike price three steps out of the money. By comparing Table 12.2 with Table 7.6, we see that the premiums collected on expired LEAPS have fallen from
$\$ 3,992,382$ to $\$ 3,205,536$, with the difference of $\$ 786,846$ being the cost of the insurance puts purchased. On the other hand, the financial exposure from puts expiring in the money falls from $\$ 1,742,423$ to $\$ 1,449,616$, a reduction of $\$ 292,807$. Of the 21,858 expired LEAP contracts, 3,504 expired in the money, and in just 798 of these instances was the stock price at expiration below the strike price of the insurance put.

Thus, in only 798 instances out of 21,858 expired LEAPS ( 3.7 percent) was the insurance protection of any value. The retention rate decreased from 66.2 percent in Run No. 3 to 64.5 percent in Run No. 25, while the account value at the end of the ten-year period decreased from 69.7 percent in Run No. 3 to 67.4 percent in Run No. 25.

## The A- Minimum Universe

Run No. 26 shows the effect of taking the A- minimum universe of 50 stocks considered in Run No. 4 and combining the same set of LEAP puts sold with the purchase of insurance puts at a strike price three steps out of the money. By comparing Table 12.14 with Table 7.10, we see that the premiums collected on expired LEAPS have fallen from $\$ 1,440,155$ to $\$ 1,201,730$, with the difference of $\$ 238,425$ being the cost of the insurance puts purchased. On the other hand, the financial exposure from puts expiring in the money falls from $\$ 431,447$ to $\$ 400,194$, a reduction of $\$ 31,252$. Of the 10,018 expired LEAP contracts, 1,291 expired in the money, and in just 261 of these instances it turns out, was the stock price at expiration below the strike price of the insurance put.

Thus, in only 261 instances out of 10,018 expired LEAPS ( 2.6 percent) was the insurance protection of any value. The retention rate decreased from 79.9 percent in Run No. 4 to 76.5 percent in Run No. 26, while the account value at the end of the ten-year period decreased from 84.9 percent in Run No. 4 to 80.3 percent in Run No. 26.

## RUN NUMBER 23

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Written Put Is below ATM 0 Strike Price:

No. of Steps LEAP Offset Put Is below ATM 3 Strike Price:

Minimum No. of Months till Expiration: 8
Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 5.0
Minimum Standard \& Poor's Rating: None
No. of Stocks Meeting Either Criterion: 217

Table 12.1
LEAP OTM and ITM Rates
LEAPS

Written \begin{tabular}{lllll}
LEAPS <br>
Expired

 

Expired <br>
OTM

$\quad$ OTM $\quad$

Expired <br>
ITM

$\quad$

ITM

 

LEAPS <br>
Active
\end{tabular}

Table 12.2
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums <br> Expired | Follected | Vorward | ITM | Exposure |
| :--- | :--- | :--- | :--- | :--- | :--- | | Realized |
| :--- |
| Gain |$\quad$| Retention |
| :--- |
| Rate |


| Near: | 20,022 | $\$ 3,104,413$ | $\$ 3,308,219$ | $\$ 2,155,055$ | $\$ 1,153,164$ | $37.1 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 19,383 | $\$ 3,389,999$ | $\$ 3,816,625$ | $\$ 2,170,194$ | $\$ 1,646,431$ | $48.6 \%$ |
| Total: | 39,405 | $\$ 6,494,411$ | $\$ 7,124,844$ | $\$ 4,325,249$ | $\$ 2,799,595$ | $43.1 \%$ |

Table 12.3
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,954 | $\$ 567,091$ | $\$ 578,315$ | $\$ 502,069$ | $\$ 76,246$ |
| Far: | 4,531 | $\$ 1,361,606$ | $\$ 1,425,978$ | $\$ 1,130,129$ | $\$ 295,850$ |
| Total: | 6,485 | $\$ 1,928,697$ | $\$ 2,004,293$ | $\$ 1,632,197$ | $\$ 372,096$ |

Table 12.4
Premiums Collected and Account Values

| Original | Premiums | Compound <br> Contracts | Unrealized <br> Collected | Account <br> Gain | Gain |
| :--- | :--- | :--- | :--- | :--- | :--- | | Value |
| :--- |


| Near: | 21,976 | $\$ 3,671,504$ | $\$ 1,391,834$ | $\$ 76,246$ | $\$ 1,468,080$ | $40.0 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 23,914 | $\$ 4,751,604$ | $\$ 2,014,816$ | $\$ 295,850$ | $\$ 2,310,665$ | $48.6 \%$ |
| Total: | 45,890 | $\$ 8,423,108$ | $\$ 3,406,649$ | $\$ 372,096$ | $\$ 3,778,745$ | $44.9 \%$ |

## RUN NUMBER 24

ATM Strike Price Is the High, Low, or Closing C Stock Price:
No. of Steps LEAP Written Put Is below ATM 0 Strike Price:
No. of Steps LEAP Offset Put Is below ATM 3 Strike Price:
Minimum No. of Months till Expiration:
8
Premium Reinvestment Rate: 6.0\%
Minimum First Call Rating: 2.0
Minimum Standard \& Poor's Rating: B
No. of Stocks Meeting Either Criterion: 178

Table 12.5
LEAP OTM and ITM Rates

| LEAPS | LEAPS | Expired | OTM | Expired | ITM | LEAPS |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Written | Expired | OTM | Rate | ITM | Rate | Active |


| Near: | 18,501 | 16,898 | 13,180 | $78.0 \%$ | 3,718 | $22.0 \%$ | 1,603 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 20,136 | 16,414 | 13,465 | $82.0 \%$ | 2,949 | $18.0 \%$ | 3,722 |
| Total: | 38,637 | 33,312 | 26,645 | $80.0 \%$ | 6,667 | $20.0 \%$ | 5,325 |

Table 12.6
Premiums Collected and Realized Gain for Expired LEAPS

|  | LEAPS <br> Expired | Premiums <br> Collected | Forward <br> Value | ITM <br> Exposure | Realized <br> Gain | Retention <br> Rate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Near: | 16,898 | $\$ 2,547,457$ | $\$ 2,714,666$ | $\$ 1,539,961$ | $\$ 1,174,705$ | $46.1 \%$ |


| Far: | 16,414 | $\$ 2,787,169$ | $\$ 3,137,963$ | $\$ 1,503,572$ | $\$ 1,634,391$ | $58.6 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Total: | 33,312 | $\$ 5,334,626$ | $\$ 5,852,629$ | $\$ 3,043,533$ | $\$ 2,809,096$ | $52.7 \%$ |

Table 12.7
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,603 | $\$ 486,381$ | $\$ 495,954$ | $\$ 421,270$ | $\$ 74,685$ |
| Far: | 3,722 | $\$ 1,135,391$ | $\$ 1,188,231$ | $\$ 2,882,713$ | $\$ 305,519$ |
| Total: | 5,325 | $\$ 1,621,772$ | $\$ 1,684,186$ | $\$ 1,303,983$ | $\$ 380,203$ |

Table 12.8
Premiums Collected and Account Values

| Original | Premiums <br> Contracts | Collected | Compound <br> Gain | Unrealized <br> Gain | Account <br> Value |
| :--- | :--- | :--- | :--- | :--- | :--- |


| Near: | 18,501 | $\$ 3,033,838$ | $\$ 1,435,859$ | $\$ 74,685$ | $\$ 1,510,544$ | $49.8 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 20,136 | $\$ 3,922,560$ | $\$ 2,020,553$ | $\$ 305,519$ | $\$ 2,326,071$ | $59.3 \%$ |
| Total: | 38,637 | $\$ 6,956,398$ | $\$ 3,456,412$ | $\$ 380,203$ | $\$ 3,836,615$ | $55.2 \%$ |

## RUN NUMBER 25

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Written Put Is below ATM 0 Strike Price:

No. of Steps LEAP Offset Put Is below ATM 3 Strike Price:

Minimum No. of Months till Expiration: 8
Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.6
Minimum Standard \& Poor's Rating: B+
No. of Stocks Meeting Either Criterion: 115

Table 12.9
LEAP OTM and ITM Rates

| LEAPS <br> Written | LEAPS <br> Expired | Expired OTM | OTM | Expired ITM | ITM | LEAPS <br> Active |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Rate |  | Rate |  |
| 12,116 | 11,080 | 9,055 | 81.7\% | 2,025 | 18.3\% | 1,036 |
| 13,186 | 10,778 | 19,299 | 86.3\% | 1,479 | 13.7\% | 2,408 |
| 25,302 | 21,858 | 18,354 | 84.0\% | 3,504 | 16.0\% | 3,444 |

Table 12.10
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Expired | Collected | | Forward |
| :--- |
| Value |$\quad$| ITM |
| :--- |
| Exposure |$\quad$| Realized |
| :--- |
| Gain |$\quad$ Retention


| Near: | 11,080 | $\$ 1,528,723$ | $\$ 1,629,084$ | $\$ 758,543$ | $\$ 870,541$ | $56.9 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 10,778 | $\$ 1,676,813$ | $\$ 1,887,890$ | $\$ 1,691,073$ | $\$ 1,196,817$ | $71.4 \%$ |
| Total: | 21,858 | $\$ 3,205,536$ | $\$ 3,516,975$ | $\$ 1,449,616$ | $\$ 2,067,358$ | $64.5 \%$ |

Table 12.11
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 1,036 | $\$ 311,806$ | $\$ 317,881$ | $\$ 267,573$ | $\$ 50,307$ |
| Far: | 2,408 | $\$ 1,708,403$ | $\$ 1,740,885$ | $\$ 511,335$ | $\$ 229,550$ |
| Total: | 3,444 | $\$ 1,020,209$ | $\$ 1,058,766$ | $\$ 778,909$ | $\$ 279,857$ |

Table 12.12
Premiums Collected and Account Values

| Original | Premiums <br> Contracts | Compound <br> Collected | Unrealized | Account <br> Gain | Value |
| :--- | :--- | :--- | :--- | :--- | :--- |


| Near: | 12,116 | $\$ 1,840,529$ | $\$ 1,074,331$ | $\$ 50,307$ | $\$ 1,124,639$ | $61.1 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 13,186 | $\$ 2,385,217$ | $\$ 1,492,354$ | $\$ 229,550$ | $\$ 1,721,903$ | $72.2 \%$ |
| Total: | 25,302 | $\$ 4,225,745$ | $\$ 2,566,685$ | $\$ 279,857$ | $\$ 2,846,542$ | $67.4 \%$ |

## RUN NUMBER 26

ATM Strike Price Is the High, Low, or Closing C Stock Price:

No. of Steps LEAP Written Put Is below ATM 0 Strike Price:

No. of Steps LEAP Offset Put Is below ATM 3 Strike Price:

Minimum No. of Months till Expiration: 8
Premium Reinvestment Rate: $\quad 6.0 \%$

Minimum First Call Rating: 1.2
Minimum Standard \& Poor's Rating: A-

No. of Stocks Meeting Either Criterion: 50

Table 12.13
LEAP OTM and ITM Rates

| LEAPS Written | LEAPS Expired | Expired OTM | OTM | Expired | ITM | LEAPS Active |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Rate | ITM | Rate |  |
| 5,516 | 5,065 | 4,292 | 84.7\% | 773 | 15.3\% | 451 |
| 16,004 | 14,953 | 4,435 | 89.5\% | 1,518 | 10.5\% | 1,051 |
| 11,520 | 10,018 | 8,727 | 87.1\% | 1,291 | 12.9\% | 1,502 |

Table 12.14
Premiums Collected and Realized Gain for Expired LEAPS

| LEAPS | Premiums | Forward | ITM | Realized | Retention |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Expired | Collected | Value | Exposure | Gain | Rate |


| Near: | 5,065 | $\$ 564,691$ | $\$ 601,888$ | $\$ 208,718$ | $\$ 393,170$ | $69.6 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 14,953 | $\$ 1,637,039$ | $\$ 1,717,371$ | $\$ 191,477$ | $\$ 525,894$ | $82.6 \%$ |
| Total: | 10,018 | $\$ 1,201,730$ | $\$ 1,319,259$ | $\$ 400,194$ | $\$ 919,064$ | $76.5 \%$ |

Table 12.15
Premiums Collected and Unrealized Gain on Active LEAPS

|  | LEAPS | Premiums <br> Collected | Forward | Residual | Unrealized |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Active |  | Value | Value | Gain |
| Near: | 451 | $\$ 119,564$ | $\$ 121,862$ | $\$ 100,945$ | $\$ 20,917$ |
| Far: | 1,051 | $\$ 264,843$ | $\$ 276,696$ | $\$ 178,769$ | $\$ 197,927$ |
| Total: | 1,502 | $\$ 384,407$ | $\$ 398,558$ | $\$ 279,714$ | $\$ 118,844$ |

Table 12.16
Premiums Collected and Account Values

| Original | Premiums | Compound | Unrealized | Account <br> Contracts | Collected |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Gain | Gain | Value |  |  |  |


| Near: | 5,516 | $\$ 684,254$ | $\$ 494,713$ | $\$ 20,917$ | $\$ 515,630$ | $75.4 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Far: | 16,004 | $\$ 1,901,882$ | $\$ 1,659,791$ | $\$ 197,927$ | $\$ 1,757,718$ | $84.0 \%$ |
| Total: | 11,520 | $\$ 1,586,137$ | $\$ 1,154,504$ | $\$ 118,844$ | $\$ 1,273,349$ | $80.3 \%$ |

## Conclusions

Historically, it would appear that the use of insurance puts to hedge against market downturns is not a cost-effective strategy when dealing with highly rated stocks, and over the long run, it appears to be only marginally beneficial for lesser-quality issues. As a result of this analysis and my own experience, I have never bought protective puts as a hedge against LEAP puts written on high-quality companies rated $\mathrm{B}+$ and above. In the short run, it is entirely possible for market prices to drop below exercise prices (this has happened to me on numerous occasions), but in such instances I prefer to use rollout techniques as my primary recovery-and-repair strategy.

I sidestep the issue of whether or not to buy insurance puts on stocks rated B and below by ordinarily not writing LEAP puts on such lesser-quality issues in the first place. On those (few) occasions that I elect to sell LEAP puts on lesser-rated companies, I weigh the cost of the insurance put against the premium received from the LEAP put written and the perceived downside risk. If I feel there is little downside risk (because the market is particularly strong, or the stock is bottoming out after a pronounced retreat), I will not bother purchasing an insurance put. If the market seems weak and the stock is well above its lows, I am far more likely to consider the use of an insurance put-or not selling a LEAP put at all.

Having said this, I would recommend the use of insurance puts when doing your first few transactions. It will make you, your broker, and your broker's branch manager more comfortable as you learn the ropes and become more proficient in selling naked puts. As your asset base grows and your option experience builds up, you can begin relaxing this constraint by phasing out the use of insurance puts, first on A rated companies, then on A- rated companies, and finally on B+ rated companies.

PART THREE-
VOLATILITY AND PREMIUMS

## 13-

## Measuring Volatility

## Introduction

The volatility of the underlying stock is extremely important in the world of options because, among other things, it determines the likelihood that an option will wind up in or out of the money by the expiration date. This chapter describes the procedure by which volatility is numerically calculated and shows how to calculate the chances that a given LEAP option will wind up in or out of the money by its expiration date.

To begin, suppose that:
$P$ is the price of the underlying issue
$S$ is the strike (exercise price) of the option
$r$ is the risk-free interest rate in decimal form
$t$ is the time in years till expiration
$v$ is the annualized volatility in decimal form
$\delta$ the annualized dividend rate in decimal form
Further, let $h$ be given by:
$h=\frac{\ln (P / S)+\left(r-\delta+v^{2} / 2\right) \times t}{v \sqrt{t}}$

Then the probability of winding up in the money by the expiration date for a put option is given by:

$$
\begin{equation*}
\text { Prob (in-the-money put) }=\int_{-\infty}^{-h+\sqrt{t}} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x \tag{13.2}
\end{equation*}
$$

The probability of winding up in the money by the expiration date for a call option is given by:
$\operatorname{Prob}$ (in-the-money call) $=1-\int_{-\infty}^{-h+\sqrt{t}} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x$
The integral in Equations 13.2 and 13.3 is the standard normal distribution, where

$$
\begin{equation*}
\int_{-\infty}^{\infty} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x=1 \tag{13.4}
\end{equation*}
$$

## Example

As an example, consider the case of an at-the-money put where the stock price $P$ is the same as the exercise price $S$. The $\log$ of 1 is zero, so the formula for $-h+v \sqrt{t}$ now becomes:
$-h+v \sqrt{t}=\left(0.5 \times v^{2}+\delta-r\right) \times\left(\frac{\sqrt{t}}{v}\right)$
What Equation 13.5 shows is that other things being equal, the higher the annual dividend rate, the more likely it is that a LEAP put will wind up in the money. This is a natural consequence of the fact that the effect of dividends is to reduce the value of the underlying stock.

Consider a case in which the volatility is 0.3 , the risk-free interest rate $r$ is 6 percent, and the annualized dividend rate $\delta$ is 1.5 percent. In this situation $-h+v \sqrt{t}$ is zero, and the integral in either Equation 13.2 or Equation 13.3 is 0.5 . Thus, the chance of such an at-the-money put (or call) winding up in the money at expiration under those circumstances is precisely one half. Whenever $0.5 \times v^{2}+\delta-r$ is greater than zero, the chance that at-the-money puts will wind up in the money is going to be greater than $50-50$; and whenever $0.5 \times v^{2}+\delta-r$ is less
than zero, the chance that at-the-money puts will wind up in the money are going to be less than 50-50. Appendix C contains a list of tables showing the probability of LEAP puts winding up in the money for a wide range of parameters.

## Volatility

Looking at the six inputs to Equations 13.1 and 13.3, the stock price, strike price, interest rate, expiration date, and dividend rate are all known variables. The unknown variable is the volatility, and estimates of it must be prepared based on the recent price history of the underlying stock.

A major assumption underlying most option-pricing models is that prices are normally distributed about the mean. In descriptive terms, this means that if a stock is currently at $\$ 20$ a share, it is just as likely to double and go to $\$ 40$ as it is to be cut in half and wind up at $\$ 10$ a share. In keeping with this assumption, annual volatility is computed by taking a time series of closing prices $P i$ where $i$ runs from 1 to $N$ and thencalculating the logarithmic change ratios $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$. The mean ratio is calculated as:

$$
\begin{align*}
\mu & =\frac{1}{N} \sum_{i=1}^{N} x_{i}=\frac{1}{N} \sum_{i=1}^{N} \ln \left(p_{i} / p_{i-1}\right)=\frac{1}{N} \sum_{i=1}^{N}\left(\ln p_{i}-\ln p_{i-1}\right) \\
& =\frac{1}{N}\left(\ln p_{N}-\ln p_{0}\right)=\frac{1}{N} \ln \left(p_{N} / p_{0}\right) \tag{13.6}
\end{align*}
$$

Note that the mean logarithmic change ratio depends solely on the ratio of the last term to the first term in the series, $p_{N} / p_{0}$.

The variance and standard deviation about the mean are calculated as:
var $=\sigma^{2}=\frac{1}{N-1} \sum_{i=1}^{N}\left(x_{i}-\mu\right)^{2}$
If the prices $p_{i}$ have been collected every $d$ (trading) days, the annualized volatility is calculated as the adjusted standard deviation, as follows:
$v=\sqrt{\frac{T}{d}} \times \sigma$

Table 13.1
Volatility Using Monthly Data

| No. | Date | Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 12/29/95 | 56.7500 | - | - |
| 1 | 01/31/96 | 55.2380 | -0.02700464 | 0.00934638 |
| 2 | 02/29/96 | 58.8170 | 0.06277973 | 0.00004750 |
| 3 | 03/29/96 | 56.8750 | -0.03357512 | 0.01065997 |
| 4 | 04/30/96 | 67.7500 | 0.17496860 | 0.01108737 |
| 5 | 05/31/96 | 75.5000 | 0.10830800 | 0.00149274 |
| 6 | 06/28/96 | 73.4440 | -0.02760950 | 0.00946370 |
| 7 | 07/31/96 | 75.1250 | 0.02263005 | 0.00221295 |
| 8 | 08/30/96 | 79,8125 | 0.06052675 | 0.00008364 |
| 9 | 09/30/96 | 95,4375 | 0.17879140 | 0.01190704 |
| 10 | 10/31/96 | 109.8750 | 0.14087180 | 0.00506941 |
| 11 | 11/29/96 | 126,8750 | 0.14385890 | 0.00550370 |
| 12 | 12/31/96 | 130.9375 | 0.03151786 | 0.00145574 |
|  | Totals |  | 0.83606383 | 0.06833014 |

where $T$ is the number of trading days in the year (ordinarily 252 to 254 ). If monthly data are used, $d=21$; if weekly data are used, $d=5$; and if daily trading data are used, $d=1$. The number of observations $N$ is usually selected so as to yield a stabilized result and is often chosen so that $N$ times $d$ equals $T$.

Table 13.1 illustrates how each of these variables is calculated from a specified price history. The example chosen employs the month-end closing prices for Intel Corporation for the year 1996.

The mean value of the price ratios in Table 13.1 is:
$\mu=0.83606383 / 12=\ln (130.9375 / 56.75) / 12=0.069672$
The variance is: var $=0.06833014 / 11=0.006212$
The standard deviation is $\sigma=\sqrt{\text { var }}=0.078815$
The annualized volatility is $v=\sqrt{12} \times \sigma:=0.273023$
This example illustrates the procedure. It is to be noted, however, that the use of monthly data for estimating the annualized volatility does not yield sufficiently accurate results for modeling purposes. If the procedure is repeated using daily data, a much different value for the annualized volatility is obtained, as shown in Table 13.2.

Table 13.2
Volatility Using Daily Data

| No. | Date | Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 12/29/95 | 56.7500 | - | - |
| 1 | 01/02/96 | 58.6250 | 0.03250553 | 0.00085345 |
| 2 | 01/03/96 | 57.7500 | -0.01503783 | 0.00033597 |
| 3 | 01/04/96 | 57.5000 | -0.00433847 | 0.00005822 |
| 4 | 01/05/96 | 57.5000 | 0.00000000 | 0.00001083 |
| 5 | 01/08/96 | 57.6250 | 0.00217155 | 0.00000125 |
| 6 | 01/09/96 | 55.0000 | -0.04662335 | 0.00249150 |
| 7 | 01/10/96 | 54.1250 | $-0.01603705$ | 0.00037360 |
| 8 | 01/11/96 | 56.8750 | 0.04955970 | 0.00214074 |
| 9 | 01/12/96 | 56.6250 | -0.00440533 | 0.00005924 |
| 10 | 01/15/96 | 53.3750 | -0.05910817 | 0.00389373 |
| 11 | 01/16/96 | 55.7500 | 0.04353501 | 0.00161953 |
| 12 | 01/17/96 | 50.0000 | -0.10885440 | 0.01257673 |
| 13 | 01/18/96 | 51.0000 | 0.01980251 | 0.00027261 |
| 14 | 01/19/96 | 51.3750 | 0.00732594 | 0.00001628 |
| 15 | 01/22/96 | 52.0000 | 0.01209189 | 0.00007745 |
| 16 | 01/23/96 | 52.6980 | 0.01333369 | 0.00010084 |
| 17 | 01/24/96 | 54.7500 | 0.03819987 | 0.00121859 |
| 18 | 01/25/96 | 54.6250 | -0.00228575 | 0.00003111 |


| 19 | 01/26/96 | 55.0000 | 0.00684148 | 0.00001260 |
| :---: | :---: | :---: | :---: | :---: |
| 20 | 01/29/96 | 54.4480 | -0.01008702 | 0.00017899 |
| 21 | 01/30/96 | 54.1250 | -0.00594993 | 0.00008541 |
| 22 | 01/31/96 | 55.2380 | 0.02035481 | 0.00029115 |
| 23 | 02/01/96 | 56.2500 | 0.01815488 | 0.00022092 |
| 24 | 02/02/96 | 56.7500 | 0.00884959 | 0.00003089 |
| 25 | 02/05/96 | 58.5000 | 0.03037108 | 0.00073330 |
| 26 | 02/06/96 | 59.5000 | 0.01694948 | 0.00018654 |
| 27 | 02/07/96 | 58.2500 | -0.02123220 | 0.00060142 |
| 28 | 02/08/96 | 57.8750 | -0.00645859 | 0.00009507 |
| 29 | 02/09/96 | 58.0000 | 0.00215746 | 0.00000129 |
| 30 | 02/12/96 | 58.2330 | 0.00400915 | 0.00000051 |
| 31 | 02/13/96 | 57.1250 | -0.01921037 | 0.00050634 |
| 32 | 02/14/96 | 58.0000 | 0.01520124 | 0.00014184 |
| 33 | 02/15/96 | 57.5000 | -0.00865809 | 0.00014279 |
| 34 | 02/16/96 | 57.5660 | 0.00114715 | 0.00000460 |
| 35 | 02/20/96 | 57.8750 | 0.00535328 | 0.00000425 |
| 36 | 02/21/96 | 59.2500 | 0.02348011 | 0.00040758 |
| 37 | 02/22/96 | 61.0000 | 0.02910813 | 0.00066649 |
| 38 | 02/23/96 | 60.8180 | -0.00298806 | 0.00003943 |
| 39 | 02/26/96 | 60.3750 | -0.00731072 | 0.00011241 |
| 40 | 02/27/96 | 60.2500 | -0.00207250 | 0.00002877 |


| 41 | $02 / 28 / 96$ | 60.7500 | 0.00826445 | 0.00002473 |
| :--- | :--- | :--- | :--- | :--- |
| 42 | $02 / 29 / 96$ | 58.8170 | -0.03233618 | 0.00126934 |
| 43 | $03 / 01 / 96$ | 56.0620 | -0.04797272 | 0.00262803 |
| 44 | $03 / 04 / 96$ | 54.8750 | -0.02140036 | 0.00060969 |
| 45 | $03 / 05 / 96$ | 55.3750 | 0.00907029 | 0.00003339 |
| 46 | $03 / 06 / 96$ | 53.2500 | -0.03913045 | 0.00179963 |
| 47 | $03 / 07 / 96$ | 53.1250 | -0.00235019 | 0.00003183 |

(Table continued on next page)

Table 13.2
Volatility Using Daily Data (Continued)

| No. | Date | Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 48 | 03/08/96 | 53.5000 | 0.00703397 | 0.00001401 |
| 49 | 03/11/96 | 55.2500 | 0.03218666 | 0.00083493 |
| 50 | 03/12/96 | 54.8750 | -0.00681049 | 0.00010205 |
| 51 | 03/13/96 | 56.1250 | 0.02252334 | 0.00036986 |
| 52 | 03/14/96 | 56.1250 | 0.00000000 | 0.00001083 |
| 53 | 03/15/96 | 58.8750 | 0.04783505 | 0.00198412 |
| 54 | 03/18/96 | 59.5000 | 0.01055973 | 0.00005283 |
| 55 | 03/19/96 | 58.7500 | -0.01268521 | 0.00025526 |
| 56 | 03/20/96 | 55.5000 | -0.05690816 | 0.00362401 |
| 57 | 03/21/96 | 55.8750 | 0.00673394 | 0.00001185 |
| 58 | 03/22/96 | 56.1250 | 0.00446427 | 0.00000138 |
| 59 | 03/25/96 | 54.8970 | -0.02212261 | 0.00064588 |
| 60 | 03/26/96 | 56.1250 | 0.02212263 | 0.00035461 |
| 61 | 03/27/96 | 56.6250 | 0.00886917 | 0.00003111 |
| 62 | 03/28/96 | 56.3750 | -0.00442487 | 0.00005954 |
| 63 | 03/29/96 | 56.8750 | 0.00883005 | 0.00003067 |
| 64 | 04/01/96 | 57.1250 | 0.00438585 | 0.00000120 |
| 65 | 04/02/96 | 56.8750 | -0.00438592 | 0.00005894 |
| 66 | 04/03/96 | 57.6250 | 0.01310063 | 0.00009622 |


| 67 | 04/04/96 | 59.2500 | 0.02780907 | 0.00060111 |
| :---: | :---: | :---: | :---: | :---: |
| 68 | 04/08/96 | 60.6250 | 0.02294148 | 0.00038612 |
| 69 | 04/09/96 | 61.8750 | 0.02040881 | 0.00029300 |
| 70 | 04/10/96 | 61.7500 | -0.00202225 | 0.00002824 |
| 71 | 04/11/96 | 60.4410 | -0.02142628 | 0.00061097 |
| 72 | 04/12/96 | 59.6250 | -0.01359277 | 0.00028508 |
| 73 | 04/15/96 | 60.5610 | 0.01557609 | 0.00015091 |
| 74 | 04/16/96 | 64.8750 | 0.06881123 | 0.00429282 |
| 75 | 04/17/96 | 64.1990 | -0.01047476 | 0.00018951 |
| 76 | 04/18/96 | 65.7500 | 0.02387206 | 0.00042356 |
| 77 | 04/19/96 | 65.2500 | -0.00763363 | 0.00011936 |
| 78 | 04/22/96 | 67.7500 | 0.03759836 | 0.00117695 |
| 79 | 04/23/96 | 68.1160 | 0.00538757 | 0.00000439 |
| 80 | 04/24/96 | 70.2500 | 0.03084814 | 0.00075936 |
| 81 | 04/25/96 | 69.6250 | -0.00893661 | 0.00014953 |
| 82 | 04/26/96 | 69.2500 | -0.00540056 | 0.00007555 |
| 83 | 04/29/96 | 68.1250 | -0.01637886 | 0.00038693 |
| 84 | 04/30/96 | 67.7500 | -0.00551984 | 0.00007764 |
| 85 | 05/01/96 | 67.8750 | 0.00184326 | 0.00000210 |
| 86 | 05/02/96 | 68.0000 | 0.00183987 | 0.00000211 |
| 87 | 05/03/96 | 68.6990 | 0.01022698 | 0.00004810 |
| 88 | 05/06/96 | 68.7500 | 0.00074210 | 0.00000650 |


| 89 | $05 / 07 / 96$ | 67.8750 | -0.01280893 | 0.00025923 |
| :--- | :--- | :--- | :--- | :--- |
| 90 | $05 / 08 / 96$ | 68.7500 | 0.01280883 | 0.00009058 |
| 91 | $05 / 09 / 96$ | 68.6250 | -0.00181983 | 0.00002613 |
| 92 | $05 / 10 / 96$ | 69.1250 | 0.00725946 | 0.00001574 |
| 93 | $05 / 13 / 96$ | 71.7500 | 0.03727144 | 0.00115463 |
| 94 | $05 / 14 / 96$ | 72.8750 | 0.01555783 | 0.00015046 |
| 95 | $05 / 15 / 96$ | 72.3750 | -0.00688472 | 0.00010356 |

(Table continued on next page)

Table 13.2
Volatility Using Daily Data (Continued)

| No. | Date | Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 96 | 05/16/96 | 71.8750 | -0.00693248 | 0.00010453 |
| 97 | 05/17/96 | 71.1250 | -0.01048963 | 0.00018992 |
| 98 | 05/20/96 | 71.0000 | -0.00175902 | 0.00002551 |
| 99 | 05/21/96 | 70.2500 | -0.01061962 | 0.00019352 |
| 100 | 05/22/96 | 69.8750 | -0.00535237 | 0.00007472 |
| 101 | 05/23/96 | 70.8750 | 0.01420985 | 0.00011921 |
| 102 | 05/24/96 | 71.0000 | 0.00176208 | 0.00000234 |
| 103 | 05/28/96 | 72.5000 | 0.02090661 | 0.00031029 |
| 104 | 05/29/96 | 71.3750 | -0.01563887 | 0.00035836 |
| 105 | 05/30/96 | 71.5000 | 0.00174968 | 0.00000238 |
| 106 | 05/31/96 | 75.5000 | 0.05443530 | 0.00261568 |
| 107 | 06/03/96 | 76.6250 | 0.01479070 | 0.00013223 |
| 108 | 06/04/96 | 76.3180 | -0.00401453 | 0.00005338 |
| 109 | 06/05/96 | 76.8750 | 0.00727182 | 0.00001584 |
| 110 | 06/06/96 | 75.2500 | -0.02136484 | 0.00060794 |
| 111 | 06/07/96 | 75.2500 | 0.00000000 | 0.00001083 |
| 112 | 06/10/96 | 74.1250 | -0.01506305 | 0.00033689 |
| 113 | 06/11/96 | 75.2500 | 0.01506296 | 0.00013857 |
| 114 | 06/12/96 | 76.7500 | 0.01973740 | 0.00027046 |


| 115 | 06/13/96 | 75.0000 | -0.02306526 | 0.00069468 |
| :---: | :---: | :---: | :---: | :---: |
| 116 | 06/14/96 | 73.0000 | -0.02702871 | 0.00091932 |
| 117 | 06/17/96 | 72.0000 | -0.01379335 | 0.00029190 |
| 118 | 06/18/96 | 70.3750 | -0.02282802 | 0.00068223 |
| 119 | 06/19/96 | 71.3750 | 0.01410962 | 0.00011703 |
| 120 | 06/20/96 | 71.1250 | -0.00350876 | 0.00004624 |
| 121 | 06/21/96 | 71.3750 | 0.00350866 | 0.00000005 |
| 122 | 06/24/96 | 73.6150 | 0.03090107 | 0.00076228 |
| 123 | 06/25/96 | 72.8750 | -0.01010310 | 0.00017942 |
| 124 | 06/26/96 | 72.5000 | -0.00515908 | 0.00007141 |
| 125 | 06/27/96 | 73.8750 | 0.01878786 | 0.00024013 |
| 126 | 06/28/96 | 73.4440 | -0.00585131 | 0.00008359 |
| 127 | 07/01/96 | 75.1250 | 0.02263005 | 0.00037398 |
| 128 | 07/02/96 | 74.7500 | -0.00500424 | 0.00006882 |
| 129 | 07/03/96 | 74.8750 | 0.00167085 | 0.00000263 |
| 130 | 07/05/96 | 72.1250 | -0.03741931 | 0.00165738 |
| 131 | 07/08/96 | 73.0000 | 0.01205855 | 0.00007686 |
| 132 | 07/09/96 | 73.3750 | 0.00512378 | 0.00000336 |
| 133 | 07/10/96 | 72.8750 | -0.00683764 | 0.00010260 |
| 134 | 07/11/96 | 69.5000 | -0.04741887 | 0.00257155 |
| 135 | 07/12/96 | 71.2500 | 0.02486799 | 0.00046554 |
| 136 | 07/15/96 | 69.3125 | -0.02756957 | 0.00095241 |


| 137 | $07 / 16 / 96$ | 70.0000 | 0.00986982 | 0.00004327 |
| :--- | :--- | :--- | :--- | :--- |
| 138 | $07 / 17 / 96$ | 71.6250 | 0.02294896 | 0.00038641 |
| 139 | $07 / 18 / 96$ | 72.5000 | 0.01214242 | 0.00007834 |
| 140 | $07 / 19 / 96$ | 72.8750 | 0.00515902 | 0.00000349 |
| 141 | $07 / 22 / 96$ | 72.1875 | -0.00947882 | 0.00016308 |
| 142 | $07 / 23 / 96$ | 69.5000 | -0.03794018 | 0.00170006 |
| 143 | $07 / 24 / 96$ | 69.0000 | -0.00722029 | 0.00011050 |

(Table continued on next page)

Table 13.2
Volatility Using Daily Data (Continued)

| No. | Date | Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 144 | 07/25/96 | 72.1250 | 0.04429425 | 0.00168122 |
| 145 | 07/26/96 | 74.2500 | 0.02903695 | 0.00066282 |
| 146 | 07/29/96 | 72.8750 | -0.01869210 | 0.00048328 |
| 147 | 07/30/96 | 74.3750 | 0.02037414 | 0.00029181 |
| 148 | 07/31/96 | 75.1250 | 0.01003346 | 0.00004545 |
| 149 | 08/01/96 | 77.0000 | 0.02465196 | 0.00045627 |
| 150 | 08/02/96 | 78.8125 | 0.02326614 | 0.00039898 |
| 151 | 08/05/96 | 78.1250 | -0.00876157 | 0.00014528 |
| 152 | 08/06/96 | 79.8750 | 0.02215279 | 0.00035574 |
| 153 | 08/07/96 | 82.3750 | 0.03081898 | 0.00075776 |
| 154 | 08/08/96 | 80.7500 | -0.01992406 | 0.00053897 |
| 155 | 08/09/96 | 82.3750 | 0.01992394 | 0.00027663 |
| 156 | 08/12/96 | 82.1250 | -0.00303949 | 0.00004008 |
| 157 | 08/13/96 | 80.2500 | -0.02309571 | 0.00069629 |
| 158 | 08/14/96 | 81.7500 | 0.01851890 | 0.00023187 |
| 159 | 08/15/96 | 81.7500 | 0.00000000 | 0.00001083 |
| 160 | 08/16/96 | 81.0000 | -0.00921662 | 0.00015646 |
| 161 | 08/19/96 | 80.7500 | -0.00309128 | 0.00004074 |
| 162 | 08/20/96 | 79.5000 | -0.01560093 | 0.00035693 |


| 163 | $08 / 21 / 96$ | 80.2500 | 0.00938974 | 0.00003719 |
| :--- | :--- | :--- | :--- | :--- |
| 164 | $08 / 22 / 96$ | 83.0000 | 0.03369383 | 0.00092430 |
| 165 | $08 / 23 / 96$ | 81.6250 | -0.01670502 | 0.00039986 |
| 166 | $08 / 26 / 96$ | 81.2500 | -0.00460480 | 0.00006235 |
| 167 | $08 / 27 / 96$ | 81.5000 | 0.00307200 | 0.00000005 |
| 168 | $08 / 28 / 96$ | 81.2500 | -0.00307221 | 0.00004050 |
| 169 | $08 / 29 / 96$ | 81.3750 | 0.00153736 | 0.00000308 |
| 170 | $09 / 30 / 96$ | 79.8125 | -0.01938798 | 0.00051436 |
| 171 | $09 / 03 / 96$ | 81.6250 | 0.02245546 | 0.00036725 |
| 172 | $09 / 04 / 96$ | 82.2500 | 0.00762774 | 0.00001880 |
| 173 | $09 / 05 / 96$ | 80.6250 | $0.09 / 96$ | $89 / 96$ |


| 185 | $09 / 23 / 96$ | 95.7500 | -0.01682891 | 0.00040483 |
| :--- | :--- | :--- | :--- | :--- |
| 186 | $09 / 24 / 96$ | 96.5000 | 0.00780230 | 0.00002035 |
| 187 | $09 / 25 / 96$ | 97.2500 | 0.00774186 | 0.00001980 |
| 188 | $09 / 26 / 96$ | 97.3750 | 0.00128448 | 0.00000403 |
| 189 | $09 / 27 / 96$ | 96.8750 | -0.00514801 | 0.00007123 |
| 190 | $09 / 30 / 96$ | 95.4375 | -0.01494988 | 0.00033275 |
| 191 | $10 / 01 / 96$ | 95.7500 | 0.00326899 | 0.00000000 |

(Table continued on next page)

Table 13.2
Volatility Using Daily Data (Continued)

| No | Date | Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 192 | 10/02/96 | 99.0000 | 0.03337913 | 0.00090526 |
| 193 | 10/03/96 | 99.5000 | 0.00503784 | 0.00000305 |
| 194 | 10/04/96 | 101.6875 | 0.02174674 | 0.00034059 |
| 195 | 10/07/96 | 104.6250 | 0.02847808 | 0.00063436 |
| 196 | 10/08/96 | 101.6250 | -0.02909297 | 0.00104876 |
| 197 | 10/09/96 | 100.7500 | -0.00864733 | 0.00014254 |
| 198 | 10/10/96 | 99.8750 | -0.00872283 | 0.00014435 |
| 199 | 10/11/96 | 105.3750 | 0.05360598 | 0.00253154 |
| 200 | 10/14/96 | 107.6250 | 0.02112752 | 0.00031812 |
| 201 | 10/15/96 | 111.1250 | 0.03200273 | 0.00082433 |
| 202 | 10/16/96 | 112.6250 | 0.01340797 | 0.00010234 |
| 203 | 10/17/96 | 110.7500 | -0.01678830 | 0.00040320 |
| 204 | 10/18/96 | 110.0000 | -0.00679503 | 0.00010174 |
| 205 | 10/21/96 | 107.7500 | -0.02066660 | 0.00057399 |
| 206 | 10/22/96 | 105.5000 | -0.02110277 | 0.00059509 |
| 207 | 10/23/96 | 109.3750 | 0.03607128 | 0.00107451 |
| 208 | 10/24/96 | 107.5000 | -0.01729146 | 0.00042366 |
| 209 | 10/25/96 | 105.3750 | -0.01996551 | 0.00054089 |
| 210 | 10/28/96 | 106.0000 | 0.00591351 | 0.00000687 |


| 211 | 10/29/96 | 104.3750 | -0.01544894 | 0.00035121 |
| :---: | :---: | :---: | :---: | :---: |
| 212 | 10/30/96 | 106.7500 | 0.02249946 | 0.00036894 |
| 213 | 10/31/96 | 109.8750 | 0.02885363 | 0.00065342 |
| 214 | 11/01/96 | 108.7500 | -0.01029165 | 0.00018450 |
| 215 | 11/04/96 | 110.2500 | 0.01369871 | 0.00010831 |
| 216 | 11/05/96 | 114.0000 | 0.03344792 | 0.00090940 |
| 217 | 11/06/96 | 118.8750 | 0.04187399 | 0.00148860 |
| 218 | 11/07/96 | 122.1250 | 0.02697261 | 0.00056079 |
| 219 | 11/08/96 | 122.2500 | 0.00102295 | 0.00000515 |
| 220 | 11/11/96 | 123.8750 | 0.01320474 | 0.00009827 |
| 221 | 11/12/96 | 121.0000 | -0.02348241 | 0.00071685 |
| 222 | 11/13/96 | 119.5000 | -0.01247422 | 0.00024856 |
| 223 | 11/14/96 | 119.8750 | 0.00313298 | 0.00000003 |
| 224 | 11/15/96 | 115.8750 | -0.03393756 | 0.00138601 |
| 225 | 11/18/96 | 115.3750 | -0.00432437 | 0.00005800 |
| 226 | 11/19/96 | 120.7500 | 0.04553452 | 0.00178446 |
| 227 | 11/20/96 | 120.8750 | 0.00103460 | 0.00000509 |
| 228 | 11/21/96 | 118.8750 | -0.01668446 | 0.00039904 |
| 229 | 11/22/96 | 122.3750 | 0.02901749 | 0.00066182 |
| 230 | 11/25/96 | 121.5000 | -0.00717588 | 0.00010957 |
| 231 | 11/26/96 | 123.7500 | 0.01834914 | 0.00022673 |
| 232 | 11/27/96 | 126.6250 | 0.02296656 | 0.00038710 |


| 233 | $11 / 29 / 96$ | 126.8750 | 0.00197237 | 0.00000174 |
| :--- | :--- | :--- | :--- | :--- |
| 234 | $12 / 02 / 96$ | 127.1250 | 0.00196844 | 0.00000175 |
| 235 | $12 / 03 / 96$ | 125.8750 | -0.00988153 | 0.00017353 |
| 236 | $12 / 04 / 96$ | 129.5000 | 0.02839157 | 0.00063001 |
| 237 | $12 / 05 / 96$ | 128.2500 | -0.00969939 | 0.00016877 |
| 238 | $12 / 06 / 96$ | 125.6875 | -0.02018281 | 0.00055105 |
| 239 | $12 / 09 / 96$ | 130.1250 | 0.03469686 | 0.00098629 |

(Table continued on next page)

Table 13.2
Volatility Using Daily Data (Continued)

| No. | Date | Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 240 | 12/10/96 | 129.1250 | -0.00771466 | 0.00012114 |
| 241 | 12/11/96 | 136.8750 | 0.05828716 | 0.00302451 |
| 242 | 12/12/96 | 136.8750 | 0.00000000 | 0.00001083 |
| 243 | 12/13/96 | 132.3750 | -0.03342930 | 0.00134842 |
| 244 | 12/16/96 | 127.2500 | -0.03948517 | 0.00182985 |
| 245 | 12/17/96 | 130.0000 | 0.02138065 | 0.00032721 |
| 246 | 12/18/96 | 135.7500 | 0.04328051 | 0.00159911 |
| 247 | 12/19/96 | 137.5000 | 0.01280883 | 0.00009058 |
| 248 | 12/20/96 | 134.6250 | -0.02113080 | 0.00059645 |
| 249 | 12/23/96 | 132.2500 | -0.01779908 | 0.00044482 |
| 250 | 12/24/96 | 135.5000 | 0.02427748 | 0.00044041 |
| 251 | 12/26/96 | 136.6250 | 0.00826816 | 0.00002477 |
| 252 | 12/27/96 | 135.3750 | -0.00919126 | 0.00015582 |
| 253 | 12/30/96 | 133.2500 | -0.01582163 | 0.00036532 |
| 254 | 12/31/96 | 130.9375 | -0.01750696 | 0.00043258 |
|  | Totals |  | 0.83605590 | 0.12709460 |

The mean value of the price ratios in Table 13.2 is:
$\mu=0.83606383 / 254=\ln (130.9375 / 56.75) / 254=0.003292$
The variance is: $\operatorname{var}=0.12709460 / 253=0.0050235$

The standard deviation is $\sigma=\sqrt{\text { var }}=0.0224132$
The annualized volatility is $v=\sqrt{254} \times \sigma$
The difference in the estimated annualized volatility brought about by using daily versus monthly data is seen to be significant and is the result of an insufficient sample size when monthly data are used.

The next step in the procedure is to calculate the value of the normal distribution. Although it is possible to use tables and interpolation to arrive at values of $\mathrm{N}(\mathrm{x})$, it is often easier to use some sort of curve-fitting formula. There are many such formulas to choose from, depending on whether the fit between the approximation and the exact distribution is to be more precise in the central or the outlying portions (the tails) of the normal distribution. A commonly used approximation for the normal distribution is given by Equations 13.9 through 13.11.

If $z \geq 0$, then let
$f(z)=\frac{e^{-z^{2} / 2}}{\sqrt{2 \pi}}$

$$
\begin{equation*}
g(z)=\frac{1}{(1+0.33267 z)} \tag{13.10}
\end{equation*}
$$

Then:

$$
\begin{aligned}
& \mathrm{N}(z)=\int_{-\infty}^{z} \frac{e^{-x^{2 / 2}} d x}{\sqrt{2 \pi}} \\
& \quad \approx 1-f(z) \times\left[0.4361836 g(z)-0.1201676 g^{2}(z)+0.9372980 g^{3}(z)\right]
\end{aligned}
$$

$$
\begin{equation*}
\text { If } z<0 \text {, then } N(z)=1-N(z) \text {. } \tag{13.11}
\end{equation*}
$$

## Stock Growth and Volatility

As mentioned earlier, long-term growth prospects in the earnings and in the corresponding stock price ordinarily have no effect on the price of a put or call option. This remarkable fact was noted by Cox and Rubenstein in their monumental book on option markets. Little emphasis was placed on this phenomenon, however, because of the relatively short expiration dates that existed on options at the time. To see why this must be the case, let's first consider a numerical example. It will be the first one examined in this chapter where I will allow prices to rise at an additional 1 percent a month. The results appear in Table 13.3.

The mean value of the price ratios in Table 13.3 is:
$\mu=0.95546772 / 12=\ln (147.5436 / 56.75) / 12=0.07962231$
The variance is: $\operatorname{var}=0.06833014 / 11=0.006212$
The standard deviation is $\sigma=\sqrt{\text { var }}=0.078815$
The annualized volatility is: $v=\sqrt{254} \times \sigma=0.273023$
Because the volatility is the same as before, the put and call premiums for the same stock and exercise prices, expiration date, and risk-free interest rate are therefore unchanged.

In general, suppose the growth-adjusted prices are given by $q_{i}=p_{i} \times(1+f)^{i}$, where $f$ is the daily, monthly or annual inflation rate. The adjusted logarithmic change ratios are $x_{i}^{\prime}=\ln$ $\left(q_{i} / q_{i-1}\right)={ }_{\text {ln }}(1+f)+$

Table 13.3
Volatility Using Monthly Data as Inflated

| No. | Date | Original Price | Adjusted Price | $x_{i}=\ln \left(p_{i} / p_{i-1}\right)$ | $\left(x_{i}-\mu\right)^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 12/29/95 | 56.7500 | 56.7500 | - | - |
| 1 | 01/31/96 | 55.2380 | 55.7904 | -0.01705427 | 0.0093464 |
| 2 | 02/29/96 | 58.8170 | 59.9992 | 0.07273010 | 0.0000475 |
| 3 | 03/29/96 | 56.8750 | 58.5984 | -0.02362479 | 0.0106600 |
| 4 | 04/30/96 | 67.7500 | 70.5009 | 0.18491890 | 0.0110874 |
| 5 | 05/31/96 | 75.5000 | 79.3513 | 0.11825850 | 0.0014928 |
| 6 | 06/28/96 | 73.4440 | 77.9623 | -0.01765920 | 0.0094637 |
| 7 | 07/31/96 | 75.1250 | 80.5442 | 0.03258051 | 0.0022129 |
| 8 | 08/30/96 | 79.8125 | 86.4255 | 0.07047696 | 0.0000836 |
| 9 | 09/30/96 | 95.4375 | 104.3786 | 0.18874160 | 0.0119070 |
| 10 | 10/31/96 | 109.8750 | 121.3704 | 0.15082210 | 0.0050694 |
| 11 | 11/29/96 | 126.8750 | 141.5504 | 0.15380920 | 0.0055037 |
| 12 | 12/31/96 | 130.9375 | 147.5436 | 0.04146811 | 0.0014557 |
|  | Totals |  |  | 0.95546772 | 0.0683301 |

$\ln \left(p_{i} / p_{i-1}\right)=\ln (1+f)+x_{i}$, where $x_{i}$ are the unadjusted ratios. The growth-adjusted mean ratio $\mu^{\prime}$ is therefore equal to $\mu+\ln (1+f)$, where g is the unadjusted mean. As a result, each of the differences $x_{i}^{\prime}-\mu^{\prime}$ is equal to $x_{i}-\mu$, from which it follows that the variance, standard deviation, and volatility for the growth-adjusted situation are the same as for the unadjusted case.

## Stock Growth and In-the-Money Probabilities

As has just been demonstrated, the effect of earnings growth on stock price is ordinarily not reflected in option premiums. Earnings growth must, however, affect the chances that a given put or call will wind up in or out of the money. This effect was ignored in the past because of the relatively short durations of standard options. When it comes to LEAPS, the effect of earnings growth can be significant because of expiration up to two and a half years away. If we denote the annual growth rate in the stock price $\alpha$, by the expected stock price at expiration is going to be $P_{e} \alpha$. If this term is used instead of the stock price at the inception of the option, the formula for $h$ in Equation 13.1 becomes:
$h=\frac{\ln (P / S)+\left(r-\delta+\alpha+v^{2} / 2\right) \times t}{v \sqrt{t}}$

So let's go back to the original example of an at-the-money LEAP put for which this time the formula for $-h_{+} v \sqrt{t}$ is given by:
$-h+v \sqrt{t}=\left(0.5 \times v^{2}+\delta-r-\alpha\right) \times\left(\frac{\sqrt{t}}{v}\right)$
Equation 13.13 shows that other things being equal, the higher the growth rate, the less likely it is that a LEAP put will wind up in the money. For the specific case where the volatility is 0.3 , the risk-free interest rate $r$ is 6 percent, and the annualized dividend rate $\delta$ is 1.5 percent, the expression for $-h+v \sqrt{t}$ becomes $-\alpha \times \sqrt{t} / 0.30$. For a growth rate of a modest 10 percent per year, and an expiration date 2.5 years away, $-h+v \sqrt{t}$ is -0.527 , for which the integral in either Equation 13.2 or Equation 13.3 is almost exactly 0.300 . Thus, the chance of such an at-the-money put (or call) winding up in the money at expiration under these circumstances is just 30 percent, substantially less than the 50 percent probability of winding up in the money had the growth rate not been taken into account.

As mentioned earlier, Appendix C contains a list of tables showing the probability of LEAP puts winding up in the money for a wide range of parameters. Of particular interest is the fact that the tables illustrate these probabilities for the five independent growth rates of zero, 5 percent, 10 percent, 15 percent, and 20 percent. It is thus possible to see the effect that earnings growth will have on LEAP puts that were initially out of the money, at the money, or even in the money.

## 14-

## Option Premiums

## Introduction

As important as knowing the chances of a LEAP put winding up in the money is knowing whether the option in question is over- or underpriced. When it comes to longterm options, market makers use one of several analytic formulas to calculate option prices. This is because the computational complexity associated with multiperiod binomial models increases dramatically with the number of steps involved, thus restricting their applicability to standard, short-term option pricing.

Depending on the sophistication of the market maker, option pricing is typically determined either by straightforward use of the original pricing formula developed by Fischer Black and Myron Scholes in 1973 or by the use of later extensions of this formula by Robert Merton, Giovanni Barone-Adesi, and Robert Whaley. In a nutshell, the Black-Scholes model determines option prices for European-style options (which can be exercised only at expiration and not before), ignoring the effects of dividends. The Merton model adjusts the Black-Scholes formula to take dividends into account (again for European-style options); the Barone-Adesi and Whaley model adjusts the Black-Scholes-Merton formula for the early exercise potential present in American-style options. This chapter shows how to use the basic Black-Scholes and Merton models to determine option prices.

## The Black-Scholes Formula for Puts

The Black-Scholes formula for the put premium for European-style options with a zero dividend rate is given by:

$$
\begin{equation*}
\text { Put }=-P \times \int_{-\infty}^{-h} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x+S \times e^{-\pi} \times \int_{-\infty}^{-h+v \sqrt{t}} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x \tag{14.1}
\end{equation*}
$$

where:
$P$ is the price of the underlying issue
$S$ is the strike (exercise price) of the option
$r$ is the risk-free interest rate in decimal form
$t$ is the time in years till expiration
$v$ is the annualized volatility in decimal form
and $h$ is given by the formula:
$h=\frac{\ln (P / S)+\left(r+v^{2} / 2\right) \times t}{v \sqrt{t}}$
When $t$ approaches zero in Equation 14.2, $h$ takes on one of two values:

1. ${ }^{h} \rightarrow+\infty$ if the stock price $P$ equals or is greater than the strike price $S$
2. $h \rightarrow-\infty$ if $P$ is less than $S$,
the result of which shows that the value of the put goes to zero if $P$ equals or is greater than $S$, or it approaches $S-P$ if $P$ is less than $S$.

The integrals in Equation 14.1 are the standard normal distribution, and the same curvefitting formula that was used in the previous chapter can be used for their evaluation. Note that the right-hand integral is the probability that the put will wind up in the money.

## The Black-Scholes Formula for Calls

For completeness, the corresponding Black-Scholes formula for the call premium is given by:

Call $=P \times \int_{-\infty}^{h} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x-S \times e^{-r t} \times \int_{-\infty}^{h-r \sqrt{t}} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x$
where $P, S, r, t$, and $h$ are as defined earlier for the put formula. If the put price has already been calculated, one can use the shortcut formula (called the put-call parity formula) for the call, as follows:

Call $=P u t+P-S_{\times} e^{-r t}$

## The Effect of Dividends on Option Premiums

To keep things simple and conservative, all put premiums used in conducting the tenyear economic simulations were calculated using a zero dividend rate. The effect of dividends is to lower the price of calls and to increase the price of puts. If I were to assume that dividends were paid continuously through the year (rather than in the usual quarterly distribution), the Merton variation of the Black-Scholes pricing formula can be used. This formula takes the following form for puts:

Put $=-P \times e^{-\alpha} \times \int_{-\infty}^{-h} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x+S \times e^{-n} \times \int_{-\infty}^{-h+v \sqrt{\hbar}} \frac{e^{-x^{2} / 2}}{\sqrt{2 \pi}} d x$
where
$\delta$ is the annual dividend rate, and $h$ is modified as follows:

$$
\begin{equation*}
h=\frac{\ln (P / S)+\left(r-\delta+v^{2} / 2\right) \times t}{v \sqrt{t}} \tag{14.6}
\end{equation*}
$$

The right-hand integral is again the probability that the put will wind up in the money and is the one adopted for that purpose in the previous chapter.

## Numerical Example

To illustrate the effect that dividends have on option premiums, consider the case where the strike price and stock price are both $\$ 100$, the volatility is 0.35 , the risk-free interest rate is 6 percent, there are 24 months till expiration, and the annual dividend rate is 2 percent. Applying the basic Black-Scholes formula yields a put premium for the zerodividend case of $\$ 13.314$. This was the figure shown in Table 1.2 back in Chapter 1. For the Merton variation, do the following:

Since $S=P=\$ 100$, the parameter $h$ in Equation 14.6 is calculated as
$h=\frac{[0.06-0.02+0.5 \times 0.35 \times 0.35] \times(24 / 12)}{0.35 \times \sqrt{(24 / 12)}}=\frac{0.2025}{0.4949748}=0.409112$
Therefore, $-h$ is -0.409112 , and $-h+v \sqrt{t}$ is $-0.409112+0.4949748$, or 0.0858628 . From tables of the normal distribution or through the use of the curve-fitting formulas in Equations 13.9 through 13.11, we have $\mathrm{N}(-0.409112)=1-\mathrm{N}(0.409112)=0.341238$ and $\mathrm{N}(0.0858628)=0.534223$. When the time to expiration is 2 years, $e^{-0.02 t}$ is 0.960790 and $e^{-0.06 t}$ is 0.886920 . So from Equation 14.5 the European put with its 2 percent annual dividend rate is calculated as

$$
\begin{aligned}
\text { European Put } & =-\$ 100 \times 0.960790 \times 0.341238 \\
& +\$ 100 \times 0.886920 \times 0.534223 \\
& =-\$ 32.785+\$ 47.381=\$ 14.596
\end{aligned}
$$

Thus, the annual 2 percent dividend has increased the price of the put by about $\$ 1.28$ over the two-year period involved, thus showing that the effect of dividends on option pricing can indeed be significant.

The pricing of American options is so complex that market makers often restrict their pricing formulas to that of Black-Scholes or one of its simpler variations. Appendix A contains tables for the prices of European-style LEAP puts with zero dividend rates. The pricing of American-style options is examined in the next chapter.

## Implied Volatility

Now that you've seen how to calculate the LEAP put premium for European-style options using the Black-Scholes-Merton formulas, the question arises as to whether one can work the process backwards and determine volatility if the premium is supplied. The answer to this question is both yes and no.

To begin, I first note that it is not possible to invert Equation 14.1 or Equation 14.5 to solve for the volatility directly. However, the volatility can be determined on a trial-anderror basis using a Newton-Raphson iterative search technique. A relatively short BASIC program for doing this follows. It is then illustrated by two numerical examples.

```
10 'SOLVE FOR IMPLIED VOLATILITY
20 INPUT "Enter Stock Price: ";P
30 INPUT "Enter Strike Price: ";S
40 INPUT "Enter Risk-Free Interest Rate (e.g., .06): ";R
5 0 ~ I N P U T ~ " E n t e r ~ A n n u a l ~ D i v i d e n d ~ R a t e ~ ( e . g . , ~ . 0 2 ) : ~ " ; D I V ~
6 0 ~ I N P U T ~ " E n t e r ~ T i m e ~ t o ~ E x p i r a t i o n ~ i n ~ M o n t h s ~ ( 0 ~ f o r ~ d a y s ) : ~ " ; T I M E X ~
7 0 ~ I N P U T ~ " E n t e r ~ P u t ~ P r e m i u m : ~ " ; P R E M I U M ~
80 IF TIMEXO THEN T=TIMEX/12: GOTO 120
90 INPUT "Enter Time to Expiration in Days: ";TIMEXX
100 T=TIMEXX/365
1 1 0
120 PRINT "Where do you want to send results: "
130 PRINT "1 = Screen"
140 PRINT "2 = Printer"
150 PRINT "3 = Save to disk"
160 INPUT "Enter your selection: ";SELECT
170 IF SELECT=0 THEN SELECT =1
180 IF SELECT=1 THEN SAVEFILE$="SCRN:"
190 IF SELECT=2 THEN SAVEFILE$="LPT1:"
200 IF SELECT=3 THEN INPUT "Enter name of savefile: ";SAVEFILE$
2 1 0 ~ O P E N ~ S A V E F I L E \$ ~ F O R ~ O U T P U T ~ A S ~ 1 ~
220 PRINT#1, "Stock Price: ";P
230 PRINT#1, "Strike Price: ";S
240 PRINT#1, "Risk-Free Interest Rate (e.g., .06): ";R
250 PRINT#1, "Annual Dividend Rate (e.g., .02): ";DIV
260 IF TIMEX>0 THEN PRINT#1, "Time to Expiration in Months: ";TIMEX
2 7 0 ~ I F ~ T I M E X X > 0 ~ T H E N ~ P R I N T \# 1 , ~ " T i m e ~ t o ~ E x p i r a t i o n ~ i n ~ D a y s : ~ " ; T I M E X X ~
280 PRINT#1, "Put Premium: ";PREMIUM
290
3 0 0 ~ ' C O M P U T E ~ B A S I C ~ P A R A M E T E R S ~
310 ERT=EXP(-R*T)
320 EDT=EXP(-DIV*T)
```

```
330 PI2=SQR(2*3.14159265#)
340 SQT=SQR(T)
350 '*****************************************************
3 6 0 ~ ' S T A R T ~ T R I A L ~ A N D ~ E R R O R ~ S E A R C H ~ F O R ~ V O L A T I L I T Y ~
370 'USING NEWTON-RAPHSON ITERATION PROCESS
380 VOLD=.5 'first guess is . }
3 9 0 ~ K O U N T = 1 ~ ' s e t ~ i t e r a t i o n ~ c o u n t e r ~
400 H=(LOG(P/S)+(R-DIV+VOLD*VOLD/2)*T)/(VOLD*SQT)
4 1 0 ~ H 1 = - H ~ ' n e g a t i v e ~ h ~
420 PH=EXP(-H1*H1/2!)/PI2
430 KH=1/(1+.33267*ABS(H1))
440 CUMH=1-PH*(.4361836*KH-.1201676*KH*KH+.937298*KH*KH*KH)
450 IF H1<<0 THEN CUMH=1-CUMH 'this is Normal(-h)
4 6 0 ~ G 1 = - H + V O L D * S Q T ~
470 GH=EXP(-G1*G1/2!)/PI2
480 KG=1/(1+.33267*ABS(G1))
490 CUMG=1-GH*(.4361836*KG-.1201676*KG*KG+.937298*KG*KG*KG)
40 IF H10 THEN CUMH=1-CUMH 'this is Normal(-h)
4 6 0 ~ G 1 = - H + V O L D * S Q T ~
470 GH=EXP(-G1*G1/2!)/PI2
480 KG=1/(1+.33267*ABS(G1))
490 CUMG=1-GH*(.4361836*KG-.1201676*KG*KG+.937298*KG*KG*KG)
500 IF G1<<0 THEN CUMG=1-CUMG 'this is Normal(-h+beta)
5 1 0 ~ P U T V A L = - P * E D T * C U M H + S * E R T * C U M G ~ ' p u t ~ V a l u e ~ a t ~ V = V O L D ~
520 F=-PREMIUM+PUTVAL 'function F at V=VOLD
5 3 0 \text { DERIVH=(H/VOLD)-SQT 'derivative of Normal(-h) at V=VOLD}
5 4 0 \text { DERIVG=H/VOLD 'derivative of Normal(-h+v*sqrt) at V=VOLD}
5 5 0 ~ D E R I V F = - P * E D T * C U M H * D E R I V H + S * E R T * C U M G * D E R I V G ~ ' d e r i v . ~ o f ~ F '
5 6 0 ~ V N E W = V O L D - F / D E R I V F ~ ' n e w ~ e s t i m a t e ~ f o r ~ v o l a t i l i t y ~
5 7 0 ~ ' * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * )
5 8 0 ~ ' D I S P L A Y ~ C O N V E R G E N C E ~ D E T A I L S ~ ( o p t i o n a l )
590 IF KOUNT=1 THEN 600 ELSE 620
600 PRINT#1, " "
610 PRINT#1, USING "\\\\\\ !";"No.","VOLD","VNEW","F"
620 PRINT#1, USING "## #.##### #.##### ###.####";KOUT,VOLD,VNEW,F
6 3 0
6 4 0
6 5 0
6 6 0
670 KF KOUNP<< 11 '
670 IF KOUNT << 11 THEN 400 'cut-off limit on iterations
6 8 0 ~ V O L = ( V N E W + V O L D ) / 2 ~ ' f i n a l ~ v a l u e ~ f o r ~ t h e ~ c r i t i c a l ~ s t o c k ~ p r i c e
6 9 0
7 0 0
7 1 0
7 2 0
7 3 0 \text { INPUT "Another Case (y/n): ";CASE\$}
7 4 0 ~ I F ~ C A S E \$ = " y " ~ O R ~ C A S E \$ = " Y " ~ T H E N ~ C L O S E ~ 1 : ~ G O T O ~ 2 0
7 5 0 ~ C L O S E ~ 1 ~
```

760 END

## Numerical Examples

As examples of the results obtainable using the computer program, consider the two cases investigated earlier:

Stock Price: \$100
Strike Price: $\$ 100$
Risk-Free Interest Rate (e.g., .06): . 06
Annual Dividend Rate (e.g., .02): 0
Time to Expiration in Months: 24
Put Premium: 13.314

| No. | VOLD | VNEW | F |
| :--- | :--- | :--- | :--- |
| 1 | 0.50000 | 0.38384 | 7.4605 |
| 2 | 0.38384 | 0.35707 | 1.6934 |
| 3 | 0.35707 | 0.35144 | 0.3544 |
| 4 | 0.35144 | 0.35029 | 0.0723 |
| 5 | 0.35029 | 0.35005 | 0.0147 |
| 6 | 0.35005 | 0.35001 | 0.0030 |

Implied Volatility: 0.35003
Stock Price: \$100
Strike Price: \$100
Risk-Free Interest Rate (e.g., .06): . 06
Annual Dividend Rate (e.g., .02): . 02
Time to Expiration in Months: 24
Put Premium: 14.596

| No | VOLD | VNEW | F |
| :--- | :--- | :--- | :--- |
| 1 | 0.50000 | 0.38456 | 7.3947 |
| 2 | 0.38456 | 0.35755 | 1.7191 |
| 3 | 0.35755 | 0.35163 | 0.3758 |
| 4 | 0.35163 | 0.35036 | 0.0808 |
| 5 | 0.35036 | 0.35008 | 0.0173 |
| 6 | 0.35008 | 0.35003 | 0.0037 |

Implied Volatility: 0.35005

At first blush, this numerical method for determining volatilities from premiums looks like a great shortcut to the laborious process of calculating them from historical price information. All one has to do is to obtain the premium quoted, say, for a LEAP put, and then use the computer program to determine the volatility. The trouble with this is that it is not ordinarily possible to determine what pricing model the market maker used in the first place to arrive at the option premium quoted. The market maker may have used Black-Scholes (thereby ignoring dividends), or the Merton variation (thereby including dividends), or a multiperiod binomial model, or even a more sophisticated model for the pricing of American-style options.

## 15-

## American-Style Options

## The Effect of American-Style Options

The ability to exercise early has no effect on the price of calls in the absence of dividends and only a moderate impact if dividends are taken into account. The principal difference between European- and American-style options occurs for put premiums. For American-style options, there is a significant upward effect on put premiums, whether or not dividends are present.

Unfortunately, there is no neat, concise, and exact formula for American-style put premiums. A good analytic approximation for these premiums is given by a formula developed by Giovanni Barone-Adesi and Robert Whaley, as follows:

$$
\begin{array}{rlrl}
\text { American Put } & =\text { European Put }+ \text { Early Exercise Premium, } & \text { if } P>P^{*} \\
& =S-P, & & \text { if } P \leq P^{*}
\end{array}
$$

where the European put premium is the one calculated using the Merton variation presented in the previous chapter, and $P^{*}$ is the critical stock price determined from the procedure outlined below.

The early exercise premium in Equation 15.1 is given by:
Early Exercise Premium $=A \times\left(\frac{P}{P^{*}}\right)^{Q}$ (15.2)
where:
$A=-\frac{P^{*} \times\left[1-e^{-\delta} \times N\left(-h^{*}\right)\right]}{Q}$
$Q=\frac{1-n-\sqrt{(n-1)^{2}+4 k}}{2}$
$n=\frac{2(r-\delta)}{v^{2}}$
$k=\frac{2 r}{v^{2}\left(1-e^{-r t}\right)}$
$\mathrm{N}\left(-h^{*}\right)$ again denotes the cumulative normal distribution function, where $h^{*}$ is the dividend adjusted parameter specified in the Merton variation, as evaluated at the critical stock price $P^{*}$.
$h^{*}=\frac{\ln \left(P^{*} / S\right)+\left(r-\delta+v^{2} / 2\right) \times t}{v \sqrt{t}}$
The critical stock price $P^{*}$ is the iterative solution to the following equation:
$S_{-} P^{*}=$ European Put $\left(P^{*}\right)-\left[1-e^{-\delta} \times N\left(-h^{*}\right)\right] \times\left(\frac{P^{*}}{Q}\right)$
where the European put premium in Equation 15.8 is evaluated at the critical stock price $P^{*}$.

## Numerical Example

I illustrate the use of the methodology with the same example used for the Merton variation in the previous chapter, in which the strike price and stock price are $\$ 100$, the volatility is 0.35 , the risk-free interest rate is 6 percent, there are 24 months till expiration, and the annual dividend rate is 2 percent. By trial and error, Equation 15.8 is satisfied when $P^{*}$ is $\$ 58.1844$ (a computer program showing how this is efficiently determined is included at the end of this chapter).

We then compute in order:

$$
\begin{aligned}
n & =\frac{2(r-\delta)}{v^{2}}=\frac{2 \times(0.06-0.02)}{0.35^{2}}=0.6530612 \\
k & =\frac{2 r}{v^{2}\left(1-e^{-n}\right)}=\frac{2 \times 0.06}{0.35^{2} \times\left(1-e^{-0.12}\right)}=8.662856 \\
Q & =\frac{1-n-\sqrt{(n-1)^{2}+4 k}}{2} \\
& =\frac{0.3469388-\sqrt{0.3469388^{2}+4 \times 8.662856}}{2}=-2.774911
\end{aligned}
$$

$$
h^{*}=\frac{\ln \left(P^{*} / S\right)+\left(r-\delta+v^{2} / 2\right) \times t}{v \sqrt{t}}
$$

$$
=\frac{\ln (58.1844 / 100)+\left(0.06-0.02+0.5 \times 0.35^{2}\right) \times 2}{0.35 \sqrt{2}}
$$

$$
=-0.6849906
$$

$\mathrm{N}\left(-h^{*}\right)=N(0.6849906)=0.7533173$

$$
\begin{aligned}
A & =-\frac{P^{*} \times\left[1-e^{-\delta} \times N\left(-h^{*}\right)\right]}{Q} \\
& =-\frac{58.1844 \times\left(1-e^{-0.04} \times 0.7533173\right)}{-2.774911}=5.791803
\end{aligned}
$$

Early Exercise Premium $=A \times\left(\frac{P}{P^{*}}\right)^{Q}$

$$
\begin{aligned}
& =5.791803 \times\left(\frac{100}{58.1844}\right)^{-2.774911} \\
& =1.288
\end{aligned}
$$

The American put premium with a 2 percent dividend rate is therefore its European put value of $\$ 14.596$ plus $\$ 1.288$, or $\$ 15.884$.

As mentioned earlier, the critical stock price $P^{*}=58.1844$ is determined by trial and error so as to satisfy Equation 15.8 . To verify that this is the case, we calculate the value of the European put premium using the Merton variation at that particular stock price, as follows:

$$
\begin{aligned}
\operatorname{Put}\left(P^{*}\right)= & -58.1844 \times e^{-0.04} \times N(0.6849906) \\
& +100 \times e^{-0.12} \times N(0.6849906+0.35 \sqrt{2}) \\
= & -58.1844 \times 0.9607894 \times 0.753317 \\
& +100 \times 0.8869204 \times 0.881003 \\
= & -42.1127+78.1380=36.0253
\end{aligned}
$$

The left-hand side of Equation 15.8 is given by:
$S_{-} P^{*}=100-58.1844=41.816$,
while the right-hand side of Equation 15.8 is calculated as:

$$
\begin{aligned}
S_{-} P^{*} & =36.0253-(1-0.9607894 \times 0.753317) \times\left(\frac{58.1844}{-2.774911}\right) \\
& =36.0253+5.7918=41.817
\end{aligned}
$$

Because the two values are identical (within computational round-off), the critical stock price of 58.1844 is confirmed.

Table 15.1
European vs. American Put Premiums

| Dividend Rate | European Put | American Put |
| :--- | :--- | :--- |
| $0 \%$ | 13.314 | 14.880 |
| 1 | 13.948 | 15.373 |
| 2 | 14.596 | 15.884 |
| 3 | 15.259 | 16.417 |

## Comparison Table

Table 15.1 compares European- and American-style put premiums where the strike price and stock price are $\$ 100$, the volatility is 0.35 , the risk-free interest rate is 6 percent, there are 24 months till expiration, and the annual dividend rate ranges from 0 percent to 3 percent.

As is clearly apparent, the premiums in all cases are greater than the one utilized for the zero-dividend, European-style case. Because of this, the premiums, retention rates, and account values shown in each run throughout this book would have been somewhat higher if actual dividends and early exercise fights were taken into account.

Appendix B contains detailed tables for the prices of American-style puts for a wide range of parameters.

## Computer Program for American Put Premiums

A relatively short BASIC program for calculating American put premiums follows. By using a Newton-Raphson iterative search technique, the critical stock price can usually be obtained to within three decimal places in just four or five iterations, as shown in the numerical example that follows the BASIC program.

```
10 'AMERICAN PUT PREMIUMS USING BARONE-ADESI AND WHALEY APPROACH
20 INPUT "Enter Stock Price";P
3 0 ~ I N P U T ~ " E n t e r ~ S t r i k e ~ P r i c e " ; S ~
40 INPUT "Enter Risk-Free Interest Rate (e.g., .06)";R
5 0 ~ I N P U T ~ " E n t e r ~ V o l a t i l i t y ~ ( e . g . , ~ 0 . 3 5 ) " ; S D ~
6 0 ~ I N P U T ~ " E n t e r ~ A n n u a l ~ D i v i d e n d ~ R a t e ~ ( e . g . , ~ . 0 2 ) " ; D I V ~
7 0 ~ I N P U T ~ " E n t e r ~ T i m e ~ t o ~ E x p i r a t i o n ~ i n ~ M o n t h s ~ ( 0 ~ f o r ~ d a y s ) " ; T I M E X ~
80 IF TIMEX>0 THEN T=TIMEX/12 GOTO 120
```

90 INPUT "Enter Time to Expiration in Days";TIMEXX
100 T=TIMEXX/365


```
120 PRINT "Where do you want to send results"
130 PRINT "1 = Screen"
140 PRINT "2 = Printer"
150 PRINT "3 = Save to disk"
160 INPUT "Enter your selection";SELECT
170 IF SELECT=0 THEN SELECT =1
180 IF SELECT=1 THEN SAVEFILE$="SCRN:"
190 IF SELECT=2 THEN SAVEFILE$="LPT1:"
200 IF SELECT=3 THEN INPUT "Enter name of savefile";SAVEFILE$
2 1 0 ~ O P E N ~ S A V E F I L E \$ ~ F O R ~ O U T P U T ~ A S ~ 1 ~
220 PRINT#1, "Stock Price";P
230 PRINT#1, "Strike Price";S
240 PRINT#1, "Risk-Free Interest Rate (e.g., .06)";R
250 PRINT#1, "Volatility (e.g., 0.35)";SD
260 PRINT#1, "Annual Dividend Rate (e.g., .02)";DIV
270 IF TIMEX>0 THEN PRINT#1, "Time to Expiration in Months";TIMEX
280 IF TIMEXX>0 THEN PRINT#1, "Time to Expiration in Days";TIMEXX
290
300 'COMPUTE BASIC PARAMETERS
310 SD2=SD*SD
320 N=2*(R-DIV)/SD2
330 ERT=EXP(-R*T)
340 EDT=EXP(-DIV*T)
350 K=2*R/(SD2*(1-ERT))
3 6 0 Q = ( 1 - N - S Q R ( ( N - 1 ) * ( N - 1 ) + 4 * K ) ) / 2
370 ALPHA=(R-DIV+.5*SD2)*T
3 8 0 ~ B E T A = S D * S Q R ( T )
390 PI2=SQR(2*3.14159265#)
400 H=(LOG(P/S)+ALPHA)/BETA
4 1 0 ~ H 1 = - H ~ ' n e g a t i v e ~ h ~
4 2 0 ~ P H = E X P ( - H 1 * H 1 / 2 ! ) / P I 2 ~
430 KH=1/(1+.33267*ABS(H1))
440 CUMH=1-PH*(.4361836*KH-.1201676*KH*KH+.937298*KH*KH*KH)
450 IF H1<<0 THEN CUMH=1-CUMH
460 G1=-H+BETA
470 GH=EXP(-G1*G1/2!)/PI2
480 KH=1/(1+.33267*ABS(G1))
490 CUMG=1-GH*(.4361836*KH-.1201676*KH*KH+.937298*KH*KH*KH)
500 IF G1<<0 THEN CUMG=1-CUMG
510 EUROPEAN=-P*EDT*CUMH+S*ERT*CUMG 'EUROPEAN PUT
520
5 5 0 ~ P O L D = P ~ ' f i r s t ~ g u e s s ~ i s ~ c u r r e n t ~ s t o c k ~ p r i c e
5 6 0 ~ K O U N T = 1 ~ ' s e t ~ i t e r a t i o n ~ c o u n t e r ~
570 H=(LOG(POLD/S) +ALPHA)/BETA
580 H1=-H 'negative h
590 PH=EXP(-H1*H1/2!)/PI2
```

```
600 KH=1/(1+.33267*ABS(H1))
610 CUMH=1-PH*(.4361836*KH-.1201676*KH*KH+.937298*KH*KH*KH)
6 2 0 ~ I F ~ H 1 \ll 0 ~ T H E N ~ C U M H = 1 - C U M H ~ ' t h i s ~ i s ~ N o r m a l ( - h )
60 G1=-H+BETA
640 GH=EXP(-G1*G1/2!)/PI2
650 KG=1/(1+.33267*ABS(G1))
660 CUMG=1-GH*(.4361836*KG-.1201676*KG*KG+.937298*KG*KG*KG)
6 7 0 ~ I F ~ G 1 \ll 0 ~ T H E N ~ C U M G = 1 - C U M G ~ ' t h i s ~ i s ~ N o r m a l ( - h + b e t a )
6 8 0 ~ P U T V A L = - P O L D * E D T * C U M H + S * E R T * C U M G ~ ' p u t ~ V a l u e ~ a t ~ P = P O L D ~
690
700
```

800 PRINT\#1, USING "\#\# \#\#\#.\#\#\#\# \#\#\#.\#\#\#\# \#\#\#.\#\#\#\#";KOUNT,POLD,PNEW,F
8 1 0

```
1060 MARGIN2=10*P+AMER100
1070 MARGIN=MARGIN1
1080 IF MARGIN2>MARGIN1 THEN MARGIN=MARGIN2
1090 PRINT#1, USING "20% of Price: $#,###.## @10%: $#,###.##";20*P,10*P
1100 PRINT#1, USING "Less OTM: $#,###.## -";OTM
1110 PRINT#1, USING "Plus Premium: $#,###.## $#,###.##";AMER100;AMER100
1120 PRINT#1, USING "\\\\";" ";" "
1130 PRINT#1, USING "Total: $#,###.## $#,###.##";MARGIN1;MARGIN2
1140 PRINT#1, USING "Margin Requirement: $#,###.## (per contract)";MARGIN
1150 PRINT#1, " "
1160 INPUT "Another Case (y/n): ";CASE$
1170 IF CASE$="y" OR CASE$="Y" THEN CLOSE 1: GOTO 20
1180 CLOSE 1
1190 END
```


## Numerical Examples

As examples of the kind of results obtainable using the computer program, look at both at-the-money and out-of-the money situations. The first is the same one that was done by hand earlier.

Stock Price: \$100
Strike Price: $\$ 100$
Risk-Free Interest Rate (e.g., .06): . 06
Volatility (e.g., 0.35): . 35
Annual Dividend Rate (e.g., .02): .02
Time to Expiration in Months: 24

| No. | POLD | PNEW | F |
| :--- | :--- | :--- | :--- |
| 1 | 100.0000 | 66.8516 | 38.8177 |
| 2 | 66.8516 | 59.0941 | 5.8858 |
| 3 | 59.0941 | 58.1949 | 0.5523 |
| 4 | 58.1949 | 58.1819 | 0.0078 |
| 5 | 58.1819 | 58.1819 | 0.0000 |


| European Put Premium: | 14.5955 |
| :--- | ---: |
| Early Exercise Premium: | 1.2884 |
| American Put Premium: | $\$ 15.8840$ |



Critical Stock Price:
Early Exercise Premium: ..... 0.6976

## American Put Premium:

| $20 \%$ of Price: | $\$ 2,000.00$ | $\$ 10 \%:$ |
| :--- | :---: | ---: |
| Less OTM: | $1,500.00$ | 903.03 |
| Plus Premium: | 903.03 | $\$ 1,903.03$ |

Margin Requirement: \$1,903.03 (per contract)

## Computer Program for American Call Premiums

For completeness, I've also developed a short BASIC program for calculating American call premiums. By using a Newton-Raphson iterative search technique, the critical stock price can usually be obtained to within three decimal places in a half dozen or so iterations, as shown in the example that follows. The reason more iterations are
needed to arrive at American call premiums is because in the absence of dividends, there is no early exercise premium for calls. As a result, the smaller the dividend rate, the higher the critical stock price and the longer it takes to converge to it.

```
1 0 ~ ' A M E R I C A N ~ C A L L ~ P R E M I U M S ~ U S I N G ~ B A R O N E - A D E S I ~ A N D ~ W H A L E Y ~ A P P R O A C H
20 INPUT "Enter Stock Price";P
3 0 ~ I N P U T ~ " E n t e r ~ S t r i k e ~ P r i c e " ; S ~
40 INPUT "Enter Risk-Free Interest Rate (e.g., .06)";R
5 0 ~ I N P U T ~ " E n t e r ~ V o l a t i l i t y ~ ( e . g . , ~ 0 . 3 5 ) " ; S D ~
6 0 ~ I N P U T ~ " E n t e r ~ A n n u a l ~ D i v i d e n d ~ R a t e ~ ( e . g . , ~ . 0 2 ) " ; D I V ~
7 0 ~ I N P U T ~ " E n t e r ~ T i m e ~ t o ~ E x p i r a t i o n ~ i n ~ M o n t h s ~ ( 0 ~ f o r ~ d a y s ) " ; T I M E X ~
80 IF TIMEX>0 THEN T=TIMEX/12 GOTO 120
90 INPUT "Enter Time to Expiration in Days";TIMEXX
100 T=TIMEXX/365
1 1 0
120 PRINT 'Where do you want to send results"
130 PRINT "1 = Screen"
140 PRINT "2 = Printer"
150 PRINT "3 = Save to disk"
160 INPUT "Enter your selection";SELECT
170 IF SELECT=0 THEN SELECT =1
180 IF SELECT=1 THEN SAVEFILE$="SCRN:"
190 IF SELECT=2 THEN SAVEFILE$="LPT1 :"
200 IF SELECT=3 THEN INPUT "Enter name of savefile";SAVEFILE$
2 1 0 ~ O P E N ~ S A V E F I L E \$ ~ F O R ~ O U T P U T ~ A S ~ 1 ~
220 PRINT#1, "Stock Price";P
230 PRINT#1, "Strike Price";S
240 PRINT#1, "Risk-Free Interest Rate (e.g., .06)";R
250 PRINT#1, "Volatility (e.g., 0.35)";SD
260 PRINT#1, "Annual Dividend Rate (e.g., .02)";DIV
270 IF TIMEX>0 THEN PRINT#1, "Time to Expiration in Months";TIMEX
2 8 0 ~ I F ~ T I M E X X > 0 ~ T H E N ~ P R I N T \# 1 , ~ " T i m e ~ t o ~ E x p i r a t i o n ~ i n ~ D a y s " ; T I M E X X ~
290
3 0 0 ~ ' C O M P U T E ~ B A S I C ~ P A R A M E T E R S ~
3 1 0 ~ S D 2 = S D * S D ~
3 2 0 ~ N = 2 * ( R - D I V ) / S D 2 '
330 ERT=EXP(-R*T)
340 EDT=EXP(-DIV*T)
350 K=2*R/(SD2*(1-ERT))
3 6 0 ~ Q = ( 1 - N + S Q R ( ( N - 1 ) * ~ ( N - 1 ) + 4 * K ) ) / 2 ~
370 ALPHA=(R-DIV+.5*SD2) *T
380 BETA=SD*SQR(T)
390 PI2=SQR(2*3.14159265#)
400 H1=(LOG(P/S)+ALPHA)/BETA
410 PH=EXP(-H1*H1/2!)/PI2
```

```
420 KH=1/(1+.33267*ABS (H1))
430CUMH=1-PH*(.4361836*KH-.1201676*KH*KH+.937298*KH*KH*KH)
440 IF H1<<0 THEN CUMH=1-CUMH
450 G1=H1-BETA
    460 GH=EXP(-G1*G1/2!)/PI2
470 KH=1/(1+.33267*ABS (G1))
480CUMG=1-GH*(.4361836*KH-.1201676*KH*KH+.937298*KH*KH*KH)
490 IF G1<<0 THEN CUMG=1-CUMG
    5 0 0 ~ E U R O P E A N = P * E D T * C U M H - S * E R T * C U M G ~ ' E U R O P E A N ~ P U T '
510
5 2 0
530
540 POLD=P 'first guess is current stock price
5 5 0 ~ K O U N T = 1 ~ ' s e t ~ i t e r a t i o n ~ c o u n t e r ~
560 H1=(LOG(POLD/S)+ALPHA)/BETA
570 PH=EXP (-H1*H1/2!)/PI2
580 KH=1/(1+.33267*ABS (H1))
590 CUMH=1-PH*(.4361836*KH-.1201676*KH*KH+.937298*KH*KH*KH)
6 0 0 ~ I F ~ H I \ll 0 ~ T H E N ~ C U M H = 1 - C U M H ~ ' t h i s ~ i s ~ N o r m a l ( h )
610 G1=H1-BETA
620 GH=EXP(-G1*G1/2!)/PI2
630 KG=1/(1+.33267*ABS (G1))
640 CUMG=1-GH*(.4361836*KG-.1201676*KG*KG+.937298*KG*KG*KG)
6 5 0 ~ I F ~ G 1 \ll 0 ~ T H E N ~ C U M G = 1 - C U M G ~ ' t h i s ~ i s ~ N o r m a l ( h - b e t a ) ~
6 6 0 ~ C A L L V A L = P O L D * E D T * C U M H - S * E R T * C U M G ~ ' c a l l ~ V a l u e ~ a t ~ P = P O L D ~
670 F=S-POLD+CALLVAL+(1-EDT*CUMH)* (POLD/Q) 'function F at P=POLD
```

```
    l**************************************************
    'START TRIAL AND ERROR SEARCH FOR CRITICAL STOCK PRICE
    'USING NEWTON-RAPHSON ITERATION PROCESS
    DERIVH=PH/(POLD*BETA) 'derivative of Normal(h) at P=POLD
    DERIVG=GH/(POLD*BETA) 'derivative of Normal(h-beta) at P=POLD
    DERIVC=EDT*CUMH+POLD*EDT*DERIVH-S*ERT*DERIVG 'deriv. of Call
    DERIVF:-1+DERIVC+(1-EDT*CUMH)/Q-EDT*DERIVH*(POLD/Q) 'deriv. of F
    PNEW=POLD-F/DERIVF 'new estimate for critical stock price
    '*************************************************
    'DISPLAY CONVERGENCE DETAILS (optional)
    IF KOUNT=1 THEN 770 ELSE }79
    PRINT#1, " "
    PRINT#1, USING "\\\\\\ !";"No.", "POLD","PNEW","F"
    PRINT#1, USING "## ###.#### ###.#### ###.####";KOUNT,POLD,PNEW, F
    '**************************************************
    IF ABS(PNEW-POLD)<<.001 THEN 840 'convergence test
    POLD=PNEW
    KOUNT=KOUNT+1 'increase counter
    IF KOUNT << 11 THEN 570 'cut-off limit on iterations
    CSP=(PNEW+POLD)/2 'final value for the critical stock price
    'COMPUTE EARLY EXERCISE PREMIUM
    A=CSP* (1-EDT*CUMH)/Q
    EARLY=A*(P/CSP)^Q 'early exercise premium
    AMERICAN=EUROPEAN+EARLY 'candidate American call premium
```

```
900 IF P=>CSP THEN AMERICAN=P-S 'premium when call is deep in the money
910 PRINT#1, " "
920 PRINT#1, USING "Critical Stock Price $###.####";CSP
930 PRINT#1, " "
940 PRINT#1, USING "European Call Premium $###.####";EUROPEAN
950 PRINT#1, USING "Early Exercise Premium $##.####";EARLY
960 PRINT#1, USING "\\";" "
970 PRINT#1, USING "American Call Premium $###.####";AMERICAN
980 PRINT#1, " "
990
1000 'COMPUTE MARGIN REQUIREMENTS
1010 IF S>P THEN OTM=100* (S-P) ELSE OTM=0
1020 AMER100=100*AMERICAN
1030 MARGIN1=20*P-OTM+AMER100
1040 MARGIN2=10*P+AMER100
1050 MARGIN=MARGIN1
1060 IF MARGIN2>MARGIN1 THEN MARGIN=MARGIN2
1070 PRINT#1, USING "20% of Price $#,###.## @10% $#,###.##";20*P,10*P
1080 PRINT#1, USING "Less OTM $#,###.## -";OTM
1090 PRINT#1, USING "Plus Premium $#,###.## $#,###.##";AMER100;AMER100
1100 PRINT#1, USING "\\\\";" "
1110 PRINT#1, USING "Total $#,###.## $#,###.##";MARGIN1;MARGIN2
1120 PRINT#1, USING "Margin Requirement $#,###.## (per contract)";MARGIN
1130 PRINT#1, " "
1140 INPUT "Another Case (y/n)";CASE$
1150 IF CASE$="Y" OR CASE$="Y" THEN CLOSE 1 GOTO 20
1160 CLOSE 1
1170 END
```


## Numerical Examples

As examples of the results obtainable with this program, I again consider both at-the-money and out-of-the money situations. The first is the same one that was done by hand, earlier. Note that the computation of call premiums typically takes longer to converge than does the computation of put premiums.

Stock Price: \$100
Strike Price: $\$ 100$
Risk-Free Interest Rate (e.g., .06): .06
Volatility (e.g., 0.35): . 35
Annual Dividend Rate (e.g., .02): . 02
Time to Expiration in Months: 24

| No. | POLD |  | PNEW |  | F |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 100.0000 |  | 170.6420 |  | 33.7405 |  |
| 2 | 170.6420 |  | 257.8725 |  | 13.3574 |  |
| 3 | 257.8725 |  | 372.5958 |  | 5.7306 |  |
| 4 | 372.5958 |  | 425.3898 |  | 1.5634 |  |
| 5 | 425.3898 |  | 427.2815 |  | 0.0528 |  |
| 6 | 427.2815 |  | 427.2836 |  | 0.0001 |  |
| 7 | 427.2836 |  | 427.2833 |  | -0.0000 |  |
| Critical Stock P |  |  |  |  |  | \$427.2834 |
| European Call |  |  |  |  |  | 21.9824 |
| Early Exercise | m: |  |  |  |  | 0.0582 |
| American Call | m: |  |  |  |  | \$ 22.0407 |
| 20\% of Price: |  | \$2,000.00 |  | @ $10 \%$ : |  | \$1,000.00 |
| Less OTM |  | 0.00 |  |  |  | -- |
| Plus Premium: |  | 2,204.07 |  |  |  | 2,204.07 |
| Total: |  | \$4,204.07 |  |  |  | \$ 3,204.07 |

Margin Requirement: \$4,204.07 (per contract)
Stock Price: \$100
Strike Price: \$115

Risk-Free Interest Rate (e.g., .06): . 06
Volatility (e.g., 0.35): . 35
Annual Dividend Rate (e.g., .02): . 02
Time to Expiration in Months: 24

| No. | POLD | PNEW | F |
| :--- | :--- | :--- | :--- |
| 1 | 100.0000 | 182.3433 | 46.6304 |
| 2 | 182.3433 | 277.3311 | 17.7129 |
| 3 | 277.3311 | 407.3093 | 7.6294 |
| 4 | 407.3093 | 486.6183 | 2.4358 |
| 5 | 486.6183 | 491.3691 | 0.1327 |
| 6 | 491.3691 | 491.3751 | 0.0002 |
| 7 | 491.3751 | 491.3751 | -0.0000 |


| Critical Stock Price: |  | $\$ 491.3751$ |
| :--- | ---: | ---: |
| European Call Premium: |  | 16.5386 |
| Early Exercise Premium: |  | 0.0433 |
| American Call Premium: | $\$ 10 \%:$ | $\$ 16.5819$ |
| Less OTM: | $1,500.00$ |  |
| Plus Premium: | $1,658.19$ | $\$ 2,000.00$ |

Margin Requirement: \$2,658.19 (per contract)

## PART FOUR-

ADDITIONAL RESOURCES

## 16

## My Favorite Web Sites

## Introduction

Almost all online brokerage organizations maintain systems for obtaining real-time quotes on listed options. There are also numerous independent information providers that offer real-time or delayed quotes under various pricing plans. I subscribe to none of these because I think there are enough free resources available on the Internet to allow an investor to make intelligent decisions without paying more than the basic monthly Internet access charges. Bear in mind that new Web sites are constantly being introduced and the features described for the sites listed in this chapter are constantly being modified and expanded-so much so that any detailed description that I could offer is quickly outdated.

I have grouped these sites into the following categories: option quotes, real-time quotes, stock screeners, market news, portals, research and analysis, online option pricers, discount broker evaluations, message boards, and Internet providers.

## Option Quotes

There are many sites offering option quotes on the Internet, and I happen to use three of them on a regular, delayed-quote basis. These are the Chicago Board Options Exchange, the Philadelphia Stock Exchange, and Dreyfus Brokerage Services.

The Chicago Board Options Exchange (CBOE) offers bid and asked quotations for both standard options and LEAPS on a 20-minute delayed basis. Its Internet address is $w w w . c b o e . c o m$, and many Internet providers allow you to expedite the process of connecting to it through the use of an embedded keyword such as CBOE or OPTIONS (both words are used by America Online, for example). You can request a quote for a specific call or put option, a short list of near-term at-the-money options, or the full list of all standard options and LEAPS available for the underlying issue. This site is the first place to learn of new LEAPS or standard options that are being introduced or to obtain the trading symbol(s) for the option(s) you are interested in.

The CBOE Web site also offers a free automated mailing service. To get there, click on Trader's Tools and then again on E-mail Alerts. You will then be presented with ten automated mailing lists, any number of which you may subscribe to. For me, the most important one is the daily letter showing contract adjustments (including stock splits, mergers, and acquisitions) to existing options as well as announcements of newly established options and LEAPS. Other mailing lists include event calendars for seminars and classes given by the Options Institute, general announcements, and updated LEAP symbol directories. You can also receive daily market statistics and new series information in Excel (.xls) spreadsheet format.

This site offers much in the way of training materials and software that is available for downloading. A detailed treatise on the tax treatment of options can be found under the Help \& Resources section. Several links to other Web sites providing information about options are also there, including links to all major stock exchanges and associated agencies and clearinghouses. In addition, the CBOE offers online seminars on various options topics; information and registration is at www.cboe.com/chat.

The Philadelphia Stock Exchange (PHLX) also offers bid and asked quotations for both standard options and LEAPS on a 20-minute delayed basis. The Internet address for these quotes is fast.quote.com/fq/newphlx/qchain. The PHLX option tables contain more information than those of the CBOE and include the implied volatility, theoretical option values based on historical volatilities, and other option measures. In addition, you can utilize filters to produce customized tables
based on such criteria as volume, open interest, and option price relative to theoretical values.

As fine as these two exchanges are, there are times when one or both are inaccessible because of Internet traffic, file maintenance, or computer downtime. (This is often not a fault of the exchanges themselves, because both depend on outside sources at the present time for market quotes.) To ensure coverage, I suggest opening and maintaining a no-cost/low-cost type of account from one of the many online brokerage services that are readily available on the Internet. Although there are numerous online brokerage establishments that will provide option quotes, many of them do not provide LEAP quotations along with them.

After examining several such online services, I selected Dreyfus Brokerage Services. Its site provides complete option chains, including LEAPS. Although many of the deep discount, online brokers do this as well, they can be very inaccessible at peak periods because of their popularity (not to mention occasional outages from system overload). The Dreyfus tables do not contain as much information as either the CBOE or PHLX does, but on the other hand download is much fasten The tables show the last trade, bid and asked price, change (if any), daily high and low, trading volume, open interest, and the option symbol. Clicking on the option description will take you right to the option order entry for subscribers authorized to trade options. Access to option and LEAP quotes is completely free after hours and on weekends, when the markets are closed.

If you wish to access the same type of information during trading hours, you can do so by establishing an account with Dreyfus. An opening and maintenance balance of just $\$ 1,000$ is required. The funds deposited can be invested in an interest-bearing money market account (or can be used to purchase equities), which is about as low-cost an arrangement as you will find. A higher balance of $\$ 2,000$ or so is required to do options. Real-time quotes are available by subscription for those who want them. Its Web site address is www.trackpbs.com, and there are a large number of links ( 66 when I last counted) to other Web sites that can provide business news and other data.

## Real-Time Quotes

Real-time quotes are costly and are ordinarily not required by buy-and-hold investors. Nonetheless, they can be instructive to watch during periods of high volatility in the markets. Such services cost from around $\$ 25$ a month for a limited number of monthly quotations to as much as $\$ 75$ a month for unlimited quotations. There are, however, Web sites that provide real-time quotes without charge (or limitation); for example, Thomson RTQ Service, whose Web site address is www.thomsonrtq.com; Free Real Time.com, whose Web site address is $w w w$. freerealtime.com; and Free Real-Time Quote, whose Web site address is www.freereal-timequote.com.

In accordance with stock exchange rules, you must register for any site providing realtime quotations, which means supplying your name, address, telephone number, and Email address (providing such information is the "price" you pay for the service).
Thomson RTQ provides you with last price, the change, the bid and asked price, bid size, asked size, the high trade, the low trade and trading volume, current rating by First Call, and other market statistics on the company. For most issues, intra-day and annual charts are available. In addition to real-time stock quotations, Thomson RTQ now offers realtime quotes on stock options. The other two sites have stated their intention to provide real-time option quotes as well and may have done so by now. Many financial Web sites are in the process of adding real-time quote capabilities to their Web sites. A listing of sites offering real-time stock quotes (both free and for fee) can be found at the Medved QuoteTracker at www.quotetracker.com (note that medved is the Russian word for bear).

## Stock-Screening Sites

There are several sites on the Internet for screening stocks on the basis of performance criteria. The two I use are Hoover's Stock-Screener and Wall Street Research Net.

Hoover's StockScreener permits searches by using up to 20 performance criteria, including six independent financial ratios, six independent growth rates, and several size, margin, return, and volatility (beta) criteria. StockScreener is easy to use. The only downside is that you cannot download the search results into a spreadsheet. The searches
can be limited by exchange and/or industry group. The search results can be presented and printed out alphabetically or in ascending or descending numerical order. Clicking on a company's name will bring up a capsule description. Detailed financial information and news articles of the kind needed by industry analysts, financial advisers, and portfolio managers are also available by paid subscription. Its Web site address is www.stockscreener.com, and like most well designed sites, it can connect you to a plethora of related addresses for additional company and economic information.

Wall Street Research Net permits searches by using up to 13 performance criteria, including several independent financial ratios, growth rates, and size categories. The searches can be limited within various index groups, including the Dow Jones and the S\&P 500, as well as by exchange and/or industry group. Although its reporting mechanism is not as flexible as StockScreener's, a great advantage of this service is the great number of links (it claims over 500,000 ) available to scores of company Web pages, government agencies, the Federal Reserve, and other sites that provide detailed statistical indicators and associated economic reports. The Web site address of Wall Street Research Net is www.wsrn.com/index.html, and just like Stock-Screener, financial information and news articles of the kind needed by industry analysts, financial advisers, and portfolio managers are available by subscription.

## Market News

There are numerous sites on the Internet for breaking news on general market conditions and individual stocks. My two favorites are Yahoo!Finance and CBS Marketwatch. Yahoo!Finance, in addition to breaking market news, has a concise list of upgrades, downgrades, coverage initiated recommendations, and earnings surprises. You can use this site to monitor the market value of your portfolio. Its Web site address is quote.yahoo.com, and there are a vast number of links to other Web sites of potential interest to small investors. I like to link to quote.yahoo.com/m2? $u$ to view in one concise table the market indexes of some 45 stock markets around the world.

CBS Marketwatch has general news features, but the one I like is the ticker containing the one-line summaries of breaking news events
and earnings announcements. Each line shows the time of day and trading symbol of the referenced stock, so you can quickly scan the page for relevant information about any stock(s) of interest. Its Web site address is http:cbs.marketwatch.com/news/headlines.htx?.

Goinvest Weekly is a weekly newspaper that points to numerous resources and news items of potential interest to investors. Its address is at www.goinvest.com. I particularly like the NewsWire feature that brings up links to three classes of breaking stories: Top Headlines, Financial Commentaries, and Economic Reports. You can also search for company news by ticker symbol. You can get directly to the News-Wire by pointing your browser to www.goinvest.com/newswire.shtml.

## Portals

There are a great number of Web sites whose greatest feature in my opinion is the numerous links they provide to other Web sites of interest to investors. My favorites are Daily Stocks, FinancialWeb, and Nomad's Stock Links.

Daily Stocks is a tremendous resource for investors, with over 200 links to various sites providing market data and commentary, news headlines, event calendar, earnings estimates, stock screeners, insider activity, public offerings, technology stocks, futures, filings, research reports, and more. There is also an options pricer for calculating European- and American-style option premiums. Its Web site address is www.dailystocks.com.

FinancialWeb is a completely free Web site offering several novel features for the individual investor. Among these are seamless links to Quote Central, StockTools, Rapid Research, Wall Street Guru, News-Vest, Stock Detective, Bear Tracker, SmallCap Investor, Strike Price, and numerous other useful sites. Selecting Quote Central sends you to www.quotecentral.com for real-time quotes and selecting Strike Price sends you to $w w w$. strikeprice.com which provides (delayed) options quotes. A particularly nice feature of Strike Price is that it is one of the few sites that can provide historical option quotes of the option series involved (including daily volume and high, low, open and closing prices) from inception on. Like many other portals, the features offered are changing and evolving so rapidly that any detailed description is quickly dated. FinancialWeb's Web site address is www.financial
web. com, and there is an interesting online, small-cap investor newsletter you can register for as well.

Nomad's Stock Links is one of the many Web sites authored by individual investors that has been developed for the sheer fun of doing it. It is maintained by an AOL member (who prefers to remain anonymous) at http://members.aol.com/nomadnus, which is perhaps best described as a work of art if not a labor of love. You have to see it to believe it. It provides links to hundreds of sites for searching, screening, charting, and tracking of stocks, indexes, options, and mutual funds. Besides the many links to sites for tracking ongoing prices and breaking news, there are links to sites providing earnings announcements and forecasts, news headlines, upcoming and recent calendar events, stock screening, insider activity, domestic and foreign market activity, market commentary, upgrade/downgrades and research alerts, IPO and other security filings, tech stocks, mutual fund ranking and trends, futures, economic releases, and investment and stock columns. By the way, you do not have to be an AOL member to access this Web site. Just point your browser to this site as you would any other Web address.

## Research and Analysis

There are many sites that provide analysis and ratings of individual stocks. The ones I like best are Zacks Investment Research, StockSmart, First Call, Briefing.com, and Option Chains.

Zacks Investment Research Net is a fee-based Web site that offers several free goodies, including the day's ten best and ten worst earnings surprises, company profiles, and annual income and balance sheets. What I really like, however, is the Wall Street Recommendations, which shows consensus estimates in earnings and the number and distribution of brokers rating a given stock as a strong buy, a moderate buy, a hold, a moderate sell, and a strong sell, along with its average score and its change from the previous week. Its site address is $w w w . z a c k s . c o m$, and there are a large number of advanced features available by paid subscription if desired.

StockSmart is a good place for delayed market quotes on up to 12 stocks at the same time. StockSmart shows winners and losers within an industry group, upcoming splits, distributions, and dividends, along with recent splits and symbol changes. For a relatively small subscrip-
tion fee ( $\$ 12.95$ a month), a host of other information is available, including delayed option quotes. What is potentially very useful is the options analyzer that can be used to evaluate either short- or long-term option strategies. The format of the basic option quote tables is well designed and nicely provides 20-day and six-month volatilities for the underlying issue. Its Web site address is www.stocksmart.com, and there are a great number of links to other Web sites of potential interest to small investors.

First Call makes its living from the sale of real-time earnings estimates and real-time buy/hold/sell recommendations to corporate and institutional clients. Much of this information, however, is available without charge to individual investors on a daily or weekly recap basis. Earnings surprises, upcoming splits and dividend announcements, consensus estimates, upcoming earnings reports, estimate revisions, and numerous other reports can all be accessed free of charge. Its Web site address is www.firstcall.com/individual.

Briefing.com has a crisp calendar of recent and announced splits. The multicolumn charts show company name, stock symbol, split ratio, announcement date, distribution date, and whether the stock is optionable or not. Splits announced during the past week are highlighted for easy reference. The general address of this Web site is $w w w$. briefing.com. To reference the split calendar I point my browser to www.briefing.com/intro/isplits.htm and to reference upgrades/down-grades I point my browser to www.briefing.com/intro/iupdown.htm. Much information is free but as a consequence is limited to perhaps three updates during the day. By subscription the information can be received constantly and continuously updated during the day.

Option Chains is part of Reuters Moneynet and is one of the few sites that lets you customize the options table for any options class by restricting it to a range of months and/or range of strike prices. It is also useful when dealing with options having a substantial number of strike prices, which often arises because of rapid growth in stock price, high volatility, and/or frequent stock splits. This is particularly useful when rolling out an option and you want to restrict the expiration date to a short (or long) horizon and strike prices to a narrow band just below the current one you're rolling out. In addition to the usual information, the table shows the date the option was last traded, which is particu-
larly useful when dealing with less frequently traded options. The Web site is www.moneynet.com/content/MONEYNET/OptionChain/OC Quote.asp, but you might want to start at www.moneynet.com itself to access the other features (many of them free) available there.

## Online Option Pricers

There are numerous Web sites that let you calculate option prices online. These models range from the simplistic Black-Scholes for European options to complex ones for evaluating American-style options. The Numa directory of derivatives software at www.numa. com/software/java.htm has links to about ten such online models; the Global Investor at www.global-investor.com/dir/g-calcs.htm has links to dozens of online financial calculators, including four on options; and the University of Arkansas Web site at comp.uark.edu/'bdow/fin info.html has over a dozen links to various sites offering derivative calculators and related articles. The two online option calculators I've used extensively (if for no other reason than to compare their results to mine) are Roberts Online Pricer available at www.intrepid.com/ and the Options Calculator made available by the CBOE at www.cboe.com. Both these sites offer online tutorials on options, which should be read before running the models.

The methods used by the Online Pricer and Options Calculator to calculate option premiums differ from the one presented in this book, and as a result the premiums obtained will be close but not identical. For example, for an at-the-money LEAP put of $\$ 100$, with a volatility of 0.40 , a dividend of 3 percent, a risk-free rate of 6 percent, and 24 months to expiration, the premium calculated for an American-style put using the Barone-Adesi and Whaley approach described earlier in this book is $\$ 18.978$. The Online Pricer uses a slightly different approximation method and yields a value of $\$ 18.695$. The Options Calculator is based on a binomial model in which the annual dividend is not spread across the year but paid discretely on a quarterly basis. As a result, the put value will be somewhat higher, with values ranging from about $\$ 19.50$ to $\$ 19.75$, depending on the number of days to the initial dividend date.

## Discount Broker Evaluation

Before signing on with any online broker, you should visit $w w w$. astro.lsa.umich.edu:80/users/philf/www/home.html, where a substantial amount of information on nearly 100 discount and/or online stock and option brokers has been compiled and evaluated. The discount brokers are divided into three classes: deep discount, middle-cost, and higher-cost discount brokers. At a minimum, the information provided includes the commission structure, account setup and maintenance charges, account minimums, broker call rates, and the fee and/or credit schedule for real-time quotes. The commission structure is ordinarily quite complete and includes per-contract and minimum trading costs for both broker-assisted and unassisted transactions. Of particular interest are the numerous comments gleaned from Internet news groups and chat rooms on the experiences (good and bad) that investors have had with the discount and/or online brokers. The Web site address and telephone number for each broker are given. In only a few instances was information provided as to whether naked options are permitted and the extent to which stop limit orders can be accommodated.

In addition to the above, the Robert's Web site at www.intrepid. com/ offers a commission pricer that shows how much it would cost in brokerage commissions to purchase a given number of shares of stock or option contracts at a given price from 50 different discount brokers. The resulting list is ordered alphabetically and by commission size, accompanied by telephone numbers or Web site addresses.

Option Sites is another site that has option broker scorecards. In addition, it lists various Web sites offering option quotes and even has a directory of the latest option books. The various option quote providers are also reviewed and rated, and I visit this site at www.optionsites. com from time to time to learn what's new.

## Message Boards

A good place to place questions and read responses about options and investing are message boards. Many exist but very few are devoted exclusively to options. The two that I read regularly are the newsgroup misc.invest.options and the options message board that is part of the Shark Attack Trading Forum. The former is unfortunately unmoder-
ated, so there tends to be a lot of irrelevant material encountered besides the dozens of posts about options that arrive weekly from practitioners, students, and occasionally members of the academic community. The latter is available only to AOL subscribers using keyword TRADERS, then clicking on Message Boards and selecting Options. The messages here are typically posted by intermediate and advanced option practitioners, and much can be learned just by reading the posts and responses left by others.

## Internet Providers

To access any of these Web sites, you need an Internet provider, and I happen to use two as needs arise.

America Online is my provider of choice, as it is for millions of individual investors. The main investment menu, accessed using the keyword QUOTES, is organized into seven sections, labeled Portfolio, Market News Center, News by Ticker, Historical Quotes, Company Research, Brokerage Center, and Mutual Fund Center. Each section will send you to or pick up information from numerous financial Web sites in a completely seamless manner. I particularly like Historical Quotes because historical stock prices and volume activities can be downloaded for analysis or charting purposes in a matter of seconds on a daily, weekly, or monthly basis as far back as January 1, 1987. The quotation service provides 15 -minute-delayed quotes on almost all listed securities but not on options or LEAPS. On the other hand, the keyword CBOE sends you seamlessly to the Chicago Board Options Exchange, where one can get information on options on a delayed-quote basis.

Metricom's Ricochet system is a wireless, radio-based Internet provider that permits me access to the Internet while on the move. Although presently operating in just the largest metropolitan areas at 28.8 kilobyte data rates, by mid-2000 the speed will be increased to 128 kilobytes and by mid-2001 the system will be extended to 46 cities nationwide. Access to the Internet via radio can be cheaper than through regular telephones. A radio modem is about $\$ 350$ and monthly service fee for unlimited access is typically $\$ 30$. Although this sounds more expensive than America Online or most other Internet service providers, you do not have to pay for a telephone line. With a Ricochet modem attached to my laptop, I can stay in touch with the markets without a telephone or electrical outlet in sight. I love it.

## 17- <br> Selected Bibliography

As I pointed out earlier, Amazon.com lists over 300 books currently available on options or closely related topics. Below are the ones I have read.

Black-Scholes and Beyond, Neil A. Chriss, McGraw-Hill, Inc., New York, NY, 496 pp., 1997, ISBN 0-7863-1025-1, \$65 (hardcover). An advanced treatise on pricing options using the Cox-Ross-Rubenstein binomial model and the latest approaches to the subject using implied volatility trees and implied binomial trees. Contains an excellent reference list of texts and papers published on the subject of option pricing.

Guide to the Markets, Investors Business Daily, John Wiley \& Sons, New York, NY, 277 pp., 1996, ISBN 0-471-15482-2, $\$ 16.95$ (softcover). One of the best books ever written about long-term investments. Its chapter on options is a model of clarity. A copy should be on every investor's desk.

How the Options Markets Work, Joseph A. Walker, The New York Institute of Finance (A Division of Simon \& Schuster), New York, NY, 229 pp., 1991, ISBN 0-13-400888$\mathrm{X}, \$ 17.95$ (softcover). This delightful book is one of the most readable introductions to options in print today. Although written before the introduction of LEAPS, it deserves a place on every option player's bookshelf.

LEAPS (Long-Term Equity Anticipation Securities), Harrison Roth, Irwin Professional Publishing, Burr Ridge, IL, 322 pp., 1994, ISBN 1-55623-819-3, \$45 (hardcover). This was the first book ever devoted specifically to LEAPS. It is an intermediate-level text that explains a great many strategies - including spreads, straddles, and stranglesinvolving long-term options. At the time this book was written there were LEAPS available on 127 issues.

Listed Stock Options (Revised Edition), Carl F. Luft and Richard K. Shiener, Irwin Professional Publishing, Burr Ridge, IL, 236 pp., 1994, ISBN 1-55738-520-3, \$24.95 (softcover). A very clear and well-written introduction to options that includes a chapter on LEAPS and their distinguishing features. There are numerous case histories throughout the text, with extremely sharp analyses of the interplay between the underlying stocks and corresponding option prices. I like this one very much.

McMillan on Options, Lawrence G. McMillan, John Wiley \& Sons, New York, NY, 570 pp., 1996, ISBN 0-471-11960-1, \$65 (hardcover). This is a companion text to the author's earlier book, Options as a Strategic Investment, and it focuses on options trading techniques by means of seemingly countless examples drawn from actual situations. The examples are both enlightening and entertaining, and much can be learned from them, even by nontraders. Note, however, that the formulas presented in the appendix contain transcription errors in some instances and should not be relied on.

The Option Advisor, Bernie Schaeffer, John Wiley \& Sons, New York, NY, 316 pp., 1997, ISBN 0-471-18539-6, \$59.95 (hardcover). An intermediate-level book for options traders. What makes this book a useful addition to my library is the detailed treatment of LEAPS and the lovely section on navigating the Internet with its many Web site addresses for obtaining relevant financial and investment information.

Option Volatility and Pricing, Sheldon Natenberg, Irwin Professional Publishing, Burr Ridge, IL, 469 pp., 1994, ISBN 1-55738-486-X, \$50 (hardcover). This is an advanced text on options strategies, with detailed discussion and analysis of how option volatility affects option pricing. There is little discussion of LEAPS.

Options (3d Edition), Robert W. Kolb, Blackwell Publishers, Malden, MA, 347 pp., 1997, ISBN 1-57718-064-X, \$64.95 (hardcover). One of the latest books containing both practical and theoretical treatments of option pricing and evaluation. This is one of very few books that treat the subject of exotic options of almost every description. Although the book names over 80 people as having reviewed various sections of the text, there are, unfortunately, several inconsistencies in the mathematical formulas (and occasionally outright transcription errors). Accompanying the book is a diskette that contains the pricing and sensitivity formulas for both European- and American-style options. The programming code appears to be error free, however, as the program arrived at the proper solution in the numerous cases that I tested it for.

Options as a Strategic Investment (3d Edition), Lawrence G. McMillan, New York Institute of Finance (A Simon \& Schuster Company), New York, NY, 882 pp., 1993, ISBN 0-13-636002-5, \$44.95 (hardcover). This is a very
complete text on basic option strategies written by an acknowledged master. The book contains an excellent 43-page chapter on LEAPS. Pricing formulas and numerical examples are all based on the original Black-Scholes model, without taking into consideration early exercise or dividends.

Options for the Stock Investor, James B. Bittman, Irwin Professional Publishing, Burr Ridge, IL, 273 pp., 1996, ISBN 1-55738-872-5, \$29.95 (hardcover). This is an intermediate-level text for investors seeking to enhance their investment yield or protect the asset values of their stock portfolios through the use of options. Included with the book is a diskette containing a computer program based on the Black-Scholes formula to calculate option premiums given the price of the underlying issue, the strike price, the dividend yield, the risk-free interest rate, the number of days to expiration, and the volatility. The program can also calculate implied volatility from option premiums. The techniques presented deal with conventional options with little reference to their longterm counterparts.

The Options Manual (3d Edition), Gary L. Gastineau, McGraw-Hill, Inc., New York, NY, 440 pp., 1995, ISBN 0-07-022981-3, \$49.95 (hardcover). This intermediate to advanced text is perhaps the best reference book on options that is available. Besides the usual treatment of option strategies, it contains unparalleled discussions of the history of options, their regulatory framework, taxation, and institutional usage. The only drawback is that the main body of the book was last updated in 1987 and does not contain any discussion of LEAPS or other changes that have taken place in the option markets since then.

Options Markets, John C. Cox and Mark Rubinstein, Prentice Hall, Englewood Cliffs, NJ, 498 pp., 1985, ISBN 0-13-638205-3, $\$ 76$ (hardcover). Although LEAPS had not yet been invented at the time of its writing, this book remains the classic source for the theoretical evaluation of option strategies and alternative approaches to option pricing. Readers not familiar with advanced mathematical techniques will appreciate the sections describing clearing operations and the roles of market makers, participating brokers, and exchanges in options market activities.

Understanding The Options Markets, Commodity Research Bureau, New York, NY, 52 pp., 1989. This pamphlet is long outdated and precedes the introduction of LEAPS, but it was ordered in such large numbers by brokerage firms that it is still being given away free to customers. The writing is often unclear and the pamphlet's primary virtue is as a curiosity piece for those compiling a history of options trading.

## APPENDIX AEUROPEAN PUT PREMIUMS

The tables that follow show the option premiums for European-style LEAP puts based on the formulas contained in Chapter 14. They are based on a stock price of $\$ 100$ and exercise (strike) prices ranging from $\$ 120$ down to $\$ 60$ in steps of $\$ 5$. Each table is presented in matrix format, with volatilities ranging from a low of 0.15 through a high of 0.65 . Time to expiration ranges from 1 month to a maximum of 30 months. A dividend rate of zero and risk-free interest rate of 6 percent are assumed in all instances.

To obtain premiums for stock prices other than $\$ 100$, simply scale or interpolate the tables. For example, suppose you want to know the put premium for a stock price of $\$ 50$, strike price of $\$ 45$ for a volatility of 0.40 , and expiration date 24 months away. From Table A.7, we see that the premium for a $\$ 100$ stock with strike $\$ 90$ for volatility 0.40 and 24-month expiration is $\$ 11.452$. The premium for the $\$ 50$ stock with strike $\$ 45$ is therefore half this amount, or $\$ 5.726$ (i.e., $\$ 572.60$ per contract).

Suppose the stock price is $\$ 60$ and the strike price is $\$ 50$ for the same volatility and expiration. From Table A.8, we see that the premium for a $\$ 100$ stock with strike $\$ 85$ is $\$ 9.527$, and from Table A.9, we see that the premium for a $\$ 100$ stock with strike $\$ 80$ is $\$ 7.782$. Multiplying each of these figures by 0.60 shows that the premium for a $\$ 60$ stock with strike $\$ 51$ is $\$ 5.716$, and the premium for a $\$ 60$ stock with strike $\$ 48$ is $\$ 4.669$. The premium for the $\$ 60$ stock with strike $\$ 50$ is therefore $\$ 4.669+0.667 \times$ ( $\$ 5.716$ - $\$ 4.669$ ), or $\$ 5.367$ (i.e., $\$ 536.70$ per contract).

Table A. 1
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 1 2 0}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 19.402 | 19.403 | 19.419 | 19.472 | 19.577 | 19.742 | 19.962 | 20.235 | 20.551 | 20.905 | 21.292 |
| 2 | 18.811 | 18.862 | 19.015 | 19.287 | 19.668 | 20.137 | 20.677 | 21.272 | 21.910 | 22.583 | 23.284 |
| 3 | 18.250 | 18.425 | 18.782 | 19.297 | 19.932 | 20.657 | 21.447 | 22.286 | 23.163 | 24.068 | 24.996 |
| 4 | 17.734 | 18.077 | 18.645 | 19.382 | 20.236 | 21.173 | 22.168 | 23.205 | 24.274 | 25.366 | 26.476 |
| 5 | 17.266 | 17.790 | 18.560 | 19.495 | 20.539 | 21.657 | 22.827 | 24.033 | 25.265 | 26.516 | 27.780 |
| 6 | 16.840 | 17.548 | 18.504 | 19.616 | 20.828 | 22.106 | 23.428 | 24.782 | 26.156 | 27.545 | 28.945 |
| 7 | 16.450 | 17.336 | 18.464 | 19.736 | 21.099 | 22.520 | 23.979 | 25.463 | 26.965 | 28.478 | 29.998 |
| 8 | 16.091 | 17.147 | 18.433 | 19.852 | 21.351 | 22.901 | 24.483 | 26.087 | 27.704 | 29.329 | 30.958 |
| 9 | 15.757 | 16.974 | 18.406 | 19.960 | 21.584 | 23.253 | 24.948 | 26.661 | 28.384 | 30.111 | 31.839 |
| 10 | 15.445 | 16.814 | 18.382 | 20.060 | 21.800 | 23.578 | 25.378 | 27.192 | 29.012 | 30.834 | 32.652 |
| 11 | 15.152 | 16.664 | 18.359 | 20.152 | 21.999 | 23.879 | 25.777 | 27.684 | 29.595 | 31.503 | 33.406 |
| 12 | 14.874 | 16.522 | 18.335 | 20.236 | 22.184 | 24.159 | 26.148 | 28.143 | 30.137 | 32.126 | 34.107 |
| 13 | 14.611 | 16.386 | 18.310 | 20.312 | 22.354 | 24.418 | 26.493 | 28.570 | 30.642 | 32.707 | 34.762 |
| 14 | 14.360 | 16.255 | 18.284 | 20.380 | 22.512 | 24.660 | 26.815 | 28.968 | 31.115 | 33.251 | 35.374 |
| 15 | 14.120 | 16.128 | 18.256 | 20.442 | 22.657 | 24.885 | 27.116 | 29.342 | 31.558 | 33.762 | 35.949 |
| 16 | 13.889 | 16.005 | 18.226 | 20.497 | 22.792 | 25.095 | 27.398 | 29.692 | 31.974 | 34.241 | 36.489 |
| 17 | 13.668 | 15.884 | 18.194 | 20.546 | 22.916 | 25.291 | 27.661 | 30.021 | 32.365 | 34.692 | 36.998 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 13.454 | 15.767 | 18.160 | 20.589 | 23.031 | 25.474 | 27.908 | 30.329 | 32.734 | 35.117 | 37.477 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 13.247 | 15.651 | 18.124 | 20.626 | 23.137 | 25.644 | 28.140 | 30.620 | 33.081 | 35.518 | 37.930 |
| 20 | 13.047 | 15.538 | 18.087 | 20.658 | 23.234 | 25.802 | 28.357 | 30.894 | 33.408 | 35.897 | 38.358 |
| 21 | 12.853 | 15.426 | 18.048 | 20.685 | 23.323 | 25.950 | 28.562 | 31.152 | 33.718 | 36.256 | 38.762 |
| 22 | 12.665 | 15.316 | 18.006 | 20.708 | 23.405 | 26.088 | 28.754 | 31.395 | 34.010 | 36.594 | 39.145 |
| 23 | 12.482 | 15.207 | 17.964 | 20.726 | 23.479 | 26.217 | 28.934 | 31.625 | 34.286 | 36.915 | 39.508 |
| 24 | 12.304 | 15.100 | 17.919 | 20.739 | 23.547 | 26.337 | 29.103 | 31.841 | 34.548 | 37.219 | 39.851 |
| 25 | 12.131 | 14.994 | 17.873 | 20.749 | 23.609 | 26.449 | 29.262 | 32.046 | 34.795 | 37.506 | 40.177 |
| 26 | 11.962 | 14.889 | 17.826 | 20.754 | 23.665 | 26.553 | 29.412 | 32.239 | 35.029 | 37.779 | 40.486 |
| 27 | 11.797 | 14.785 | 17.777 | 20.756 | 23.715 | 26.649 | 29.552 | 32.421 | 35.250 | 38.037 | 40.778 |
| 28 | 11.636 | 14.683 | 17.726 | 20.754 | 23.761 | 26.739 | 29.684 | 32.592 | 35.460 | 38.282 | 41.056 |
| 29 | 11.479 | 14.581 | 17.674 | 20.750 | 23.801 | 26.822 | 29.808 | 32.754 | 35.658 | 38.514 | 41.319 |
| 20 | 11.325 | 14.479 | 17.621 | 20.742 | 23.836 | 26.898 | 29.924 | 32.907 | 35.845 | 38.734 | 41.569 |

Table A. 2
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 115$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 14.428 | 14.447 | 14.519 | 14.665 | 14.884 | 15.167 | 15.503 | 15.882 | 16.296 | 16.737 | 17.201 |
| 2 | 13.896 | 14.063 | 14.382 | 14.826 | 15.363 | 15.967 | 16.621 | 17.312 | 18.030 | 18.770 | 19.527 |
| 3 | 13.447 | 13.829 | 14.400 | 15.100 | 15.887 | 16.733 | 17.620 | 18.538 | 19.477 | 20.432 | 21.400 |
| 4 | 13.073 | 13.673 | 14.468 | 15.384 | 16.375 | 17.417 | 18.493 | 19.594 | 20.711 | 21.841 | 22.979 |
| 5 | 12.753 | 13.561 | 14.553 | 15.653 | 16.819 | 18.028 | 19.264 | 20.520 | 21.789 | 23.067 | 24.350 |
| 6 | 12.474 | 13.472 | 14.639 | 15.902 | 17.221 | 18.576 | 19.953 | 21.345 | 22.747 | 24.155 | 25.565 |
| 7 | 12.225 | 13.397 | 14.722 | 16.130 | 17.586 | 19.071 | 20.574 | 22.089 | 23.610 | 25.133 | 26.657 |
| 8 | 11.998 | 13.330 | 14.798 | 16.337 | 17.917 | 19.521 | 21.139 | 22.765 | 24.394 | 26.022 | 27.648 |
| 9 | 11.789 | 13.268 | 14.867 | 16.527 | 18.220 | 19.933 | 21.656 | 23.383 | 25.111 | 26.836 | 28.555 |
| 10 | 11.594 | 13.209 | 14.929 | 16.699 | 18.498 | 20.311 | 22.131 | 23.953 | 25.772 | 27.585 | 29.391 |
| 11 | 11.410 | 13.152 | 14.983 | 16.857 | 18.753 | 20.660 | 22.571 | 24.479 | 26383 | 28.278 | 30.164 |
| 12 | 11.236 | 13.095 | 15.030 | 17.001 | 18.988 | 20.983 | 22.978 | 24.968 | 26.950 | 28.923 | 30.883 |
| 12 | 11.070 | 13.039 | 15.071 | 17.132 | 19.206 | 21.283 | 23.356 | 25.423 | 27.479 | 29.524 | 31.554 |
| 13 | 110.610 | 12.867 | 15.158 | 17.461 | 19.764 | 22.060 | 24.346 | 26.617 | 28.873 | 31.109 | 33.324 |
| 14 | 10.911 | 12.982 | 15.106 | 17.252 | 19.407 | 21.561 | 23.709 | 25.847 | 27.974 | 30.086 | 32.182 |
| 15 | 10.758 | 12.925 | 15.135 | 17.361 | 19.592 | 21.819 | 24.038 | 26.245 | 28.437 | 30.613 | 32.771 |
| 10.467 | 12.809 | 15.177 | 17.552 | 19.923 | 22.285 | 24.634 | 26.968 | 29.282 | 31.575 | 33.846 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 10.328 | 12.750 | 15.192 | 17.635 | 20.071 | 22.496 | 24.905 | 27.297 | 29.668 | 32.015 | 34.338 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 10.193 | 12.691 | 15.201 | 17.709 | 20.208 | 22.692 | 25.160 | 27.607 | 30.031 | 32.431 | 34.802 |
| 20 | 10.062 | 12.631 | 15.207 | 17.777 | 20.335 | 22.877 | 25.399 | 27.900 | 30.375 | 32 | 823 |
| 35.241 |  |  |  |  |  |  |  |  |  |  |  |
| 21 | 9.933 | 12.571 | 15.209 | 17.838 | 20.452 | 23.049 | 25.624 | 28.176 | 30.700 | 33.194 | 35.657 |
| 22 | 9.808 | 12.510 | 15.207 | 17.892 | 20.561 | 23.211 | 25.837 | 28.436 | 31.007 | 33.546 | 36.051 |
| 23 | 9.686 | 12.448 | 15.201 | 17.941 | 20.662 | 23.362 | 26.036 | 28.683 | 31.298 | 33.879 | 36.424 |
| 24 | 9.567 | 12.386 | 15.193 | 17.984 | 20.756 | 23.504 | 26.225 | 28.916 | 31.573 | 34.195 | 36.778 |
| 25 | 9.450 | 12.322 | 15.181 | 18.023 | 20.842 | 23.637 | 26.402 | 29.136 | 31.834 | 34.495 | 37.114 |
| 26 | 9.335 | 12.258 | 15.167 | 18.056 | 20.922 | 23.761 | 26.570 | 29.344 | 32.082 | 34.779 | 37.433 |
| 27 | 9.221 | 12.194 | 15.150 | 18.085 | 20.996 | 23.878 | 26.727 | 29.542 | 32.316 | 35.049 | 37.736 |
| 28 | 9.110 | 12.129 | 15.130 | 18.110 | 21.063 | 23.987 | 26.876 | 29.728 | 32.539 | 35.305 | 38.023 |
| 29 | 9.001 | 12.064 | 15.109 | 18.131 | 21.125 | 24.089 | 27.016 | 29.905 | 32.750 | 35.548 | 38.296 |
| 30 | 8.893 | 11.998 | 15.085 | 18.148 | 21.182 | 24.184 | 27.148 | 30.072 | 32.950 | 35.779 | 38.556 |

Table A. 3
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 110$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 9.482 | 9.604 | 9.832 | 10.147 | 10.525 | 10.949 | 11.407 | 11.891 | 12.393 | 12.910 | 13.439 |
| 2 | 9.143 | 9.557 | 10.106 | 10.741 | 11.429 | 12.154 | 12.904 | 13.671 | 14.451 | 15.241 | 16.037 |
| 3 | 8.930 | 9.606 | 10.408 | 11.279 | 12.194 | 13.136 | 14.097 | 15.070 | 16.052 | 17.040 | 18.032 |
| 4 | 8.776 | 9.677 | 10.683 | 11.747 | 12.844 | 13.962 | 15.094 | 16.235 | 17.381 | 18.531 | 19.682 |
| 5 | 8.654 | 9.747 | 10.928 | 12.154 | 13.408 | 14.676 | 15.955 | 17.239 | 18.526 | 19.814 | 21.101 |
| 6 | 8.549 | 9.811 | 11.144 | 12.514 | 13.904 | 15.305 | 16.712 | 18.123 | 19.534 | 20.943 | 22.350 |
| 7 | 8.455 | 9.867 | 11.336 | 12.833 | 14.346 | 15.866 | 17.390 | 18.914 | 20.436 | 21.954 | 23.468 |
| 8 | 8.368 | 9.914 | 11.506 | 13.120 | 14.744 | 16.372 | 18.002 | 19.628 | 21.251 | 22.869 | 24.480 |
| 9 | 8.284 | 9.954 | 11.658 | 13.378 | 15.105 | 16.833 | 18.559 | 20.280 | 21.996 | 23.704 | 25.404 |
| 10 | 8.204 | 9.988 | 11.793 | 13.612 | 15.434 | 17.253 | 19.069 | 20.878 | 22.680 | 24.472 | 26.255 |
| 11 | 8.126 | 10.011 | 11.915 | 13.825 | 15.734 | 17.640 | 19.539 | 21.430 | 23.312 | 25.183 | 27.042 |
| 12 | 8.049 | 10.030 | 12.024 | 14.019 | 16.011 | 17.997 | 19.975 | 21.943 | 23.899 | 25.843 | 27.773 |
| 12 | 7.974 | 10.044 | 12.121 | 14.196 | 16.266 | 18.327 | 20.379 | 22.419 | 24.446 | 26.459 | 28.455 |
| 13 | 7.754 | 10.057 | 12.354 | 14.643 | 16.922 | 19.187 | 21.437 | 23.671 | 25.887 | 28.082 | 30.256 |
| 14 | 7.900 | 10.053 | 12.208 | 14.358 | 16.501 | 18.634 | 20.756 | 22.864 | 24.957 | 27.035 | 29.094 |
| 15 | 7.826 | 10.057 | 12.285 | 14.507 | 16.719 | 18.920 | 21.108 | 23.281 | 25.437 | 27.575 | 29.693 |
| 17 | 7.882 | 10.052 | 12.416 | 14.769 | 17.110 | 19.438 | 21.747 | 24.039 | 26.310 | 28.560 | 30.787 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 7.609 | 10.044 | 12.470 | 14.884 | 17.285 | 19.670 | 22.037 | 24.384 | 26.710 | 29.012 | 31.288 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 7.537 | 10.033 | 12.517 | 14.990 | 17.448 | 19.889 | 22.310 | 24.710 | 27.087 | 29.438 | 31.761 |
| 20 | 7.466 | 10.018 | 12.559 | 15.088 | 17.600 | 20.094 | 22.568 | 25.018 | 27.443 | 29.841 | 32.209 |
| 21 | 7.394 | 10.000 | 12.596 | 15.177 | 17.742 | 20.287 | 22.810 | 25.309 | 27.781 | 30.223 | 32.633 |
| 22 | 7.323 | 9.980 | 12.627 | 15.259 | 17.874 | 20.469 | 23.039 | 25.584 | 28.100 | 30.585 | 33.035 |
| 23 | 7.252 | 9.958 | 12.654 | 15.335 | 17.998 | 20.639 | 23.256 | 25.845 | 28.403 | 30.928 | 33.417 |
| 24 | 7.181 | 9.933 | 12.676 | 15.404 | 18.113 | 20.800 | 23.460 | 26.091 | 28.690 | 31.254 | 33.779 |
| 25 | 7.111 | 9.906 | 12.694 | 15.467 | 18.221 | 20.951 | 23.653 | 26.325 | 28.963 | 31.563 | 34.124 |
| 26 | 7.041 | 9.878 | 12.709 | 15.525 | 18.321 | 21.093 | 23.836 | 26.546 | 29.221 | 31.857 | 34.451 |
| 27 | 6.972 | 9.848 | 12.720 | 15.577 | 18.415 | 21.227 | 24.008 | 26.756 | 29.467 | 32.137 | 34.762 |
| 28 | 6.903 | 9.816 | 12.727 | 15.625 | 18.502 | 21.352 | 24.172 | 26.956 | 29.700 | 32.402 | 35.058 |
| 29 | 6.835 | 9.783 | 12.732 | 15.668 | 18.583 | 21.471 | 24.326 | 27.145 | 29.922 | 32.655 | 35.339 |
| 30 | 6.768 | 9.748 | 12.734 | 15.707 | 18.659 | 21.582 | 24.472 | 27.324 | 30.133 | 32.895 | 35.607 |

Table A. 4
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 105$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 4.837 | 5.239 | 5.707 | 6.211 | 6.738 | 7.279 | 7.829 | 8.387 | 8.950 | 9.516 | 10.085 |
| 2 | 4.952 | 5.666 | 6.423 | 7.204 | 7.997 | 8.798 | 9.605 | 10.415 | 11.227 | 12.041 | 12.856 |
| 3 | 5.064 | 6.003 | 6.970 | 7.952 | 8.941 | 9.935 | 10.931 | 11.929 | 12.927 | 13.924 | 14.920 |
| 4 | 5.156 | 6.275 | 7.412 | 8.558 | 9.708 | 10.860 | 12.012 | 13.163 | 14.313 | 15.461 | 16.607 |
| 5 | 5.228 | 6.500 | 7.782 | 9.069 | 10.357 | 11.645 | 12.931 | 14.215 | 15.496 | 16.774 | 18.048 |
| 6 | 5.284 | 6.689 | 8.099 | 9.510 | 10.920 | 12.328 | 13.733 | 15.134 | 16.532 | 17.925 | 19.313 |
| 7 | 5.327 | 6.850 | 8.374 | 9.897 | 11.417 | 12.933 | 14.446 | 15.953 | 17.456 | 18.952 | 20.442 |
| 8 | 5.359 | 6.989 | 8.616 | 10.240 | 11.861 | 13.477 | 15.087 | 16.692 | 18.290 | 19.881 | 21.464 |
| 9 | 5.382 | 7.108 | 8.830 | 10.548 | 12.262 | 13.969 | 15.671 | 17.365 | 19.051 | 20.728 | 22.396 |
| 10 | 5.397 | 7.211 | 9.021 | 10.826 | 12.626 | 14.419 | 16.205 | 17.982 | 19.750 | 21.507 | 23.254 |
| 11 | 5.404 | 7.300 | 9.192 | 11.079 | 12.959 | 14.832 | 16.697 | 18.551 | 20.395 | 22.228 | 24.048 |
| 12 | 5.405 | 7.378 | 9.347 | 11.310 | 13.266 | 15.214 | 17.152 | 19.079 | 20.995 | 22.897 | 24.785 |
| 12 | 5.368 | 7.597 | 9.830 | 12.059 | 14.279 | 16.488 | 18.683 | 20.863 | 23.026 | 25.169 | 27.291 |
| 13 | 5.402 | 7.445 | 9.486 | 11.521 | 13.548 | 15.567 | 17.575 | 19.571 | 21.553 | 23.521 | 25.474 |
| 14 | 5.394 | 7.503 | 9.612 | 11.715 | 13.810 | 15.895 | 17.969 | 20.030 | 22.076 | 24.105 | 26.118 |
| 15 | 5.382 | 7.554 | 9.726 | 11.894 | 14.053 | 16.202 | 18.338 | 20.460 | 22.565 | 24.653 | 26.722 |
| 17 | 5.350 | 7.634 | 9.925 | 12.211 | 14.490 | 16.756 | 19.008 | 21.243 | 23.459 | 25.655 | 27.827 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 5.330 | 7.666 | 10.011 | 12.353 | 14.686 | 17.007 | 19.313 | 21.601 | 23.868 | 26.113 | 28.334 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 5.308 | 7.692 | 10.089 | 12.484 | 14.870 | 17.244 | 19.601 | 21.939 | 24.255 | 26.547 | 28.813 |
| 20 | 5.284 | 7.714 | 10.159 | 12.605 | 15.042 | 17.466 | 19.872 | 22.258 | 24.621 | 26.958 | 29.266 |
| 21 | 5.258 | 7.731 | 10.224 | 12.718 | 15.203 | 17.675 | 20.128 | 22.560 | 24.967 | 27.347 | 29.696 |
| 22 | 5.231 | 7.745 | 10.282 | 12.823 | 15.355 | 17.872 | 20.371 | 22.846 | 25.296 | 27.716 | 30.105 |
| 23 | 5.202 | 7.755 | 10.335 | 12.920 | 15.496 | 18.058 | 20.600 | 23.118 | 25.608 | 28.067 | 30.492 |
| 24 | 5.172 | 7.761 | 10.382 | 13.010 | 15.630 | 18.234 | 20.817 | 23.375 | 25.904 | 28.400 | 30.861 |
| 25 | 5.141 | 7.765 | 10.425 | 13.094 | 15.755 | 18.400 | 21.023 | 23.619 | 26.185 | 28.717 | 31.211 |
| 26 | 5.109 | 7.766 | 10.464 | 13.171 | 15.872 | 18.556 | 21.218 | 23.851 | 26.453 | 29.019 | 31.545 |
| 27 | 5.076 | 7.764 | 10.498 | 13.243 | 15.982 | 18.704 | 21.403 | 24.072 | 26.708 | 29.306 | 31.862 |
| 28 | 5.042 | 7.760 | 10.528 | 13.310 | 16.086 | 18.844 | 21.578 | 24.282 | 26.950 | 29.579 | 32.164 |
| 29 | 5.008 | 7.754 | 10.555 | 13.372 | 16.183 | 18.976 | 21.744 | 24.481 | 27.181 | 29.839 | 32.452 |
| 20 | 4.973 | 7.746 | 10.578 | 13.429 | 16.274 | 19.101 | 21.902 | 24.670 | 27.400 | 30.087 | 32.727 |

Table A. 5
European-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 100$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 1.485 | 2.057 | 2.629 | 3.202 | 3.776 | 4.349 | 4.922 | 5.495 | 6.067 | 6.639 | 7.211 |
| 2 | 1.965 | 2.767 | 3.572 | 4.378 | 5.185 | 5.991 | 6.797 | 7.603 | 8.408 | 9.212 | 10.015 |
| 3 | 2.283 | 3.258 | 4.237 | 5.220 | 6.202 | 7.185 | 8.167 | 9.149 | 10.128 | 11.107 | 12.083 |
| 4 | 2.520 | 3.636 | 4.760 | 5.888 | 7.018 | 8.147 | 9.275 | 10.401 | 11.526 | 12.649 | 13.769 |
| 5 | 2.705 | 3.943 | 5.192 | 6.447 | 7.703 | 8.959 | 10.214 | 11.466 | 12.716 | 13.963 | 15.207 |
| 6 | 2.854 | 4.199 | 5.560 | 6.927 | 8.296 | 9.665 | 11.032 | 12.397 | 13.758 | 15.115 | 16.468 |
| 7 | 2.976 | 4.419 | 5.879 | 7.348 | 8.819 | 10.290 | 11.760 | 13.225 | 14.687 | 16.143 | 17.594 |
| 8 | 3.079 | 4.608 | 6.160 | 7.722 | 9.287 | 10.852 | 12.414 | 13.973 | 15.526 | 17.073 | 18.613 |
| 9 | 3.164 | 4.774 | 6.410 | 8.058 | 9.709 | 11.361 | 13.009 | 14.653 | 16.291 | 17.921 | 19.544 |
| 10 | 3.237 | 4.920 | 6.634 | 8.362 | 10.094 | 11.826 | 13.555 | 15.278 | 16.994 | 18.702 | 20.400 |
| 11 | 3.298 | 5.049 | 6.836 | 8.639 | 10.446 | 12.254 | 14.057 | 15.855 | 17.644 | 19.423 | 21.192 |
| 12 | 3.349 | 5.165 | 7.020 | 8.892 | 10.771 | 12.649 | 14.523 | 16.390 | 18.248 | 20.095 | 21.929 |
| 13 | 3.393 | 5.267 | 7.187 | 9.125 | 11.071 | 13.016 | 14.956 | 16.889 | 18.811 | 20.721 | 22.617 |
| 14 | 3.429 | 5.360 | 7.339 | 9.340 | 11.349 | 13.358 | 15.361 | 17.355 | 19.338 | 21.307 | 23.262 |
| 15 | 3.460 | 5.442 | 7.479 | 9.539 | 11.608 | 13.677 | 15.739 | 17.792 | 19.832 | 21.858 | 23.867 |
| 17 | 3.485 | 5.516 | 7.607 | 9.724 | 11.850 | 13.975 | 16.094 | 18.203 | 20.298 | 22.377 | 24.437 |
| 1 | 5.583 | 7.725 | 9.895 | 12.076 | 14.256 | 16.429 | 18.590 | 20.737 | 22.866 | 24.975 |  |
| 105 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 3.521 | 5.642 | 7.834 | 10.055 | 12.287 | 14.519 | 16.743 | 18.955 | 21.151 | 23.328 | 25.483 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 3.533 | 5.696 | 7.934 | 10.204 | 12.486 | 14.767 | 17.041 | 19.300 | 21.543 | 23.765 | 25.964 |
| 20 | 3.542 | 5.744 | 8.026 | 10.343 | 12.672 | 15.001 | 17.321 | 19.627 | 21.915 | 24.180 | 26.420 |
| 21 | 3.548 | 5.787 | 8.111 | 10.472 | 12.847 | 15.222 | 17.587 | 19.937 | 22.267 | 24.573 | 26.853 |
| 22 | 3.552 | 5.825 | 8.189 | 10.594 | 13.012 | 15.431 | 17.839 | 20.231 | 22.601 | 24.947 | 27.264 |
| 23 | 3.553 | 5.859 | 8.262 | 10.707 | 13.168 | 15.628 | 18.077 | 20.509 | 22.919 | 25.302 | 27.655 |
| 24 | 3.551 | 5.889 | 8.329 | 10.813 | 13.314 | 15.815 | 18.304 | 20.774 | 23.222 | 25.640 | 28.027 |
| 25 | 3.548 | 5.915 | 8.390 | 10.913 | 13.452 | 15.992 | 18.519 | 21.026 | 23.509 | 25.962 | 28.382 |
| 26 | 3.543 | 5.938 | 8.447 | 11.006 | 13.583 | 16.159 | 18.723 | 21.266 | 23.783 | 26.269 | 28.719 |
| 27 | 3.536 | 5.957 | 8.499 | 11.093 | 13.706 | 16.318 | 18.917 | 21.495 | 24.044 | 26.561 | 29.041 |
| 28 | 3.527 | 5.974 | 8.547 | 11.174 | 13.822 | 16.469 | 19.102 | 21.712 | 24.293 | 26.840 | 29.348 |
| 29 | 3.517 | 5.988 | 8.591 | 11.251 | 13.932 | 16.612 | 19.277 | 21.919 | 24.531 | 27.106 | 29.640 |
| 20 | 3.506 | 6.000 | 8.631 | 11.322 | 14.035 | 16.747 | 19.444 | 22.117 | 24.757 | 27.360 | 29.920 |

Table A. 6
European-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 95$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.192 | 0.490 | 0.874 | 1.308 | 1.774 | 2.262 | 2.764 | 3.278 | 3.798 | 4.325 | 4.856 |
| 2 | 0.494 | 1.037 | 1.667 | 2.345 | 3.053 | 3.779 | 4.518 | 5.265 | 6.019 | 6.777 | 7.538 |
| 3 | 0.750 | 1.470 | 2.278 | 3.134 | 4.018 | 4.920 | 5.833 | 6.754 | 7.681 | 8.611 | 9.543 |
| 4 | 0.964 | 1.825 | 2.777 | 3.777 | 4.806 | 5.852 | 6.909 | 7.973 | 9.042 | 10.113 | 11.186 |
| 5 | 1.144 | 2.125 | 3.199 | 4.324 | 5.476 | 6.647 | 7.827 | 9.015 | 10.206 | 11.400 | 12.593 |
| 6 | 1.298 | 2.383 | 3.565 | 4.799 | 6.061 | 7.342 | 8.632 | 9.929 | 11.229 | 12.530 | 13.830 |
| 7 | 1.430 | 2.608 | 3.887 | 5.219 | 6.581 | 7.960 | 9.350 | 10.746 | 12.144 | 13.542 | 14.937 |
| 8 | 1.546 | 2.806 | 4.173 | 5.595 | 7.048 | 8.518 | 9.999 | 11.484 | 12.972 | 14.457 | 15.940 |
| 9 | 1.647 | 2.983 | 4.430 | 5.935 | 7.471 | 9.026 | 10.590 | 12.159 | 13.728 | 15.295 | 16.857 |
| 10 | 1.736 | 3.142 | 4.663 | 6.245 | 7.859 | 9.491 | 11.133 | 12.779 | 14.424 | 16.066 | 17.702 |
| 11 | 1.815 | 3.285 | 4.876 | 6.529 | 8.215 | 9.920 | 11.635 | 13.353 | 15.069 | 16.780 | 18.485 |
| 12 | 1.885 | 3.414 | 5.070 | 6.790 | 8.544 | 10.318 | 12.101 | 13.886 | 15.669 | 17.445 | 19.214 |
| 13 | 1.947 | 3.531 | 5.248 | 7.031 | 8.850 | 10.688 | 12.535 | 14.384 | 16.229 | 18.067 | 19.895 |
| 14 | 2.002 | 3.638 | 5.412 | 7.255 | 9.135 | 11.034 | 12.941 | 14.850 | 16.754 | 18.650 | 20.534 |
| 15 | 2.051 | 3.736 | 5.563 | 7.463 | 9.400 | 11.357 | 13.323 | 15.288 | 17.247 | 19.197 | 21.135 |
| 16 | 2.094 | 3.825 | 5.703 | 7.657 | 9.649 | 11.661 | 13.681 | 15.700 | 17.712 | 19.714 | 21.701 |
| 17 | 2.133 | 3.906 | 5.833 | 7.838 | 9.882 | 11.947 | 14.019 | 16.089 | 18.151 | 20.201 | 22.236 |


| 18 | 2.168 | 3.981 | 5.954 | 8.007 | 10.101 | 12.216 | 14.337 | 16.456 | 18.566 | 20.663 | 22.742 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 2.198 | 4.050 | 6.067 | 8.166 | 10.308 | 12.470 | 14.639 | 16.804 | 18.960 | 21.100 | 23.222 |
| 20 | 2.225 | 4.113 | 6.171 | 8.315 | 10.502 | 12.710 | 14.924 | 17.134 | 19.333 | 21.515 | 23.677 |
| 21 | 2.249 | 4.170 | 6.269 | 8.455 | 10.686 | 12.937 | 15.195 | 17.447 | 19.687 | 21.909 | 24.110 |
| 22 | 2.270 | 4.223 | 6.360 | 8.586 | 10.859 | 13.153 | 15.452 | 17.745 | 20.024 | 22.284 | 24.521 |
| 23 | 2.288 | 4.272 | 6.444 | 8.710 | 11.023 | 13.357 | 15.696 | 18.028 | 20.345 | 22.641 | 24.912 |
| 24 | 2.303 | 4.316 | 6.524 | 8.827 | 11.178 | 13.551 | 15.928 | 18.297 | 20.650 | 22.981 | 25.285 |
| 25 | 2.317 | 4.357 | 6.597 | 8.936 | 11.325 | 13.735 | 16.149 | 18.553 | 20.941 | 23.305 | 25.641 |
| 26 | 2.328 | 4.394 | 6.666 | 9.040 | 11.464 | 13.910 | 16.359 | 18.798 | 21.219 | 23.615 | 25.980 |
| 27 | 2.337 | 4.428 | 6.731 | 9.137 | 11.596 | 14.076 | 16.559 | 19.031 | 21.484 | 23.910 | 26.304 |
| 28 | 2.345 | 4.459 | 6.791 | 9.229 | 11.721 | 14.234 | 16.750 | 19.254 | 21.737 | 24.192 | 26.613 |
| 29 | 2.351 | 4.487 | 6.847 | 9.316 | 11.839 | 14.385 | 16.932 | 19.466 | 21.979 | 24.461 | 26.908 |
| 20 | 2.355 | 4.513 | 6.899 | 9.398 | 11.952 | 14.528 | 17.106 | 19.669 | 22.209 | 24.719 | 27.190 |

Table A. 7
European-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 90$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.007 | 0.058 | 0.187 | 0.394 | 0.666 | 0.989 | 1.352 | 1.745 | 2.161 | 2.596 | 3.046 |
| 2 | 0.066 | 0.274 | 0.622 | 1.074 | 1.599 | 2.175 | 2.788 | 3.429 | 4.089 | 4.766 | 5.453 |
| 3 | 0.162 | 0.524 | 1.051 | 1.688 | 2.399 | 3.159 | 3.954 | 4.773 | 5.611 | 6.461 | 7.322 |
| 4 | 0.268 | 0.765 | 1.440 | 2.228 | 3.088 | 3.997 | 4.938 | 5.903 | 6.884 | 7.877 | 8.878 |
| 5 | 0.374 | 0.988 | 1.790 | 2.706 | 3.693 | 4.728 | 5.794 | 6.883 | 7.987 | 9.101 | 10.223 |
| 6 | 0.474 | 1.193 | 2.105 | 3.132 | 4.232 | 5.378 | 6.554 | 7.752 | 8.964 | 10.185 | 11.412 |
| 7 | 0.568 | 1.380 | 2.390 | 3.518 | 4.717 | 5.962 | 7.238 | 8.534 | 9.842 | 11.160 | 12.482 |
| 8 | 0.656 | 1550 | 2.650 | 3.868 | 5.158 | 6.494 | 7.860 | 9.245 | 10.642 | 12.046 | 13.454 |
| 9 | 0.736 | 1.707 | 2.887 | 4.189 | 5.562 | 6.982 | 8.430 | 9.897 | 11.375 | 12.860 | 14.346 |
| 10 | 0.811 | 1.851 | 3.106 | 4.484 | 5.935 | 7.431 | 8.956 | 10.499 | 12.052 | 13.611 | 15.170 |
| 11 | 0.879 | 1.983 | 3.308 | 4.757 | 6.279 | 7.848 | 9.445 | 11.058 | 12.681 | 14.309 | 15.935 |
| 12 | 0.942 | 2.105 | 3.494 | 5.010 | 6.600 | 8.236 | 9.899 | 11.579 | 13.268 | 14.959 | 16.648 |
| 13 | 1.000 | 2.218 | 3.667 | 5.245 | 6.899 | 8.598 | 10.325 | 12.067 | 13.817 | 15.569 | 17.316 |
| 14 | 1.053 | 2.323 | 3.828 | 5.465 | 7.179 | 8.938 | 10.724 | 12.525 | 14.333 | 16.141 | 17.944 |
| 15 | 1.102 | 2.420 | 3.979 | 5.671 | 7.441 | 9.257 | 11.100 | 12.957 | 14.819 | 16.680 | 18.535 |
| 16 | 1146 | 2.510 | 4.119 | 5.864 | 7.688 | 9.558 | 11.454 | 13.364 | 15.278 | 17.189 | 19.092 |
| 17 | 1.188 | 2.593 | 4.250 | 6.046 | 7.920 | 9.841 | 11.788 | 13.748 | 15.712 | 17.670 | 19.620 |


| 18 | 1.226 | 2.671 | 4373 | 6.216 | 8.140 | 10.110 | 12.105 | 14.113 | 16.123 | 18.126 | 20.119 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 1.261 | 2.744 | 4.489 | 6.377 | 8.347 | 10.363 | 12.405 | 14.458 | 16.512 | 18.559 | 20.594 |
| 20 | 1.293 | 2.811 | 4.597 | 6.529 | 8.543 | 10.604 | 12690 | 14.787 | 16.883 | 18.971 | 21.044 |
| 21 | 1.322 | 2.874 | 4.699 | 6.672 | 8.729 | 10.832 | 12.961 | 15.099 | 17.235 | 19.362 | 21.473 |
| 22 | 1.349 | 2.933 | 4.794 | 6.807 | 8.905 | 11.049 | 13.218 | 15.396 | 17.571 | 19.735 | 21.881 |
| 23 | 1.373 | 2.987 | 4.884 | 6.935 | 9.072 | 11.256 | 13.464 | 15.680 | 17.891 | 20.090 | 22.270 |
| 24 | 1.396 | 3.038 | 4.969 | 7.056 | 9.230 | 11.452 | 13.697 | 15.950 | 18.196 | 20.429 | 22.641 |
| 25 | 1.416 | 3.086 | 5.049 | 7.171 | 9.381 | 11.639 | 13.920 | 16.207 | 18.488 | 20.753 | 22.995 |
| 26 | 1.435 | 3.130 | 5.124 | 7.280 | 9.525 | 11.817 | 14.133 | 16.454 | 18.766 | 21.062 | 23.334 |
| 27 | 1452 | 3.171 | 5.195 | 7.383 | 9.661 | 11.987 | 14.336 | 16.689 | 19.032 | 21.357 | 23.657 |
| 28 | 1.467 | 3210 | 5.262 | 7.481 | 9.791 | 12.150 | 14.530 | 16.914 | 19.287 | 21.640 | 23.966 |
| 29 | 1.481 | 3.245 | 5.325 | 7.573 | 9.915 | 12.304 | 14.716 | 17.129 | 19.530 | 21.911 | 24.262 |
| 20 | 1.493 | 3.278 | 5.384 | 7.661 | 10.032 | 12.452 | 14.893 | 17.335 | 19.764 | 22.170 | 24.545 |

Table A. 8
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 8 5}$

## Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.003 | 0.023 | 0.080 | 0.188 | 0.347 | 0.555 | 0.806 | 1.092 | 1.410 | 1.752 |
| 2 | 0.004 | 0.046 | 0.175 | 0.404 | 0.723 | 1.118 | 1.571 | 2.072 | 2.609 | 3.175 | 3.764 |
| 3 | 0.020 | 0.139 | 0.400 | 0.795 | 1.295 | 1.875 | 2.515 | 3.200 | 3.919 | 4.665 | 5.432 |
| 4 | 0.050 | 0.256 | 0.645 | 1.185 | 1.837 | 2.568 | 3.359 | 4.192 | 5.059 | 5.949 | 6.859 |
| 5 | 0.088 | 0.383 | 0.889 | 1.556 | 2.337 | 3.198 | 4.116 | 5.076 | 6.067 | 7.081 | 8.111 |
| 6 | 0.132 | 0.512 | 1.123 | 1.903 | 2.797 | 3.772 | 4.802 | 5.873 | 6.973 | 8.094 | 9.230 |
| 7 | 0.178 | 0.638 | 1.346 | 2.226 | 3.222 | 4.298 | 5.429 | 6.599 | 7.796 | 9.013 | 10.244 |
| 8 | 0.226 | 0.760 | 1.556 | 2.527 | 3.616 | 4.783 | 6.005 | 7.264 | 8.550 | 9.854 | 11.170 |
| 9 | 0.273 | 0.877 | 1.753 | 2.809 | 3.982 | 5.233 | 6.538 | 7.879 | 9.246 | 10.629 | 12.024 |
| 10 | 0.319 | 0.989 | 1.939 | 3.072 | 4.323 | 5.652 | 7.033 | 8.451 | 9.892 | 11.349 | 12.815 |
| 11 | 0.364 | 1.094 | 2.113 | 3.318 | 4.641 | 6.043 | 7.496 | 8.984 | 10.494 | 12.019 | 13.553 |
| 12 | 0.407 | 1.194 | 2.278 | 3.549 | 4.940 | 6.409 | 7.929 | 9.483 | 11.058 | 12.647 | 14.242 |
| 13 | 0.449 | 1.289 | 2.432 | 3.767 | 5.221 | 6.754 | 8.336 | 9.952 | 11.588 | 13.236 | 14.890 |
| 14 | 0.488 | 1.378 | 2.578 | 3.972 | 5.486 | 7.078 | 8.720 | 10.394 | 12.087 | 13.791 | 15.499 |
| 15 | 0.525 | 1.462 | 2.716 | 4.165 | 5.736 | 7.384 | 9.082 | 10.811 | 12.558 | 14.315 | 16.074 |
| 16 | 0.561 | 1.542 | 2.846 | 4.348 | 5.972 | 7.674 | 9.425 | 11.206 | 13.004 | 14.811 | 16.618 |
| 17 | 0.594 | 1.617 | 2.969 | 4.520 | 6.196 | 7.948 | 9.749 | 11.580 | 13.427 | 15.281 | 17.133 |


| 18 | 0.626 | 1.688 | 3.085 | 4.684 | 6.408 | 8.209 | 10.058 | 11.935 | 13.828 | 15.727 | 17.622 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.656 | 1.755 | 3.195 | 4.839 | 6.609 | 8.456 | 10.351 | 12.273 | 14.210 | 16.151 | 18.087 |
| 20 | 0.684 | 1.818 | 3.299 | 4.986 | 6.800 | 8.691 | 10.630 | 12.595 | 14.573 | 16.554 | 18.529 |
| 21 | 0.710 | 1.878 | 3.397 | 5.126 | 6.982 | 8.916 | 10.896 | 12.902 | 14.9204 | 16.939 | 18.950 |
| 22 | 0.735 | 1.935 | 3.491 | 5.259 | 7.155 | 9.129 | 11.149 | 13.194 | 15.250 | 17.306 | 19.352 |
| 23 | 0.758 | 1.988 | 3.579 | 5.385 | 7.320 | 9.333 | 11.391 | 13.474 | 15.566 | 17.656 | 19.735 |
| 24 | 0.780 | 2.039 | 3.664 | 5.506 | 7.478 | 9.527 | 11.622 | 13.741 | 15.868 | 17.991 | 20.101 |
| 25 | 0.801 | 2.086 | 3.743 | 5.620 | 7.628 | 9.713 | 11.843 | 13.996 | 16.156 | 18.311 | 20.452 |
| 26 | 0.820 | 2.131 | 3.819 | 5.729 | 7.771 | 9.891 | 12.055 | 14.241 | 16.433 | 18.617 | 20.786 |
| 27 | 0.838 | 2.174 | 3.891 | 5.833 | 7.908 | 10.060 | 12.257 | 14.475 | 16.697 | 18.911 | 21.107 |
| 28 | 0.855 | 2.214 | 3.960 | 5.932 | 8.038 | 10.223 | 12.451 | 14.699 | 16.950 | 19.192 | 21.414 |
| 29 | 0.870 | 2.252 | 4.024 | 6.027 | 8.163 | 10.379 | 12.637 | 14.914 | 17.193 | 19.461 | 21.708 |
| 20 | 0.885 | 2.287 | 4.086 | 6.117 | 8.283 | 10.527 | 12.815 | 15.120 | 17.426 | 19.719 | 21.990 |

Table A. 9
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 8 0}$

## Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.001 | 0.010 | 0.037 | 0.093 | 0.184 | 0.312 | 0.477 | 0.676 | 0.907 |
| 2 | 0.000 | 0.005 | 0.035 | 0.119 | 0.273 | 0.500 | 0.792 | 1.143 | 1.541 | 1.981 | 2.454 |
| 3 | 0.001 | 0.025 | 0.120 | 0.318 | 0.619 | 1.012 | 1.482 | 2.013 | 2.595 | 3.216 | 3.870 |
| 4 | 0.006 | 0.065 | 0.242 | 0.556 | 0.994 | 1.533 | 2.152 | 2.834 | 3.564 | 4.333 | 5.132 |
| 5 | 0.014 | 0.118 | 0.382 | 0.808 | 1.369 | 2.036 | 2.784 | 3.593 | 4.450 | 5.343 | 6.265 |
| 6 | 0.026 | 0.182 | 0.530 | 1. 059 | 1.731 | 2.512 | 3.373 | 4.294 | 5.262 | 6.264 | 7.293 |
| 7 | 0.042 | 0.251 | 0.681 | 1.305 | 2.078 | 2.960 | 3.922 | 4.944 | 6.010 | 7.109 | 8.232 |
| 8 | 0.060 | 0.323 | 0.831 | 1.543 | 2.408 | 3.382 | 4.436 | 5.548 | 6.703 | 7.889 | 9.099 |
| 9 | 0.081 | 0.396 | 0.977 | 1.771 | 2.720 | 3.779 | 4.917 | 6.112 | 7.348 | 8.614 | 9.902 |
| 10 | 0.102 | 0.469 | 1.120 | 1.989 | 3.016 | 4.153 | 5.369 | 6.640 | 7.951 | 9.291 | 10.650 |
| 11 | 0.125 | 0.542 | 1.257 | 2.198 | 3.297 | 4.507 | 5.794 | 7.136 | 8.517 | 9.924 | 11.350 |
| 12 | 0.148 | 0.612 | 1.389 | 2.396 | 3.563 | 4.841 | 6.195 | 7.603 | 9.049 | 10.519 | 12.007 |
| 13 | 0.171 | 0.681 | 1.516 | 2.585 | 3.816 | 5.158 | 6.575 | 8.045 | 9.551 | 11.081 | 12.626 |
| 14 | 0.194 | 0.748 | 1.637 | 2.766 | 4.057 | 5.458 | 6.934 | 8.462 | 10.025 | 11.611 | 13.210 |
| 15 | 0.217 | 0.813 | 1.754 | 2.938 | 4.285 | 5.743 | 7.275 | 8.858 | 10.475 | 12.113 | 13.763 |
| 16 | 0.239 | 0.875 | 1.865 | 3.102 | 4.503 | 6.014 | 7.600 | 9.234 | 10.902 | 12.589 | 14.287 |
| 17 | 0.261 | 0.935 | 1.972 | 3.258 | 4.710 | 6.272 | 7.908 | 9.592 | 11.308 | 13.042 | 14.785 |


| 18 | 0.283 | 0.993 | 2.074 | 3.408 | 4.908 | 6.519 | 8.202 | 9.933 | 11.694 | 13.472 | 15.258 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.303 | 1.049 | 2.171 | 3.550 | 5.097 | 6.754 | 8.482 | 10.258 | 12.062 | 13.883 | 15.709 |
| 20 | 0.323 | 1.102 | 2.265 | 3.687 | 5.277 | 6.978 | 8.750 | 10.568 | 12.414 | 14.274 | 16.139 |
| 21 | 0.343 | 1.152 | 2.354 | 3.817 | 5.450 | 7.192 | 9.006 | 10.865 | 12.750 | 14.648 | 16.549 |
| 22 | 0.361 | 1.201 | 2.439 | 3.942 | 5.615 | 7.398 | 9.251 | 11.148 | 13.071 | 15.005 | 16.940 |
| 23 | 0.379 | 1.248 | 2.521 | 4.061 | 5.773 | 7.594 | 9.485 | 11.420 | 13.378 | 15.347 | 17.315 |
| 24 | 0.396 | 1.292 | 2.599 | 4.175 | 5.924 | 7.782 | 9.710 | 11.680 | 13.673 | 15.675 | 17.673 |
| 25 | 0.413 | 1.335 | 2.674 | 4.285 | 6.069 | 7.963 | 9.925 | 11.929 | 13.955 | 15.988 | 18.016 |
| 26 | 0.428 | 1.376 | 2.745 | 4.389 | 6.207 | 8.135 | 10.132 | 12.168 | 14.226 | 16.289 | 18.345 |
| 27 | 0.443 | 1.415 | 2.814 | 4.490 | 6.341 | 8.301 | 10.330 | 12.398 | 14.485 | 16.577 | 18.660 |
| 28 | 0.457 | 1.452 | 2.879 | 4.586 | 6.468 | 8.461 | 10.520 | 12.618 | 14.734 | 16.853 | 18.962 |
| 29 | 0.471 | 1.487 | 2.942 | 4.678 | 6.591 | 8.613 | 10.703 | 12.830 | 14.974 | 17.119 | 19.252 |
| 30 | 0.484 | 1.521 | 3.002 | 4.766 | 6.708 | 8.760 | 10.878 | 13.033 | 15.204 | 17.373 | 19.530 |

Table A. 10
European-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 75$

## Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.018 | 0.047 | 0.098 | 0.174 | 0.279 | 0.412 |
| 2 | 0.000 | 0.000 | 0.004 | 0.026 | 0.083 | 0.189 | 0.349 | 0.564 | 0.830 | 1.142 | 1.494 |
| 3 | 0.000 | 0.003 | 0.027 | 0.104 | 0.255 | 0.486 | 0.795 | 1.173 | 1.611 | 2.098 | 2.628 |
| 4 | 0.000 | 0.012 | 0.073 | 0.224 | 0.480 | 0.837 | 1.284 | 1.805 | 2.388 | 3.022 | 3.697 |
| 5 | 0.001 | 0.028 | 0.137 | 0.370 | 0.730 | 1.205 | 1.774 | 2.421 | 3.130 | 3.889 | 4.687 |
| 6 | 0.003 | 0.051 | 0.216 | 0.531 | 0.990 | 1.572 | 2.252 | 3.010 | 3.829 | 4.698 | 5.604 |
| 7 | 0.007 | 0.081 | 0.303 | 0.699 | 1.250 | 1.930 | 2.710 | 3.568 | 4.487 | 5.453 | 6.455 |
| 8 | 0.012 | 0.115 | 0.396 | 0.869 | 1.507 | 2.277 | 3.148 | 4.097 | 5.105 | 6.159 | 7.247 |
| 9 | 0.018 | 0.153 | 0.491 | 1.038 | 1.757 | 2.611 | 3.566 | 4.597 | 5.687 | 6.821 | 7.988 |
| 10 | 0.025 | 0.193 | 0.589 | 1.205 | 2.000 | 2.930 | 3.963 | 5.071 | 6.236 | 7.444 | 8.682 |
| 11 | 0.034 | 0.235 | 0.686 | 1.368 | 2.234 | 3.237 | 4.341 | 5.520 | 6.755 | 8.031 | 9.336 |
| 12 | 0.043 | 0.278 | 0.782 | 1.527 | 2.459 | 3.530 | 4.701 | 5.947 | 7.247 | 8.585 | 9.952 |
| 13 | 0.054 | 0.322 | 0.876 | 1.681 | 2.676 | 3.810 | 5.045 | 6.352 | 7.713 | 9.111 | 10.535 |
| 14 | 0.064 | 0.366 | 0.969 | 1.830 | 2.884 | 4.078 | 5.372 | 6.738 | 8.156 | 9.609 | 11.087 |
| 15 | 0.075 | 0.409 | 1.060 | 1.975 | 3.085 | 4.335 | 5.685 | 7.106 | 8.577 | 10.083 | 11.612 |
| 16 | 0.087 | 0.452 | 1.148 | 2.114 | 3.277 | 4.581 | 5.984 | 7.457 | 8.979 | 10.534 | 12.110 |
| 17 | 0.098 | 0.495 | 1.234 | 2.248 | 3.462 | 4.817 | 6.270 | 7.792 | 9.362 | 10.963 | 12.585 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.110 | 0.536 | 1.317 | 2.378 | 3.640 | 5.043 | 6.544 | 8.113 | 9.728 | 11.374 | 13.037 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.122 | 0.577 | 1.397 | 2.503 | 3.811 | 5.260 | 6.806 | 8.420 | 10.078 | 11.765 | 13.470 |
| 20 | 0.134 | 0.617 | 1.475 | 2.623 | 3.975 | 5.468 | 7.058 | 8.714 | 10.413 | 12.140 | 13.882 |
| 21 | 0.145 | 0.656 | 1.551 | 2.739 | 4.133 | 5.668 | 7.299 | 8.996 | 10.734 | 12.499 | 14.277 |
| 22 | 0.157 | 0.694 | 1.624 | 2.851 | 4.285 | 5.860 | 7.531 | 9.266 | 11.042 | 12.843 | 14.655 |
| 23 | 0.168 | 0.730 | 1.694 | 2.958 | 4.431 | 6.045 | 7.754 | 9.525 | 11.337 | 13.172 | 15.017 |
| 24 | 0.179 | 0.766 | 1.762 | 3.062 | 4.571 | 6.222 | 7.968 | 9.775 | 11.621 | 13.488 | 15.365 |
| 25 | 0.190 | 0.800 | 1.827 | 3.162 | 4.707 | 6.393 | 8.173 | 10.014 | 11.893 | 13.792 | 15.698 |
| 26 | 0.201 | 0.834 | 1.891 | 3.258 | 4.837 | 6.557 | 8.371 | 10.245 | 12.154 | 14.083 | 16.017 |
| 27 | 0.211 | 0.866 | 1.952 | 3.351 | 4.963 | 6.716 | 8.561 | 10.466 | 12.406 | 14.363 | 16.324 |
| 28 | 0.221 | 0.897 | 2.010 | 3.440 | 5.083 | 6.868 | 8.745 | 10.679 | 12.648 | 14.632 | 16.618 |
| 29 | 0.231 | 0.927 | 2.067 | 3.526 | 5.200 | 7.015 | 8.921 | 10.885 | 12.881 | 14.891 | 16.901 |
| 30 | 0.240 | 0.956 | 2.122 | 3.609 | 5.312 | 7.156 | 9.091 | 11.082 | 13.105 | 15.140 | 17.173 |

Table A. 11
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 70$

## Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.009 | 0.023 | 0.051 | 0.096 | 0.160 |
| 2 | 0.000 | 0.000 | 0.000 | 0.004 | 0.019 | 0.058 | 0.130 | 0.243 | 0.399 | 0.598 | 0.838 |
| 3 | 0.000 | 0.000 | 0.004 | 0.026 | 0.087 | 0.203 | 0.381 | 0.623 | 0.925 | 1.280 | 1.683 |
| 4 | 0.000 | 0.001 | 0.017 | 0.075 | 0.202 | 0.410 | 0.702 | 1.070 | 1.505 | 2.000 | 2.544 |
| 5 | 0.000 | 0.005 | 0.040 | 0.146 | 0.348 | 0.653 | 1.053 | 1.537 | 2.093 | 2.710 | 3.376 |
| 6 | 0.000 | 0.011 | 0.073 | 0.234 | 0.514 | 0.912 | 1.414 | 2.005 | 2.669 | 3.393 | 4.167 |
| 7 | 0.001 | 0.020 | 0.115 | 0.334 | 0.692 | 1.178 | 1.775 | 2.463 | 3.224 | 4.045 | 4.914 |
| 8 | 0.002 | 0.033 | 0.164 | 0.443 | 0.876 | 1.446 | 2.130 | 2.906 | 3.757 | 4.665 | 5.621 |
| 9 | 0.003 | 0.049 | 0.218 | 0.556 | 1.061 | 1.710 | 2.475 | 3.334 | 4.265 | 5.254 | 6.288 |
| 10 | 0.005 | 0.067 | 0.276 | 0.673 | 1.246 | 1.969 | 2.810 | 3.744 | 4.751 | 5.814 | 6.920 |
| 11 | 0.007 | 0.087 | 0.337 | 0.790 | 1.429 | 2.221 | 3.133 | 4.138 | 5.215 | 6.346 | 7.518 |
| 12 | 0.010 | 0.109 | 0.399 | 0.908 | 1.609 | 2.467 | 3.445 | 4.516 | 5.657 | 6.852 | 8.086 |
| 13 | 0.013 | 0.132 | 0.463 | 1.024 | 1.785 | 2.705 | 3.746 | 4.879 | 6.080 | 7.334 | 8.626 |
| 17 | 0.026 | 0.208 | 0.655 | 1.364 | 2.287 | 3.373 | 4.582 | 5.879 | 7.242 | 8.653 | 10.096 |
| 17 | 0.031 | 0.235 | 0.718 | 1.473 | 2.445 | 3.581 | 4.840 | 6.187 | 7.598 | 9.054 | 10.543 |
| 15 | 0.021 | 0.182 | 0.591 | 1.253 | 2.124 | 3.158 | 4.314 | 5.559 | 6.872 | 8.233 | 9.629 |
| 17 | 0.527 | 1.140 | 1.957 | 2.935 | 4.035 | 5.226 | 6.485 | 7.794 | 9.139 |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.036 | 0.261 | 0.781 | 1.579 | 2.598 | 3.782 | 5.088 | 6.482 | 7.938 | 9.439 | 10.970 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.041 | 0.288 | 0.842 | 1.682 | 2.746 | 3.976 | 5.327 | 6.766 | 8.265 | 9.808 | 11.379 |
| 20 | 0.047 | 0.315 | 0.903 | 1.783 | 2.890 | 4.164 | 5.558 | 7.038 | 8.579 | 10.161 | 11.770 |
| 21 | 0.053 | 0.341 | 0.962 | 1.880 | 3.029 | 4.344 | 5.780 | 7.301 | 8.881 | 10.501 | 12.146 |
| 22 | 0.059 | 0.367 | 1.019 | 1.976 | 3.163 | 4.519 | 5.995 | 7.554 | 9.171 | 10.827 | 12.506 |
| 23 | 0.065 | 0.393 | 1.076 | 2.068 | 3.294 | 4.688 | 6.201 | 7.797 | 9.450 | 11.140 | 12.852 |
| 24 | 0.071 | 0.419 | 1.131 | 2.158 | 3.420 | 4.851 | 6.400 | 8.032 | 9.719 | 11.441 | 13.184 |
| 25 | 0.077 | 0.444 | 1.185 | 2.245 | 3.542 | 5.008 | 6.593 | 8.258 | 9.978 | 11.731 | 13.503 |
| 26 | 0.083 | 0.468 | 1.237 | 2.329 | 3.660 | 5.161 | 6.778 | 8.476 | 10.227 | 12.010 | 13.810 |
| 27 | 0.089 | 0.492 | 1.288 | 2.411 | 3.775 | 5.308 | 6.958 | 8.687 | 10.467 | 12.279 | 14.106 |
| 28 | 0.095 | 0.516 | 1.338 | 2.490 | 3.885 | 5.450 | 7.131 | 8.890 | 10.699 | 12.538 | 14.390 |
| 29 | 0.101 | 0.539 | 1.386 | 2.567 | 3.993 | 5.587 | 7.298 | 9.086 | 10.922 | 12.787 | 14.664 |
| 30 | 0.106 | 0.562 | 1.433 | 2.642 | 4.096 | 5.720 | 7.459 | 9.275 | 11.138 | 13.027 | 14.927 |

Table A. 12
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 6 5}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.012 | 0.026 | 0.051 |
| 2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.014 | 0.040 | 0.089 | 0.167 | 0.279 | 0.424 |
| 3 | 0.000 | 0.000 | 0.000 | 0.005 | 0.024 | 0.071 | 0.159 | 0.295 | 0.483 | 0.720 | 1.005 |
| 4 | 0.000 | 0.000 | 0.003 | 0.020 | 0.071 | 0.176 | 0.345 | 0.581 | 0.882 | 1.242 | 1.657 |
| 5 | 0.000 | 0.001 | 0.009 | 0.048 | 0.144 | 0.317 | 0.573 | 0.908 | 1.318 | 1.792 | 2.322 |
| 6 | 0.000 | 0.002 | 0.020 | 0.088 | 0.238 | 0.483 | 0.825 | 1.256 | 1.766 | 2.343 | 2.978 |
| 7 | 0.000 | 0.004 | 0.036 | 0.140 | 0.346 | 0.664 | 1.090 | 1.610 | 2.213 | 2.884 | 3.613 |
| 8 | 0.000 | 0.007 | 0.057 | 0.200 | 0.465 | 0.855 | 1.360 | 1.964 | 2.652 | 3.409 | 4.223 |
| 9 | 0.000 | 0.012 | 0.083 | 0.268 | 0.591 | 1.050 | 1.630 | 2.313 | 3.080 | 3.916 | 4.808 |
| 10 | 0.001 | 0.019 | 0.113 | 0.340 | 0.721 | 1.247 | 1.899 | 2.655 | 3.496 | 4.405 | 5.368 |
| 11 | 0.001 | 0.026 | 0.146 | 0.417 | 0.854 | 1.444 | 2.163 | 2.988 | 3.897 | 4.874 | 5.903 |
| 12 | 0.002 | 0.036 | 0.181 | 0.496 | 0.988 | 1.639 | 2.422 | 3.311 | 4.284 | 5.324 | 6.415 |
| 13 | 0.002 | 0.046 | 0.219 | 0.577 | 1.122 | 1.831 | 2.674 | 3.624 | 4.658 | 5.757 | 6.905 |
| 14 | 0.003 | 0.058 | 0.259 | 0.659 | 1.255 | 2.020 | 2.920 | 3.928 | 5.018 | 6.172 | 7.374 |
| 15 | 0.005 | 0.070 | 0.299 | 0.741 | 1.387 | 2.205 | 3.160 | 4.221 | 5.365 | 6.571 | 7.824 |
| 16 | 0.006 | 0.084 | 0.341 | 0.824 | 1.517 | 2.385 | 3.392 | 4.505 | 5.699 | 6.954 | 8.254 |
| 17 | 0.008 | 0.098 | 0.383 | 0.906 | 1.645 | 2.562 | 3.617 | 4.779 | 6.021 | 7.322 | 8.667 |


| 18 | 0.009 | 0.112 | 0.426 | 0.987 | 1.770 | 2.734 | 3.836 | 5.044 | 6.331 | 7.677 | 9.064 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.011 | 0.127 | 0.469 | 1.067 | 1.893 | 2.901 | 4.048 | 5.300 | 6.630 | 8.017 | 9.445 |
| 20 | 0.014 | 0.143 | 0.512 | 1.146 | 2.013 | 3.063 | 4.254 | 5.548 | 6.919 | 8.346 | 9.811 |
| 21 | 0.016 | 0.159 | 0.554 | 1.224 | 2.130 | 3.222 | 4.453 | 5.787 | 7.197 | 8.662 | 10.163 |
| 22 | 0.018 | 0.175 | 0.597 | 1.301 | 2.245 | 3.375 | 4.646 | 6.019 | 7.466 | 8.966 | 10.501 |
| 23 | 0.021 | 0.191 | 0.639 | 1.376 | 2.356 | 3.525 | 4.833 | 6.242 | 7.725 | 9.259 | 10.827 |
| 24 | 0.024 | 0.207 | 0.680 | 1.449 | 2.465 | 3.670 | 5.014 | 6.459 | 7.976 | 9.542 | 11.141 |
| 25 | 0.026 | 0.224 | 0.721 | 1.521 | 2.571 | 3.811 | 5.189 | 6.668 | 8.218 | 9.815 | 11.444 |
| 26 | 0.029 | 0.240 | 0.761 | 1.592 | 2.675 | 3.947 | 5.359 | 6.871 | 8.451 | 10.079 | 11.735 |
| 27 | 0.032 | 0.256 | 0.801 | 1.661 | 2.775 | 4.080 | 5.524 | 7.067 | 8.677 | 10.333 | 12.016 |
| 28 | 0.035 | 0.272 | 0.840 | 1.728 | 2.873 | 4.209 | 5.684 | 7.256 | 8.895 | 10.578 | 12.287 |
| 29 | 0.038 | 0.288 | 0.878 | 1.793 | 2.968 | 4.335 | 5.839 | 7.440 | 9.106 | 10.815 | 12.548 |

Table A. 13
European-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 60$

## Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.005 | 0.013 |
| 2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.009 | 0.026 | 0.059 | 0.112 | 0.190 |
| 3 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.020 | 0.056 | 0.122 | 0.224 | 0.367 | 0.550 |
| 4 | 0.000 | 0.000 | 0.000 | 0.004 | 0.021 | 0.064 | 0.149 | 0.283 | 0.472 | 0.714 | 1.009 |
| 5 | 0.000 | 0.000 | 0.001 | 0.012 | 0.051 | 0.135 | 0.280 | 0.492 | 0.770 | 1.111 | 1.511 |
| 6 | 0.000 | 0.000 | 0.004 | 0.027 | 0.095 | 0.229 | 0.439 | 0.730 | 1.096 | 1.531 | 2.028 |
| 7 | 0.000 | 0.000 | 0.009 | 0.049 | 0.153 | 0.339 | 0.618 | 0.986 | 1.436 | 1.959 | 2.545 |
| 8 | 0.000 | 0.001 | 0.016 | 0.078 | 0.221 | 0.463 | 0.809 | 1.251 | 1.781 | 2.385 | 3.053 |
| 9 | 0.000 | 0.002 | 0.026 | 0.113 | 0.297 | 0.596 | 1.007 | 1.521 | 2.125 | 2.805 | 3.550 |
| 10 | 0.000 | 0.004 | 0.039 | 0.153 | 0.381 | 0.735 | 1.210 | 1.792 | 2.466 | 3.217 | 4.031 |
| 11 | 0.000 | 0.006 | 0.054 | 0.197 | 0.469 | 0.878 | 1.414 | 2.060 | 2.800 | 3.617 | 4.497 |
| 12 | 0.000 | 0.009 | 0.071 | 0.245 | 0.561 | 1.023 | 1.618 | 2.326 | 3.128 | 4.006 | 4.947 |
| 13 | 0.000 | 0.013 | 0.091 | 0.295 | 0.656 | 1.170 | 1.820 | 2.586 | 3.447 | 4.384 | 5.381 |
| 14 | 0.000 | 0.017 | 0.112 | 0.348 | 0.752 | 1.316 | 2.021 | 2.842 | 3.758 | 4.749 | 5.800 |
| 15 | 0.001 | 0.023 | 0.135 | 0.403 | 0.849 | 1.462 | 2.218 | 3.091 | 4.060 | 5.102 | 6.203 |
| 17 | 0.001 | 0.028 | 0.159 | 0.459 | 0.946 | 1.606 | 2.411 | 3.335 | 4.353 | 5.444 | 6.592 |
| 1 | 0.035 | 0.184 | 0.516 | 1.044 | 1.748 | 2.601 | 3.572 | 4.637 | 5.774 | 6.967 |  |
| 101 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.002 | 0.041 | 0.210 | 0.574 | 1.141 | 1.889 | 2.787 | 3.803 | 4.913 | 6.094 | 7.328 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.002 | 0.049 | 0.237 | 0.632 | 1.237 | 2.027 | 2.968 | 4.028 | 5.180 | 6.402 | 7.677 |
| 20 | 0.003 | 0.057 | 0.264 | 0.689 | 1.332 | 2.162 | 3.145 | 4.247 | 5.439 | 6.701 | 8.013 |
| 21 | 0.004 | 0.065 | 0.292 | 0.747 | 1.426 | 2.295 | 3.318 | 4.459 | 5.691 | 6.990 | 8.338 |
| 22 | 0.005 | 0.073 | 0.321 | 0.805 | 1.518 | 2.426 | 3.486 | 4.665 | 5.934 | 7.269 | 8.651 |
| 23 | 0.005 | 0.082 | 0.349 | 0.862 | 1.610 | 2.553 | 3.650 | 4.866 | 6.170 | 7.539 | 8.953 |
| 24 | 0.006 | 0.091 | 0.378 | 0.919 | 1.699 | 2.677 | 3.810 | 5.061 | 6.399 | 7.800 | 9.245 |
| 25 | 0.007 | 0.100 | 0.406 | 0.975 | 1.787 | 2.799 | 3.966 | 5.250 | 6.620 | 8.052 | 9.528 |
| 26 | 0.008 | 0.110 | 0.435 | 1.030 | 1.873 | 2.918 | 4.118 | 5.434 | 6.835 | 8.297 | 9.800 |
| 27 | 0.010 | 0.120 | 0.463 | 1.085 | 1.958 | 3.034 | 4.265 | 5.612 | 7.043 | 8.534 | 10.064 |
| 28 | 0.011 | 0.129 | 0.491 | 1.139 | 2.041 | 3.147 | 4.409 | 5.786 | 7.245 | 8.763 | 10.318 |
| 29 | 0.012 | 0.139 | 0.520 | 1.192 | 2.122 | 3.258 | 4.549 | 5.954 | 7.441 | 8.985 | 10.564 |
| 30 | 0.013 | 0.149 | 0.547 | 1.244 | 2.201 | 3.365 | 4.685 | 6.118 | 7.631 | 9.199 | 10.802 |

## APPENDIX BAMERICAN PUT PREMIUMS

The tables that follow show the option premiums for American-style LEAP puts based on the formulas contained in Chapter 15. They are based on a stock price of $\$ 100$ and exercise (strike) prices ranging from $\$ 120$ down to $\$ 60$ in steps of $\$ 5$. Dividend rates of zero, 1 percent, 2 percent, and 3 percent are considered. Each table is presented in matrix format, with volatilities ranging from a low of 0.150 through a high of 0.650 . Time to expiration ranges from 1 month to a maximum of 30 months. The risk-free interest rate in all instances is 6 percent.

To obtain premiums for stock prices other than $\$ 100$, simply scale the tables. For example, suppose you want to know the put premium for a stock price of $\$ 50$, strike price of $\$ 45$ for a volatility of 0.40 , expiration date 24 months away, and annual dividend rate of 2 percent. From Table B.33, we see that the premium for a $\$ 100$ stock with strike $\$ 90$ for volatility 0.40 , 24-month expiration, and 2 percent dividend is $\$ 13.430$. The premium for the $\$ 50$ stock with strike $\$ 45$ is therefore half this amount, or $\$ 6.715$ (i.e., $\$ 671.50$ per contract).

Suppose the stock price was $\$ 60$ and the strike price was $\$ 50$ for the same volatility and expiration. From Table B.34, we see that the premium for a $\$ 100$ stock with strike $\$ 85$ is $\$ 11.213$, and from Table B.35, we see that the premium for a $\$ 100$ stock with strike $\$ 80$ is $\$ 9.201$. Multiplying each of these figures by 0.60 shows that the premium for a $\$ 60$ stock with strike $\$ 51$ is $\$ 6.728$, and the premium for a $\$ 60$ stock with strike $\$ 48$ is $\$ 5.521$. The premium for the $\$ 60$ stock with strike $\$ 50$ is therefore $\$ 5.521+0.667 \times$ ( $\$ 6.728$ - $\$ 5.521$ ), or $\$ 6.326$ (i.e., $\$ 632.60$ per contract).

Table B. 1
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 120 /$ Dividend Rate $=\mathbf{0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.036 | 20.183 | 20.409 | 20.695 | 21.029 | 21.400 |
| 2 | 20.000 | 20.000 | 20.000 | 20.001 | 20.161 | 20.512 | 20.981 | 21.529 | 22.135 | 22.785 | 23.468 |
| 3 | 20.000 | 20.000 | 20.000 | 20.106 | 20.528 | 21.132 | 21.847 | 22.636 | 23.477 | 24.357 | 25.265 |
| 4 | 20.000 | 20.000 | 20.001 | 20.306 | 20.943 | 21.754 | 22.669 | 23.653 | 24.683 | 25.748 | 26.836 |
| 5 | 20.000 | 20.000 | 20.038 | 20.540 | 21.362 | 22.349 | 23.434 | 24.582 | 25.773 | 26.994 | 28.237 |
| 6 | 20.000 | 20.000 | 20.111 | 20.786 | 21.769 | 22.910 | 24.144 | 25.436 | 26.768 | 28.127 | 29.504 |
| 7 | 20.000 | 20.000 | 20.205 | 21.033 | 22.159 | 23.438 | 24.804 | 26.226 | 27.684 | 29.166 | 30.663 |
| 8 | 20.000 | 20.000 | 20.310 | 21.276 | 22.532 | 23.935 | 25.423 | 26.962 | 28.534 | 30.128 | 31.734 |
| 9 | 20.000 | 20.000 | 20.420 | 21.512 | 22.887 | 24.405 | 26.003 | 27.650 | 29.328 | 31.024 | 32.731 |
| 10 | 20.000 | 20.000 | 20.533 | 21.741 | 23.226 | 24.849 | 26.550 | 28.297 | 30.072 | 31.864 | 33.662 |
| 11 | 20.000 | 20.000 | 20.647 | 21.962 | 23.549 | 25.271 | 27.068 | 28.909 | 30.774 | 32.653 | 34.538 |
| 12 | 20.000 | 20.003 | 20.760 | 22.176 | 23.858 | 25.673 | 27.560 | 29.488 | 31.438 | 33.400 | 35.365 |
| 16 | 20.000 | 20.064 | 21.194 | 22.956 | 24.971 | 27.108 | 29.308 | 31.539 | 33.785 | 36.034 | 38.278 |
| 13 | 20.000 | 20.013 | 20.872 | 22.381 | 24.154 | 26.056 | 28.027 | 30.038 | 32.068 | 34.107 | 36.148 |
| 14 | 20.000 | 20.027 | 20.981 | 22.580 | 24.438 | 26.422 | 28.474 | 30.561 | 32.667 | 34.780 | 36.892 |
| 15 | 20.000 | 20.044 | 21.089 | 22.771 | 24.710 | 26.772 | 28.900 | 31.061 | 33.239 | 35.421 | 37.601 |
| 17 | 20.000 | 20.086 | 21.296 | 23.134 | 25.223 | 27.431 | 29.699 | 31.998 | 34.309 | 36.621 | 38.926 |


| 18 | 20.000 | 20.110 | 21.396 | 23.306 | 25.465 | 27.741 | 30.075 | 32.438 | 34.811 | 37.183 | 39.547 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 20.000 | 20.135 | 21.493 | 23.473 | 25.699 | 28.040 | 30.437 | 32.861 | 35.294 | 37.724 | 40.144 |
| 20 | 20.000 | 20.160 | 21.588 | 23.634 | 25.924 | 28.327 | 30.785 | 33.269 | 35.759 | 38.245 | 40.718 |
| 21 | 20.000 | 20.186 | 21.680 | 23.790 | 26.142 | 28605 | 31.122 | 33.662 | 36.207 | 38.746 | 41.270 |
| 22 | 20.000 | 20.212 | 21.770 | 23.941 | 26.352 | 28.873 | 31.446 | 34.041 | 36.640 | 39.230 | 41.803 |
| 23 | 20.000 | 20.239 | 21.858 | 24.087 | 26.555 | 29.132 | 31.760 | 34.408 | 37.058 | 39.697 | 42.318 |
| 24 | 20.000 | 20.266 | 21.943 | 24.229 | 26.752 | 29.383 | 32.064 | 34.763 | 37.462 | 40.149 | 42.815 |
| 25 | 20.000 | 20.292 | 22.026 | 24.366 | 26.943 | 29.627 | 32.358 | 35.107 | 37.854 | 40.587 | 43.296 |
| 26 | 20.000 | 20.319 | 22.107 | 24.499 | 27.128 | 29.862 | 32.643 | 35.440 | 38.233 | 41.010 | 43.762 |
| 27 | 20.000 | 20.346 | 22.185 | 24.629 | 27.308 | 30.091 | 32.920 | 35.763 | 38.601 | 41.421 | 44.213 |
| 28 | 20.000 | 20.372 | 22.261 | 24.754 | 27.482 | 30.313 | 33.189 | 36.077 | 38.958 | 41.819 | 44.651 |
| 29 | 20.000 | 20.398 | 22.336 | 24.876 | 27.652 | 30.529 | 33.450 | 36.381 | 39.305 | 42.206 | 45.076 |
| 30 | 20.000 | 20.423 | 22.408 | 24.995 | 27.816 | 30.739 | 33.704 | 36.678 | 39.641 | 42.582 | 45.488 |

Table B. 2
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 115 /$ Dividend Rate $=\mathbf{0 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 15.000 | 15.000 | 15.000 | 15.002 | 15.111 | 15.336 | 15.637 | 15.993 | 16.391 | 16.822 | 17.277 |
| 2 | 15.000 | 15.000 | 15.007 | 15.241 | 15.673 | 16.217 | 16.832 | 17.497 | 18.197 | 18.924 | 19.670 |
| 3 | 15.000 | 15.000 | 15.125 | 15.614 | 16.291 | 17.071 | 17.916 | 18.804 | 19.722 | 20.662 | 21.617 |
| 4 | 15.000 | 15.000 | 15.306 | 16.004 | 16.878 | 17.848 | 18.878 | 19.945 | 21.039 | 22.151 | 23.277 |
| 5 | 15.000 | 15.010 | 15.506 | 16.380 | 17.422 | 18.554 | 19.741 | 20.961 | 22.205 | 23.465 | 24.734 |
| 6 | 15.000 | 15.048 | 15.711 | 16.738 | 17.927 | 19.200 | 20.524 | 21.880 | 23.255 | 24.644 | 26.041 |
| 7 | 15.000 | 15.102 | 15.912 | 17.076 | 18.395 | 19.796 | 21.243 | 22.719 | 24.214 | 25.719 | 27.230 |
| 8 | 15.000 | 15.165 | 16.107 | 17.395 | 18.833 | 20.348 | 21.908 | 23.495 | 25.097 | 26.707 | 28.321 |
| 9 | 15.000 | 15.232 | 16.295 | 17.696 | 19.242 | 20.864 | 22.528 | 24.216 | 25.917 | 27.624 | 29.333 |
| 10 | 15.000 | 15.303 | 16.475 | 17.980 | 19.628 | 21.348 | 23.108 | 24.890 | 26.683 | 28.480 | 30.277 |
| 11 | 15.000 | 15.373 | 16.648 | 18.250 | 19.992 | 21.804 | 23.654 | 25.523 | 27.402 | 29.283 | 31.162 |
| 12 | 15.000 | 15.444 | 16.813 | 18.507 | 20.337 | 22.236 | 24.169 | 26.121 | 28.080 | 30.040 | 31.996 |
| 12 | 15.000 | 15.514 | 16.972 | 18.751 | 20.665 | 22.645 | 24.658 | 26.687 | 28.722 | 30.756 | 32.785 |
| 13 | 15.000 | 15.583 | 17.124 | 18.984 | 20.977 | 23.034 | 25.122 | 27.225 | 29.332 | 31.436 | 33.534 |
| 15 | 15.000 | 15.650 | 17.271 | 19.207 | 21.275 | 23.404 | 25.564 | 27.737 | 29.912 | 32.084 | 34.246 |
| 17 | 15.000 | 15.716 | 17.411 | 19.420 | 21.559 | 23.758 | 25.986 | 28.226 | 30.467 | 32.702 | 34.926 |
| 17 | 17.546 | 19.625 | 21.831 | 24.097 | 26.391 | 28.694 | 30.998 | 33.293 | 35.576 |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 15.000 | 15.842 | 17.676 | 19.821 | 22.093 | 24.422 | 26.778 | 29.143 | 31.506 | 33.860 | 36.199 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 15.000 | 15.903 | 17.802 | 20.010 | 22.343 | 24.734 | 27.151 | 29.575 | 31.995 | 34.404 | 36.797 |
| 20 | 15.000 | 15.962 | 17.922 | 20.191 | 22.585 | 25.035 | 27.509 | 29.990 | 32.465 | 34.927 | 37.371 |
| 21 | 15.000 | 16.019 | 18.038 | 20.365 | 22.817 | 25.324 | 27.854 | 30.389 | 32.918 | 35.431 | 37.925 |
| 22 | 15.000 | 16.074 | 18.150 | 20.534 | 23.041 | 25.603 | 28.187 | 30.775 | 33.354 | 35.917 | 38.458 |
| 23 | 15.000 | 16.128 | 18.258 | 20.696 | 23.258 | 25.873 | 28.509 | 31.147 | 33.776 | 36.386 | 38.972 |
| 24 | 15.000 | 16.180 | 18.363 | 20.853 | 23.467 | 26.134 | 28.820 | 31.507 | 34.183 | 36.839 | 39.469 |
| 25 | 15.000 | 16.230 | 18.463 | 21.005 | 23.669 | 26.386 | 29.121 | 31.856 | 34.577 | 37.278 | 39.950 |
| 26 | 15.001 | 16.279 | 18.561 | 21.152 | 23.865 | 26.630 | 29.412 | 32.193 | 34.959 | 37.702 | 40.415 |
| 27 | 15.002 | 16.326 | 18.655 | 21.294 | 24.055 | 26.867 | 29.695 | 32.520 | 35.329 | 38.114 | 40.866 |
| 28 | 15.003 | 16.372 | 18.747 | 21.432 | 24.239 | 27.096 | 29.969 | 32.838 | 35.688 | 38.512 | 41.303 |
| 29 | 15.005 | 16.416 | 18.835 | 21.565 | 24.417 | 27.319 | 30.235 | 33.146 | 36.037 | 38.900 | 41.727 |
| 27 | 15.007 | 16.458 | 18.921 | 21.695 | 24.591 | 27.536 | 30.494 | 33.445 | 36.376 | 39.276 | 42.138 |

Table B. 3
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 110 /$ Dividend Rate $=0 \%$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 10.000 | 10.000 | 10.062 | 10.301 | 10.641 | 11.043 | 11.487 | 11.960 | 12.456 | 12.968 | 13.492 |
| 2 | 10.000 | 10.048 | 10.422 | 10.976 | 11.620 | 12.317 | 13.049 | 13.803 | 14.573 | 15.356 | 16.147 |
| 3 | 10.000 | 10.201 | 10.818 | 11.600 | 12.464 | 13.374 | 14.312 | 15.270 | 16.241 | 17.220 | 18.206 |
| 4 | 10.000 | 10.379 | 11.189 | 12.155 | 13.196 | 14.278 | 15.385 | 16.508 | 17.642 | 18.782 | 19.927 |
| 5 | 10.003 | 10.558 | 11.531 | 12.653 | 13.844 | 15.073 | 16.324 | 17.589 | 18.863 | 20.142 | 21.422 |
| 6 | 10.021 | 10.730 | 11.845 | 13.103 | 14.427 | 15.785 | 17.164 | 18.555 | 19.952 | 21.352 | 22.753 |
| 7 | 10.049 | 10.894 | 12.135 | 13.515 | 14.957 | 16.433 | 17.927 | 19.430 | 20.939 | 22.448 | 23.957 |
| 8 | 10.083 | 11.049 | 12.404 | 13.894 | 15.445 | 17.027 | 18.626 | 20.233 | 21.843 | 23.452 | 25.059 |
| 9 | 10.120 | 11.195 | 12.655 | 14.247 | 15.898 | 17.578 | 19.273 | 20.975 | 22.679 | 24.380 | 26.078 |
| 10 | 10.158 | 11.333 | 12.889 | 14.576 | 16.320 | 18.091 | 19.876 | 21.666 | 23.457 | 25.245 | 27.027 |
| 11 | 10.196 | 11.464 | 13.110 | 14.884 | 16.715 | 18.572 | 20.441 | 22.314 | 24.187 | 26.055 | 27.916 |
| 12 | 10.235 | 11.588 | 13.317 | 15.175 | 17.086 | 19.024 | 20.972 | 22.924 | 24.873 | 26.817 | 28.752 |
| 16 | 10.272 | 11.705 | 13.514 | 15.449 | 17.437 | 19.451 | 21.475 | 23.500 | 25.523 | 27.538 | 29.542 |
| 13 | 10.380 | 12.024 | 14.043 | 16.189 | 18.387 | 20.608 | 22.837 | 25.063 | 27.283 | 29.491 | 31.683 |
| 17 | 10.309 | 11.817 | 13.700 | 15.708 | 17.770 | 19.856 | 21.951 | 24.047 | 26.138 | 28.221 | 30.291 |
| 15 | 10.345 | 11.923 | 13.876 | 15.954 | 18.086 | 20.241 | 22.404 | 24.567 | 26.724 | 28.871 | 31.004 |
| 10.413 | 12.120 | 14.203 | 16.413 | 18.675 | 20.959 | 23.250 | 25.538 | 27.817 | 30.083 | 32.332 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 10.445 | 12.212 | 14.356 | 16.627 | 18.950 | 21.295 | 23.645 | 25.992 | 28.329 | 30.651 | 32.954 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 10.476 | 12.299 | 14.501 | 16.831 | 19.214 | 21.617 | 24.025 | 26.428 | 28.820 | 31.195 | 33.550 |
| 20 | 10.505 | 12.382 | 14.641 | 17.028 | 19.467 | 21.926 | 24.390 | 26.847 | 29.292 | 31.718 | 34.123 |
| 21 | 10.533 | 12.462 | 14.775 | 17.217 | 19.711 | 22.224 | 24.741 | 27.251 | 29.746 | 32.222 | 34.674 |
| 22 | 10.559 | 12.539 | 14.904 | 17.398 | 19.945 | 22.511 | 25.080 | 27.640 | 30.184 | 32.708 | 35.205 |
| 23 | 10.584 | 12.612 | 15.027 | 17.573 | 20.171 | 22.788 | 25.406 | 28.015 | 30.607 | 33.176 | 35.718 |
| 24 | 10.608 | 12.683 | 15.146 | 17.742 | 20.389 | 23.055 | 25.722 | 28.378 | 31.015 | 33.629 | 36.213 |
| 25 | 10.631 | 12.750 | 15.261 | 17.904 | 20.600 | 23.314 | 26.027 | 28.729 | 31.410 | 34.066 | 36.691 |
| 26 | 10.654 | 12.815 | 15.372 | 18.062 | 20.804 | 23.564 | 26.322 | 29.068 | 31.793 | 34.490 | 37.154 |
| 27 | 10.675 | 12.878 | 15.479 | 18.214 | 21.001 | 23.806 | 26.609 | 29.397 | 32.163 | 34.900 | 37.603 |
| 28 | 10.696 | 12.938 | 15.582 | 18.361 | 21.193 | 24.041 | 26.886 | 29.717 | 32.523 | 35.298 | 38.037 |
| 29 | 10.717 | 12.996 | 15.682 | 18.503 | 21.378 | 24.269 | 27.156 | 30.027 | 32,872 | 35.684 | 38.459 |
| 20 | 10.736 | 13.052 | 15.778 | 18.642 | 21.558 | 24.490 | 27.417 | 30.327 | 33.211 | 36.059 | 38.868 |

Table B. 4
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 105 /$ Dividend Rate $=0 \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 5.047 | 5.360 | 5.793 | 6.279 | 6.795 | 7.330 | 7.876 | 8.430 | 8.990 | 9.554 | 10.122 |
| 2 | 5.255 | 5.865 | 6.578 | 7.334 | 8.112 | 8.903 | 9.703 | 10.507 | 11.316 | 12.126 | 12.938 |
| 3 | 5.461 | 6.282 | 7.196 | 8.148 | 9.118 | 10.099 | 11.086 | 12.077 | 13.070 | 14.064 | 15.058 |
| 4 | 5.646 | 6.635 | 7.711 | 8.822 | 9.950 | 11.087 | 12.229 | 13.373 | 14.518 | 15.662 | 16.806 |
| 5 | 5.811 | 6.941 | 8.156 | 9.404 | 10.668 | 11.939 | 13.214 | 14.490 | 15.767 | 17.041 | 18.314 |
| 6 | 5.958 | 7.212 | 8.549 | 9.918 | 11.302 | 12.693 | 14.086 | 15.480 | 16.873 | 18.264 | 19.651 |
| 7 | 6.091 | 7.455 | 8.902 | 10.380 | 11.872 | 13.371 | 14.872 | 16.373 | 17.871 | 19.366 | 20.857 |
| 8 | 6.212 | 7.675 | 9.222 | 10.800 | 12.392 | 13.990 | 15.590 | 17.188 | 18.784 | 20.374 | 21.960 |
| 9 | 6.322 | 7.876 | 9.515 | 11.185 | 12.870 | 14.560 | 16.251 | 17.940 | 19.625 | 21.305 | 22.977 |
| 10 | 6.423 | 8.061 | 9.785 | 11.542 | 13.313 | 15.089 | 16.866 | 18.640 | 20.408 | 22.170 | 23.924 |
| 11 | 6.515 | 8.232 | 10.037 | 11.875 | 13.727 | 15.584 | 17.440 | 19.294 | 21.141 | 22.980 | 24.809 |
| 12 | 6.600 | 8.391 | 10.271 | 12.186 | 14.114 | 16.048 | 17.980 | 19.908 | 21.829 | 23.741 | 25.642 |
| 16 | 6.679 | 8.539 | 10.491 | 12.478 | 14.480 | 16.486 | 18.490 | 20.489 | 22.480 | 24.460 | 26.428 |
| 13 | 6.753 | 8.678 | 10.699 | 12.755 | 14.825 | 16.900 | 18.972 | 21.039 | 23.096 | 25.141 | 27.173 |
| 17 | 6.822 | 8.809 | 10.894 | 13.016 | 15.153 | 17.293 | 19.431 | 21.562 | 23.682 | 25.789 | 27.881 |
| 17 | 6.947 | 9.049 | 11.256 | 13.501 | 15.762 | 18.025 | 20.285 | 22.536 | 24.774 | 26.996 | 29.200 |
| 11.080 | 13.265 | 15.464 | 17.668 | 19.868 | 22.060 | 24.240 | 26.407 | 28.556 |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 7.004 | 9.160 | 11.423 | 13.727 | 16.045 | 18.367 | 20.684 | 22.992 | 25.285 | 27.561 | 29.817 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 7.058 | 9.266 | 11.583 | 13.942 | 16.317 | 18.695 | 21.067 | 23.429 | 25.775 | 28.103 | 30.409 |
| 20 | 7.109 | 9.366 | 11.736 | 14.149 | 16.578 | 19.009 | 21.435 | 23.849 | 26.246 | 28.624 | 30.978 |
| 21 | 7.157 | 9.462 | 11.882 | 14.347 | 16.828 | 19.312 | 21.789 | 24.253 | 26.699 | 29.125 | 31.525 |
| 22 | 7.203 | 9.553 | 12.022 | 14.538 | 17.069 | 19.603 | 22.129 | 24.642 | 27.136 | 29.607 | 32.052 |
| 23 | 7.246 | 9.640 | 12.157 | 14.721 | 17.301 | 19.884 | 22.458 | 25.018 | 27.558 | 30.073 | 32.560 |
| 24 | 7.288 | 9.724 | 12.286 | 14.897 | 17.525 | 20.155 | 22.776 | 25.381 | 27.965 | 30.523 | 33.051 |
| 25 | 7.327 | 9.804 | 12.410 | 15.067 | 17.741 | 20.416 | 23.082 | 25.732 | 28.358 | 30.957 | 33.525 |
| 26 | 7.364 | 9.881 | 12.530 | 15.231 | 17.950 | 20.670 | 23.379 | 26.071 | 28.739 | 31.378 | 33.984 |
| 27 | 7.400 | 9.955 | 12.645 | 15.390 | 18.152 | 20.915 | 23.667 | 26.400 | 29.109 | 31.786 | 34.428 |
| 28 | 7.434 | 10.026 | 12.757 | 15.543 | 18.348 | 21.153 | 23.946 | 26.720 | 29.466 | 32.181 | 34.859 |
| 29 | 7.466 | 10.094 | 12.864 | 15.691 | 18.537 | 21.383 | 24.217 | 27.029 | 29.814 | 32.565 | 35.277 |
| 30 | 7.497 | 10.160 | 12.968 | 15.835 | 18.721 | 21.607 | 24.479 | 27.330 | 30.151 | 32.937 | 35.682 |

Table B. 5
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 100 /$ Dividend Rate $=0 \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 1.521 | 2.090 | 2.660 | 3.232 | 3.804 | 4.376 | 4.948 | 5.520 | 6.092 | 6.664 | 7.236 |
| 2 | 2.048 | 2.844 | 3.645 | 4.448 | 5.252 | 6.057 | 6.862 | 7.666 | 8.470 | 9.274 | 10.076 |
| 3 | 2.418 | 3.384 | 4.358 | 5.336 | 6.316 | 7.296 | 8.277 | 9.257 | 10.236 | 11.214 | 12.191 |
| 4 | 2.707 | 3.815 | 4.932 | 6.056 | 7.181 | 8.308 | 9.435 | 10.561 | 11.685 | 12.808 | 13.929 |
| 5 | 2.947 | 4.176 | 5.419 | 6.668 | 7.921 | 9.175 | 10.428 | 11.681 | 12.931 | 14.180 | 15.425 |
| 6 | 3.151 | 4.489 | 5.843 | 7.205 | 8.571 | 9.938 | 11.305 | 12.671 | 14.034 | 15.393 | 16.749 |
| 7 | 3.330 | 4.765 | 6.220 | 7.684 | 9.154 | 10.624 | 12.094 | 13.562 | 15.027 | 16.488 | 17.943 |
| 8 | 3.488 | 5.013 | 6.561 | 8.119 | 9.683 | 11.249 | 12.814 | 14.376 | 15.934 | 17.487 | 19.034 |
| 9 | 3.630 | 5.238 | 6.872 | 8.518 | 10.170 | 11.824 | 13.476 | 15.125 | 16.770 | 18.409 | 20.040 |
| 10 | 3.759 | 5.444 | 7.158 | 8.885 | 10.620 | 12.356 | 14.091 | 15.822 | 17.547 | 19.266 | 20.976 |
| 11 | 3.876 | 5.634 | 7.423 | 9.228 | 11.040 | 12.854 | 14.666 | 16.473 | 18.274 | 20.067 | 21.851 |
| 12 | 3.983 | 5.810 | 7.670 | 9.547 | 11.433 | 13.320 | 15.205 | 17.085 | 18.957 | 20.821 | 22.673 |
| 13 | 4.083 | 5.973 | 7.901 | 9.848 | 11.803 | 13.760 | 15.714 | 17.662 | 19.602 | 21.532 | 23.450 |
| 14 | 4.175 | 6.127 | 8.119 | 10.131 | 12.153 | 14.176 | 16.196 | 18.209 | 20.213 | 22.206 | 24.185 |
| 15 | 4.260 | 6.270 | 8.324 | 10.399 | 12.484 | 14.570 | 16.653 | 18.729 | 20.794 | 22.847 | 24.885 |
| 16 | 4.340 | 6.406 | 8.518 | 10.653 | 12.799 | 14.946 | 17.089 | 19.224 | 21.348 | 23.458 | 25.551 |
| 17 | 4.414 | 6.534 | 8.702 | 10.895 | 13.099 | 15.305 | 17.505 | 19.697 | 21.877 | 24.041 | 26.187 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 4.484 | 6.655 | 8.877 | 11.126 | 13.386 | 15.647 | 17.903 | 20.150 | 22.383 | 24.599 | 26.797 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 4.550 | 6.770 | 9.044 | 11.346 | 13.660 | 15.976 | 18.285 | 20.584 | 22.868 | 25.135 | 27.381 |
| 20 | 4.612 | 6.879 | 9.204 | 11.557 | 13.924 | 16.291 | 18.652 | 21.001 | 23.335 | 25.650 | 27.942 |
| 21 | 4.670 | 6.983 | 9.356 | 11.760 | 14.176 | 16.594 | 19.004 | 21.403 | 23.784 | 26.145 | 28.482 |
| 22 | 4.725 | 7.082 | 9.502 | 11.954 | 14.419 | 16.885 | 19.344 | 21.789 | 24.217 | 26.622 | 29.002 |
| 23 | 4.777 | 7.176 | 9.642 | 12.141 | 14.653 | 17.166 | 19.671 | 22.162 | 24.634 | 27.082 | 29.504 |
| 24 | 4.827 | 7.267 | 9.777 | 12.321 | 14.879 | 17.438 | 19.988 | 22.523 | 25.037 | 27.527 | 29.988 |
| 25 | 4.874 | 7.353 | 9.906 | 12.494 | 15.097 | 17.700 | 20.294 | 22.871 | 25.427 | 27.957 | 30.456 |
| 26 | 4.919 | 7.436 | 10.030 | 12.661 | 15.307 | 17.953 | 20.589 | 23.208 | 25.804 | 28.373 | 30.909 |
| 27 | 4.961 | 7.516 | 10.150 | 12.823 | 15.511 | 18.199 | 20.876 | 23.535 | 26.170 | 28.776 | 31.348 |
| 28 | 5.002 | 7.593 | 10.266 | 12.979 | 15.708 | 18.437 | 21.154 | 23.852 | 26.524 | 29.166 | 31.773 |
| 29 | 5.040 | 7.666 | 10.378 | 13.130 | 15.899 | 18.667 | 21.423 | 24.159 | 26.868 | 29.545 | 32.185 |
| 30 | 5.077 | 7.737 | 10.486 | 13.276 | 16.084 | 18.891 | 21.685 | 24.458 | 27.202 | 29.913 | 32.585 |

Table B. 6
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 95 /$ Dividend Rate $=0 \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.197 | 0.499 | 0.884 | 1.320 | 1.787 | 2.276 | 2.779 | 3.292 | 3.813 | 4.340 | 4.872 |
| 2 | 0.516 | 1.066 | 1.700 | 2.382 | 3.091 | 3.819 | 4.559 | 5.308 | 6.062 | 6.821 | 7.583 |
| 3 | 0.793 | 1.525 | 2.341 | 3.201 | 4.089 | 4.993 | 5.909 | 6.832 | 7.761 | 8.692 | 9.626 |
| 4 | 1.032 | 1.911 | 2.874 | 3.881 | 4.914 | 5.964 | 7.025 | 8.092 | 9.164 | 10.238 | 11.313 |
| 5 | 1.240 | 2.244 | 3.333 | 4.466 | 5.626 | 6.802 | 7.988 | 9.180 | 10.375 | 11.573 | 12.770 |
| 6 | 1.423 | 2.538 | 3.738 | 4.984 | 6.256 | 7.543 | 8.841 | 10.144 | 11.450 | 12.756 | 14.062 |
| 7 | 1.587 | 2.801 | 4.102 | 5.449 | 6.823 | 8.212 | 9.610 | 11.014 | 12.419 | 13.825 | 15.228 |
| 8 | 1.735 | 3.039 | 4.432 | 5.873 | 7.339 | 8.822 | 10.313 | 11.809 | 13.306 | 14.802 | 16.294 |
| 9 | 1.870 | 3.257 | 4.735 | 6.262 | 7.815 | 9.384 | 10.961 | 12.542 | 14.124 | 15.703 | 17.278 |
| 10 | 1.993 | 3.457 | 5.015 | 6.622 | 8.256 | 9.906 | 11.563 | 13.225 | 14.885 | 16.542 | 18.193 |
| 11 | 2.106 | 3.643 | 5.275 | 6.958 | 8.668 | 10.394 | 12.127 | 13.863 | 15.597 | 17.327 | 19.050 |
| 12 | 2.211 | 3.815 | 5.518 | 7.272 | 9.054 | 10.852 | 12.656 | 14.463 | 16.267 | 18.065 | 19.856 |
| 13 | 2.308 | 3.977 | 5.747 | 7.568 | 9.418 | 11.284 | 13.156 | 15.030 | 16.900 | 18.763 | 20.616 |
| 14 | 2.398 | 4.128 | 5.961 | 7.848 | 9.763 | 11.693 | 13.630 | 15.567 | 17.499 | 19.424 | 21.338 |
| 15 | 2.483 | 4.271 | 6.164 | 8.112 | 10.089 | 12.081 | 14.080 | 16.078 | 18.069 | 20.052 | 22.023 |
| 16 | 2.562 | 4.405 | 6.357 | 8.364 | 10.400 | 12.452 | 14.509 | 16.564 | 18.613 | 20.651 | 22.676 |
| 17 | 2.636 | 4.532 | 6.540 | 8.603 | 10.696 | 12.805 | 14.918 | 17.029 | 19.132 | 21.224 | 23.301 |
| 102 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 2.706 | 4.653 | 6.714 | 8.831 | 10.980 | 13.143 | 15.310 | 17.474 | 19.630 | 21.772 | 23.898 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 2.772 | 4.768 | 6.880 | 9.050 | 11.251 | 13.467 | 15.686 | 17.902 | 20.107 | 22.298 | 24.472 |
| 20 | 2.835 | 4.877 | 7.038 | 9.259 | 11.511 | 13.778 | 16.047 | 18.312 | 20.568 | 22.803 | 25.022 |
| 21 | 2.893 | 4.981 | 7.190 | 9.460 | 11.761 | 14.077 | 16.395 | 18.707 | 21.007 | 23.290 | 25.552 |
| 22 | 2.949 | 5.081 | 7.336 | 9.653 | 12.001 | 14.365 | 16.730 | 19.088 | 21.432 | 23.759 | 26.063 |
| 23 | 3.002 | 5.176 | 7.475 | 9.838 | 12.233 | 14.642 | 17.053 | 19.455 | 21.843 | 24.211 | 26.555 |
| 24 | 3.053 | 5.267 | 7.610 | 10.017 | 12.457 | 14.910 | 17.365 | 19.810 | 22.239 | 24.648 | 27.031 |
| 25 | 3.101 | 5.354 | 7.739 | 10.189 | 12.673 | 15.169 | 17.666 | 20.153 | 22.623 | 25.070 | 27.491 |
| 26 | 3.146 | 5.438 | 7.863 | 10.356 | 12.881 | 15.420 | 17.958 | 20.485 | 22.994 | 25.479 | 27.935 |
| 27 | 3.190 | 5.518 | 7.983 | 10.516 | 13.083 | 15.663 | 18.241 | 20.807 | 23.354 | 25.875 | 28.366 |
| 28 | 3.231 | 5.595 | 8.099 | 10.672 | 13.278 | 15.898 | 18.515 | 21.119 | 23.703 | 26.259 | 28.784 |
| 29 | 3.271 | 5.670 | 8.211 | 10.822 | 13.468 | 16.126 | 18.781 | 21.422 | 24.041 | 28.632 | 29.189 |
| 20 | 3.309 | 5.741 | 8.319 | 10.968 | 13.652 | 16.347 | 19.040 | 21.716 | 24.370 | 26.994 | 29.582 |

Table B. 7
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 90 / \text { Dividend Rate }=0 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0008 | 0.060 | 0.190 | 0.398 | 0.672 | 0.996 | 1.359 | 1.753 | 2.170 | 2.606 | 3.056 |
| 2 | 0.072 | 0.284 | 0.637 | 1.092 | 1.620 | 2.199 | 2.815 | 3.457 | 4.119 | 4.797 | 5.486 |
| 3 | 0.175 | 0.547 | 1.082 | 1.726 | 2.442 | 3.207 | 4.005 | 4.828 | 5.669 | 6.522 | 7.386 |
| 4 | 0.292 | 0.804 | 1.493 | 2.290 | 3.159 | 4.074 | 5.021 | 5.990 | 6.976 | 7.973 | 8.978 |
| 5 | 0.410 | 1.047 | 1.866 | 2.796 | 3.794 | 4.838 | 5.912 | 7.008 | 8.118 | 9.238 | 10.365 |
| 6 | 0.525 | 1.273 | 2.208 | 3.253 | 4.367 | 5.524 | 6.711 | 7.917 | 9.138 | 10.367 | 11.602 |
| 7 | 0.635 | 1.484 | 2.523 | 3.672 | 4.889 | 6.149 | 7.437 | 8.744 | 10.063 | 11.390 | 12.722 |
| 8 | 0.740 | 1.680 | 2.814 | 4.058 | 5.369 | 6.723 | 8.104 | 9.502 | 10.913 | 12.330 | 13.750 |
| 9 | 0.839 | 1.864 | 3.084 | 4.416 | 5.815 | 7.255 | 8.721 | 10.205 | 11.699 | 13.199 | 14.701 |
| 10 | 0.932 | 2.035 | 3.337 | 4.751 | 6.230 | 7.751 | 9.298 | 10.860 | 12.432 | 14.009 | 15.586 |
| 11 | 1.020 | 2.197 | 3.575 | 5.064 | 6.620 | 8.216 | 9.838 | 11.475 | 13.120 | 14.769 | 16.416 |
| 12 | 1.103 | 2.349 | 3.798 | 5.360 | 6.987 | 8.655 | 10.347 | 12.054 | 13.768 | 15.484 | 17.198 |
| 13 | 1.182 | 2.492 | 4.009 | 5.639 | 7.334 | 9.070 | 10.829 | 12.602 | 14.381 | 16.161 | 17.936 |
| 14 | 1.256 | 2.628 | 4.209 | 5.903 | 7.663 | 9.463 | 11.286 | 13.121 | 14.962 | 16.802 | 18.637 |
| 15 | 1.327 | 2.757 | 4.399 | 6.155 | 7.977 | 9.837 | 11.721 | 13.616 | 15.516 | 17.413 | 19.304 |
| 17 | 1.394 | 2.880 | 4.579 | 6.394 | 8.275 | 10.195 | 12.136 | 14.089 | 16.044 | 17.996 | 19.940 |
| 1 | 2.996 | 4.752 | 6.623 | 8560 | 10.536 | 12.533 | 14.540 | 16.549 | 18.553 | 20.547 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 1.518 | 3.107 | 4.916 | 6.842 | 8.833 | 10.863 | 12.913 | 14.973 | 17.033 | 19.087 | 21.130 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 1.575 | 3.214 | 5.074 | 7.051 | 9.095 | 11.177 | 13.279 | 15.389 | 17.498 | 19.599 | 21.688 |
| 20 | 1.629 | 3.315 | 5.224 | 7.253 | 9.347 | 11.479 | 13.630 | 15.788 | 17.945 | 20.092 | 22.225 |
| 21 | 1.681 | 3.412 | 5.369 | 7.446 | 9.589 | 11.769 | 13.968 | 16.173 | 18.375 | 20.566 | 22.742 |
| 22 | 1.731 | 3.505 | 5.508 | 7.632 | 9.822 | 12.049 | 14.294 | 16.544 | 18.790 | 21.024 | 23.240 |
| 23 | 1.778 | 3.595 | 5.642 | 7.811 | 10.047 | 12.319 | 14.609 | 16.903 | 19.190 | 21.465 | 23.721 |
| 24 | 1.824 | 3.680 | 5.771 | 7.984 | 10.264 | 12.580 | 14.913 | 17.249 | 19.578 | 21.891 | 24.185 |
| 25 | 1.867 | 3.763 | 5.895 | 8.151 | 10.474 | 12.833 | 15.207 | 17.584 | 19.952 | 22.304 | 24.634 |
| 26 | 1.908 | 3.842 | 6.015 | 8.313 | 10.677 | 13.077 | 15.492 | 17.908 | 20.315 | 22.704 | 25.069 |
| 27 | 1.948 | 3.919 | 6.131 | 8.469 | 10.874 | 13.314 | 15.768 | 18.223 | 20.666 | 23.091 | 25.490 |
| 28 | 1.986 | 3.992 | 6.243 | 8.620 | 11.064 | 13.543 | 16.036 | 18.528 | 21.007 | 23.466 | 25.898 |
| 29 | 2.022 | 4.063 | 6.351 | 8.766 | 11.249 | 13.766 | 16.296 | 18.824 | 21.338 | 23.830 | 26.294 |
| 20 | 2.057 | 4.132 | 6.456 | 8.908 | 11.428 | 13.982 | 16.549 | 19.112 | 21.660 | 24.184 | 26.679 |

Table B. 8
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 85 /$ Dividend Rate $=0 \%$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.003 | 0.024 | 0.082 | 0.190 | 0.350 | 0.559 | 0.810 | 1.098 | 1.415 | 1.759 |
| 2 | 0.005 | 0.050 | 0.181 | 0.412 | 0.735 | 1.132 | 1.587 | 2.090 | 2.629 | 3.196 | 3.787 |
| 3 | 0.024 | 0.148 | 0.415 | 0.816 | 1.321 | 1.906 | 2.549 | 3.238 | 3.961 | 4.710 | 5.479 |
| 4 | 0.057 | 0.273 | 0.673 | 1.222 | 1.881 | 2.620 | 3.416 | 4.256 | 5.127 | 6.023 | 6.937 |
| 5 | 0.101 | 0.411 | 0.931 | 1.611 | 2.403 | 3.274 | 4.201 | 5.169 | 6.167 | 7.187 | 8.224 |
| 6 | 0.151 | 0.552 | 1.183 | 1.980 | 2.889 | 3.876 | 4.918 | 5.999 | 7.108 | 8.238 | 9.383 |
| 7 | 0.205 | 0.693 | 1.425 | 2.327 | 3.342 | 4.434 | 5.579 | 6.761 | 7.970 | 9.199 | 10.440 |
| 8 | 0.261 | 0.830 | 1.657 | 2.655 | 3.766 | 4.953 | 6.191 | 7.466 | 8.767 | 10.085 | 11.414 |
| 9 | 0.318 | 0.964 | 1.877 | 2.964 | 4.164 | 5.438 | 6.764 | 8.124 | 9.508 | 10.908 | 12.319 |
| 10 | 0.374 | 1.093 | 2.087 | 3.257 | 4.539 | 5.895 | 7.301 | 8.740 | 10.202 | 11.679 | 13.164 |
| 11 | 0.430 | 1.218 | 2.288 | 3.534 | 4.894 | 6.326 | 7.807 | 9.320 | 10.855 | 12.403 | 13.959 |
| 12 | 0.484 | 1.338 | 2.479 | 3.798 | 5.230 | 6.734 | 8.286 | 9.868 | 11.472 | 13.087 | 14.708 |
| 13 | 0.537 | 1.453 | 2.661 | 4.050 | 5.550 | 7.122 | 8.740 | 10.389 | 12.056 | 13.735 | 15.418 |
| 14 | 0.589 | 1.563 | 2.836 | 4.289 | 5.855 | 7.491 | 9.173 | 10.884 | 12.613 | 14.351 | 16.093 |
| 15 | 0.639 | 1.670 | 3.003 | 4.519 | 6.146 | 7.843 | 9.586 | 11.356 | 13.143 | 14.938 | 16.735 |
| 17 | 0.687 | 1.772 | 3.164 | 4.738 | 6.424 | 8.180 | 9.980 | 11.808 | 13.650 | 15.499 | 17.348 |
| 17 | 0.734 | 1.870 | 3.318 | 4.949 | 6.692 | 8.504 | 10.359 | 12.240 | 14.135 | 16.036 | 17.935 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.779 | 1.964 | 3.465 | 5.151 | 6.948 | 8.814 | 10.722 | 12.655 | 14.601 | 16.551 | 18.498 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.822 | 2.055 | 3.608 | 5.346 | 7.195 | 9.113 | 11.071 | 13.054 | 15.049 | 17.046 | 19.038 |
| 20 | 0.864 | 2.143 | 3.745 | 5.533 | 7.433 | 9.400 | 11.408 | 13.439 | 15.480 | 17.523 | 19.558 |
| 21 | 0.904 | 2.227 | 3.877 | 5.714 | 7.662 | 9.677 | 11.732 | 13.809 | 15.896 | 17.981 | 20.059 |
| 22 | 0.943 | 2.309 | 4.004 | 5.888 | 7.883 | 9.945 | 12.045 | 14.167 | 16.297 | 18.424 | 20.541 |
| 23 | 0.981 | 2.387 | 4.127 | 6.056 | 8.097 | 10.203 | 12.348 | 14.513 | 16.684 | 18.852 | 21.007 |
| 24 | 1.017 | 2.463 | 4.246 | 6.219 | 8.303 | 10.453 | 12.641 | 14.847 | 17.059 | 19.265 | 21.458 |
| 25 | 1.052 | 2.536 | 4.361 | 6.376 | 8.503 | 10.695 | 12.924 | 15.171 | 17.421 | 19.665 | 21.894 |
| 26 | 1.085 | 2.607 | 4.472 | 6.529 | 8.697 | 10.930 | 13.199 | 15.485 | 17.773 | 20.052 | 22.316 |
| 27 | 1.118 | 2.675 | 4.579 | 6.677 | 8.885 | 11.158 | 13.466 | 15.789 | 18.114 | 20.428 | 22.725 |
| 28 | 1.149 | 2.741 | 4.683 | 6.820 | 9.067 | 11.379 | 13.724 | 16.084 | 18.445 | 20.793 | 23.121 |
| 29 | 1.179 | 2.805 | 4.785 | 6.959 | 9.245 | 11.593 | 13.976 | 16.372 | 18.766 | 21.147 | 23.506 |
| 20 | 1.209 | 2.867 | 4.883 | 7.094 | 9.417 | 11.802 | 14.220 | 16.651 | 19.078 | 21.491 | 23.880 |

Table B. 9
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 80 /$ Dividend Rate $=\mathbf{0 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.002 | 0.011 | 0.038 | 0.094 | 0.186 | 0.315 | 0.480 | 0.680 | 0.910 |
| 2 | 0.000 | 0.006 | 0.037 | 0.123 | 0.279 | 0.508 | 0.802 | 1.154 | 1.554 | 1.995 | 2.470 |
| 3 | 0.002 | 0.029 | 0.127 | 0.328 | 0.634 | 1.031 | 1.504 | 2.039 | 2.624 | 3.248 | 3.905 |
| 4 | 0.008 | 0.072 | 0.256 | 0.577 | 1.021 | 1.567 | 2.192 | 2.879 | 3.614 | 4.388 | 5.191 |
| 5 | 0.018 | 0.131 | 0.405 | 0.841 | 1.412 | 2.088 | 2.844 | 3.661 | 4.525 | 5.425 | 6.353 |
| 6 | 0.033 | 0.201 | 0.564 | 1.107 | 1.792 | 2.585 | 3.457 | 4.389 | 5.366 | 6.377 | 7.414 |
| 7 | 0.052 | 0.278 | 0.727 | 1.370 | 2.160 | 3.057 | 4.033 | 5.068 | 6.146 | 7.256 | 8.391 |
| 8 | 0.075 | 0.359 | 0.891 | 1.627 | 2.512 | 3.505 | 4.576 | 5.704 | 6.874 | 8.075 | 9.298 |
| 9 | 0.099 | 0.442 | 1.053 | 1.875 | 2.849 | 3.931 | 5.089 | 6.303 | 7.557 | 8.841 | 10.145 |
| 10 | 0.126 | 0.527 | 1.212 | 2.115 | 3.171 | 4.335 | 5.575 | 6.869 | 8.201 | 9.561 | 10.939 |
| 11 | 0.154 | 0.611 | 1.368 | 2.347 | 3.480 | 4.721 | 6.036 | 7.404 | 8.809 | 10.240 | 11.689 |
| 12 | 0.183 | 0.694 | 1.519 | 2.570 | 3.776 | 5.089 | 6.475 | 7.913 | 9.387 | 10.884 | 12.398 |
| 13 | 0.212 | 0.777 | 1.666 | 2.785 | 4.060 | 5.441 | 6.894 | 8.398 | 9.936 | 11.497 | 13.072 |
| 14 | 0.242 | 0.858 | 1.808 | 2.992 | 4.332 | 5.778 | 7.295 | 8.861 | 10.460 | 12.080 | 13.713 |
| 15 | 0.272 | 0.937 | 1.946 | 3.191 | 4.594 | 6.101 | 7.679 | 9.304 | 10.961 | 12.637 | 14.325 |
| 16 | 0.301 | 1.014 | 2.080 | 3.384 | 4.846 | 6.412 | 8.047 | 9.729 | 11.441 | 13.171 | 14.911 |
| 17 | 0.331 | 1.090 | 2.210 | 3.570 | 5.089 | 6.711 | 8.401 | 10.137 | 11.901 | 13.683 | 15.472 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.360 | 1.163 | 2.335 | 3.750 | 5.323 | 6.999 | 8.742 | 10.529 | 12.344 | 14.174 | 16.011 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.388 | 1.235 | 2.457 | 3.924 | 5.549 | 7.276 | 9.070 | 10.907 | 12.770 | 14.647 | 16.529 |
| 20 | 0.416 | 1.305 | 2.575 | 4.093 | 5.768 | 7.545 | 9.387 | 11.272 | 13.181 | 15.103 | 17.028 |
| 21 | 0.444 | 1.373 | 2.690 | 4.255 | 5.979 | 7.804 | 9.694 | 11.624 | 13.577 | 15.542 | 17.509 |
| 22 | 0.470 | 1.439 | 2.801 | 4.413 | 6.184 | 8.055 | 9.990 | 11.964 | 13.961 | 15.967 | 17.973 |
| 23 | 0.497 | 1.503 | 2.909 | 4.566 | 6.382 | 8.298 | 10.276 | 12.293 | 14.331 | 16.378 | 18.422 |
| 24 | 0.522 | 1.566 | 3.013 | 4.715 | 6.574 | 8.533 | 10.554 | 12.612 | 14.690 | 16.775 | 18.856 |
| 25 | 0.547 | 1.627 | 3.115 | 4.859 | 6.761 | 8.762 | 10.824 | 12.922 | 15.038 | 17.160 | 19.276 |
| 26 | 0.572 | 1.686 | 3.214 | 4.999 | 6.942 | 8.983 | 11.085 | 13.222 | 15.375 | 17.533 | 19.682 |
| 27 | 0.596 | 1.743 | 3.310 | 5.135 | 7.118 | 9.199 | 11.339 | 13.513 | 15.703 | 17.895 | 20.077 |
| 28 | 0.619 | 1.799 | 3.403 | 5.267 | 7.289 | 9.408 | 11.586 | 13.796 | 16.021 | 18.246 | 20.460 |
| 29 | 0.641 | 1.854 | 3.494 | 5.396 | 7.455 | 9.612 | 11.826 | 14.072 | 16.330 | 18.587 | 20.832 |
| 30 | 0.663 | 1.907 | 3.583 | 5.521 | 7.617 | 9.810 | 12.060 | 14.339 | 16.631 | 18.919 | 21.193 |

Table B. 10
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 7 5} /$ Dividend Rate $=\mathbf{0 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.018 | 0.048 | 0.099 | 0.176 | 0.281 | 0.414 |
| 2 | 0.000 | 0.001 | 0.005 | 0.028 | 0.086 | 0.193 | 0.355 | 0.571 | 0.838 | 1.152 | 1.506 |
| 3 | 0.000 | 0.004 | 0.030 | 0.109 | 0.263 | 0.498 | 0.810 | 1.190 | 1.630 | 2.121 | 2.653 |
| 4 | 0.001 | 0.015 | 0.079 | 0.235 | 0.496 | 0.859 | 1.310 | 1.836 | 2.424 | 3.062 | 3.741 |
| 5 | 0.003 | 0.033 | 0.149 | 0.389 | 0.757 | 1.239 | 1.816 | 2.470 | 3.185 | 3.950 | 4.755 |
| 6 | 0.006 | 0.060 | 0.234 | 0.560 | 1.029 | 1.621 | 2.311 | 3.079 | 3.908 | 4.785 | 5.699 |
| 7 | 0.011 | 0.094 | 0.329 | 0.739 | 1.305 | 1.998 | 2.791 | 3.661 | 4.591 | 5.568 | 6.581 |
| 8 | 0.017 | 0.133 | 0.431 | 0.922 | 1.578 | 2.365 | 3.252 | 4.216 | 5.238 | 6.306 | 7.407 |
| 9 | 0.025 | 0.176 | 0.537 | 1.105 | 1.846 | 2.720 | 3.695 | 4.745 | 5.852 | 7.002 | 8.185 |
| 10 | 0.035 | 0.223 | 0.645 | 1.288 | 2.108 | 3.064 | 4.119 | 5.249 | 6.435 | 7.662 | 8.919 |
| 11 | 0.046 | 0.272 | 0.754 | 1.468 | 2.364 | 3.395 | 4.526 | 5.731 | 6.990 | 8.288 | 9.616 |
| 12 | 0.059 | 0.323 | 0.863 | 1.645 | 2.612 | 3.715 | 4.917 | 6.192 | 7.519 | 8.885 | 10.277 |
| 13 | 0.072 | 0.375 | 0.972 | 1.818 | 2.853 | 4.024 | 5.293 | 6.634 | 8.025 | 9.454 | 10.907 |
| 14 | 0.086 | 0.428 | 1.079 | 1.988 | 3.086 | 4.322 | 5.655 | 7.058 | 8.510 | 9.998 | 11.509 |
| 15 | 0.101 | 0.480 | 1.185 | 2.153 | 3.313 | 4.610 | 6.003 | 7.465 | 8.976 | 10.520 | 12.086 |
| 16 | 0.116 | 0.533 | 1.289 | 2.314 | 3.533 | 4.888 | 6.339 | 7.858 | 9.423 | 11.020 | 12.638 |
| 17 | 0.131 | 0.586 | 1.392 | 2.471 | 3.746 | 5.157 | 6.664 | 8.236 | 9.853 | 11.501 | 13.168 |


| 18 | 0.147 | 0.638 | 1.492 | 2.624 | 3.953 | 5.418 | 6.977 | 8.600 | 10.268 | 11.965 | 13.679 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.163 | 0.690 | 1.590 | 2.773 | 4.154 | 5.670 | 7.280 | 8.953 | 10.668 | 12.411 | 14.170 |
| 20 | 0.179 | 0.741 | 1.686 | 2.919 | 4.349 | 5.915 | 7.573 | 9.293 | 11.055 | 12.842 | 14.644 |
| 21 | 0.196 | 0.791 | 1.781 | 3.060 | 4.538 | 6.152 | 7.857 | 9.623 | 11.429 | 13.259 | 15.102 |
| 22 | 0.212 | 0.841 | 1.873 | 3.198 | 4.723 | 6.382 | 8.132 | 9.942 | 11.791 | 13.662 | 15.544 |
| 23 | 0.228 | 0.889 | 1.963 | 3.332 | 4.902 | 6.606 | 8.399 | 10.252 | 12.141 | 14.052 | 15.972 |
| 24 | 0.244 | 0.937 | 2.050 | 3.463 | 5.076 | 6.823 | 8.659 | 10.552 | 12.481 | 14.430 | 16.386 |
| 25 | 0.260 | 0.984 | 2.136 | 3.590 | 5.246 | 7.035 | 8.911 | 10.844 | 12.811 | 14.796 | 16.787 |
| 26 | 0.275 | 1.030 | 2.220 | 3.715 | 5.411 | 7.240 | 9.156 | 11.127 | 13.131 | 15.152 | 17.177 |
| 27 | 0.291 | 1.075 | 2.302 | 3.836 | 5.572 | 7.440 | 9.394 | 11.403 | 13.442 | 15.497 | 17.554 |
| 28 | 0.306 | 1.120 | 2.382 | 3.954 | 5.729 | 7.635 | 9.627 | 11.671 | 13.745 | 15.833 | 17.921 |
| 29 | 0.321 | 1.163 | 2.461 | 4.069 | 5.882 | 7.825 | 9.853 | 11.932 | 14.039 | 16.160 | 18.278 |
| 20 | 0.336 | 1.205 | 2.537 | 4.182 | 6.031 | 8.010 | 10.073 | 12.186 | 14.326 | 16.477 | 18.624 |

Table B. 11
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 7 0} /$ Dividend Rate $=\mathbf{0 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.009 | 0.024 | 0.052 | 0.097 | 0.161 |
| 2 | 0.000 | 0.000 | 0.001 | 0.005 | 0.021 | 0.060 | 0.133 | 0.247 | 0.404 | 0.604 | 0.845 |
| 3 | 0.000 | 0.001 | 0.006 | 0.029 | 0.092 | 0.210 | 0.390 | 0.634 | 0.938 | 1.296 | 1.701 |
| 4 | 0.000 | 0.002 | 0.020 | 0.081 | 0.211 | 0.424 | 0.719 | 1.091 | 1.531 | 2.029 | 2.577 |
| 5 | 0.000 | 0.007 | 0.046 | 0.156 | 0.364 | 0.675 | 1.081 | 1.571 | 2.133 | 2.755 | 3.427 |
| 6 | 0.001 | 0.015 | 0.083 | 0.251 | 0.539 | 0.945 | 1.456 | 2.055 | 2.727 | 3.459 | 4.240 |
| 7 | 0.002 | 0.026 | 0.129 | 0.358 | 0.727 | 1.225 | 1.832 | 2.531 | 3.303 | 4.134 | 5.013 |
| 8 | 0.004 | 0.042 | 0.183 | 0.476 | 0.922 | 1.507 | 2.205 | 2.995 | 3.858 | 4.780 | 5.748 |
| 9 | 0.006 | 0.060 | 0.244 | 0.599 | 1.121 | 1.787 | 2.570 | 3.445 | 4.393 | 5.397 | 6.446 |
| 10 | 0.008 | 0.082 | 0.309 | 0.726 | 1.321 | 2.065 | 2.926 | 3.880 | 4.906 | 5.987 | 7.111 |
| 11 | 0.012 | 0.106 | 0.378 | 0.856 | 1.520 | 2.337 | 3.273 | 4.301 | 5.400 | 6.552 | 7.746 |
| 12 | 0.016 | 0.133 | 0.449 | 0.986 | 1.717 | 2.603 | 3.610 | 4.707 | 5.874 | 7.094 | 8.352 |
| 13 | 0.021 | 0.161 | 0.522 | 1.117 | 1.911 | 2.864 | 3.936 | 5.099 | 6.331 | 7.613 | 8.933 |
| 14 | 0.026 | 0191 | 0.596 | 1.246 | 2.102 | 3.118 | 4.253 | 5.478 | 6.771 | 8.112 | 9.489 |
| 15 | 0.032 | 0.222 | 0.671 | 1.375 | 2.290 | 3.365 | 4.561 | 5.845 | 7.195 | 8.592 | 10.024 |
| 16 | 0.039 | 0.254 | 0.746 | 1.503 | 2.474 | 3.606 | 4.859 | 6.199 | 7.604 | 9.054 | 10.538 |
| 17 | 0.046 | 0.287 | 0.820 | 1.628 | 2.653 | 3.841 | 5.149 | 6.543 | 7.999 | 9.500 | 11.033 |


| 18 | 0.053 | 0.320 | 0.895 | 1.752 | 2.829 | 4.070 | 5.430 | 6.875 | 8.381 | 9.931 | 11.510 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.060 | 0.353 | 0.969 | 1.874 | 3.001 | 4.293 | 5.703 | 7.197 | 8.751 | 10.347 | 11.970 |
| 20 | 0.068 | 0.387 | 1.042 | 1.993 | 3.169 | 4.510 | 5.968 | 7.510 | 9.110 | 10.750 | 12.415 |
| 21 | 0.077 | 0.421 | 1.115 | 2.111 | 3.334 | 4.721 | 6.226 | 7.813 | 9.457 | 11.139 | 12.846 |
| 22 | 0.085 | 0.455 | 1.187 | 2.226 | 3.494 | 4.928 | 6.477 | 8.108 | 9.794 | 11.517 | 13.262 |
| 23 | 0.094 | 0.489 | 1.257 | 2.339 | 3.651 | 5.129 | 6.721 | 8.394 | 10.121 | 11.883 | 13.666 |
| 24 | 0.102 | 0.522 | 1.327 | 2.449 | 3.805 | 5.324 | 6.959 | 8.672 | 10.438 | 12.238 | 14.057 |
| 25 | 0.111 | 0.556 | 1.396 | 2.558 | 3.955 | 5.516 | 7.191 | 8.943 | 10.747 | 12.583 | 14.437 |
| 26 | 0.120 | 0.589 | 1.463 | 2.664 | 4.101 | 5.702 | 7.416 | 9.207 | 11.048 | 12.919 | 14.806 |
| 27 | 0.129 | 0.622 | 1.530 | 2.769 | 4.244 | 5.884 | 7.636 | 9.464 | 11.340 | 13.245 | 15.164 |
| 28 | 0.138 | 0.654 | 1.595 | 2.871 | 4.384 | 6.062 | 7.851 | 9.714 | 11.624 | 13.562 | 15.513 |
| 29 | 0.147 | 0.686 | 1.659 | 2.971 | 4.521 | 6.236 | 8.060 | 9.958 | 11.902 | 13.871 | 15.852 |
| 30 | 0.155 | 0.718 | 1.723 | 3.069 | 4.655 | 6.405 | 8.265 | 10.196 | 12.172 | 14.172 | 16.182 |

Table B. 12
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 6 5} /$ Dividend Rate $=\mathbf{0 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.012 | 0.027 | 0.052 |
| 2 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.015 | 0.041 | 0.091 | 0.170 | 0.282 | 0.429 |
| 3 | 0.000 | 0.000 | 0.001 | 0.006 | 0.026 | 0.075 | 0.164 | 0.302 | 0.491 | 0.730 | 1.018 |
| 4 | 0.000 | 0.000 | 0.004 | 0.023 | 0.077 | 0.184 | 0.356 | 0.595 | 0.899 | 1.263 | 1.681 |
| 5 | 0.000 | 0.001 | 0.012 | 0.053 | 0.154 | 0.331 | 0.591 | 0.932 | 1.346 | 1.825 | 2.361 |
| 6 | 0.000 | 0.003 | 0.025 | 0.098 | 0.253 | 0.504 | 0.853 | 1.291 | 1.807 | 2.392 | 3.033 |
| 7 | 0.000 | 0.006 | 0.043 | 0.154 | 0.368 | 0.695 | 1.129 | 1.659 | 2.271 | 2.951 | 3.689 |
| 8 | 0.001 | 0.011 | 0.068 | 0.220 | 0.495 | 0.896 | 1.413 | 2.029 | 2.728 | 3.497 | 4.322 |
| 9 | 0.001 | 0.018 | 0.097 | 0.294 | 0.630 | 1.103 | 1.698 | 2.395 | 3.177 | 4.027 | 4.933 |
| 10 | 0.002 | 0.026 | 0.131 | 0.374 | 0.771 | 1.314 | 1.983 | 2.757 | 3.615 | 4.541 | 5.521 |
| 11 | 0.003 | 0.036 | 0.169 | 0.458 | 0.915 | 1.526 | 2.265 | 3.111 | 4.040 | 5.037 | 6.086 |
| 12 | 0.004 | 0.048 | 0.210 | 0.546 | 1.062 | 1.737 | 2.544 | 3.457 | 4.454 | 5.517 | 6.631 |
| 13 | 0.005 | 0.061 | 0.254 | 0.637 | 1.209 | 1.946 | 2.817 | 3.795 | 4.855 | 5.980 | 7.155 |
| 14 | 0.007 | 0.076 | 0.300 | 0.730 | 1.357 | 2.153 | 3.085 | 4.124 | 5.244 | 6.428 | 7.660 |
| 15 | 0.009 | 0.091 | 0.348 | 0.823 | 1.504 | 2.358 | 3.348 | 4.444 | 5.622 | 6.862 | 8.148 |
| 16 | 0.011 | 0.108 | 0.397 | 0.917 | 1.650 | 2.559 | 3.605 | 4.756 | 5.988 | 7.281 | 8.618 |
| 17 | 0.014 | 0.126 | 0.447 | 1.011 | 1.795 | 2.756 | 3.856 | 5.060 | 6.344 | 7.687 | 9.073 |


| 18 | 0.017 | 0.145 | 0.498 | 1.106 | 1.938 | 2.950 | 4.101 | 5.356 | 6.690 | 8.080 | 9.513 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.020 | 0.164 | 0.550 | 1.200 | 2.079 | 3.140 | 4.341 | 5.644 | 7.025 | 8.462 | 9.938 |
| 20 | 0.023 | 0.184 | 0.602 | 1.293 | 2.218 | 3.327 | 4.575 | 5.925 | 7.351 | 8.832 | 10.351 |
| 21 | 0.027 | 0.205 | 0.654 | 1.385 | 2.355 | 3.510 | 4.803 | 6.199 | 7.668 | 9.191 | 10.750 |
| 22 | 0.030 | 0.225 | 0.706 | 1.477 | 2.490 | 3.689 | 5.026 | 6.465 | 7.977 | 9.540 | 11.138 |
| 23 | 0.034 | 0.247 | 0.758 | 1.567 | 2.622 | 3.865 | 5.245 | 6.725 | 8.277 | 9.879 | 11.514 |
| 24 | 0.038 | 0.268 | 0.809 | 1.657 | 2.753 | 4.036 | 5.458 | 6.978 | 8.569 | 10.209 | 11.880 |
| 25 | 0.042 | 0.290 | 0.861 | 1.745 | 2.881 | 4.205 | 5.666 | 7.226 | 8.854 | 10.530 | 12.235 |
| 26 | 0.047 | 0.312 | 0.912 | 1.832 | 3.007 | 4.370 | 5.870 | 7.467 | 9.132 | 10.842 | 12.580 |
| 27 | 0.051 | 0.333 | 0.963 | 1.918 | 3.130 | 4.531 | 6.069 | 7.702 | 9.402 | 11.146 | 12.916 |
| 28 | 0.056 | 0.355 | 1.014 | 2.003 | 3.251 | 4.689 | 6.263 | 7.932 | 9.666 | 11.443 | 13.244 |
| 29 | 0.060 | 0.377 | 1.063 | 2.087 | 3.370 | 4.845 | 6.454 | 8.157 | 9.924 | 11.731 | 13.562 |
| 20 | 0.065 | 0.399 | 1.113 | 2.169 | 3.487 | 4.996 | 6.640 | 8.377 | 10.175 | 12.013 | 13.873 |

Table B. 13
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 6 0} /$ Dividend Rate $=\mathbf{0 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.002 | 0.006 | 0.013 |
| 2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.003 | 0.010 | 0.028 | 0.061 | 0.115 | 0.193 |
| 3 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.022 | 0.059 | 0.126 | 0.229 | 0.373 | 0.559 |
| 4 | 0.000 | 0.000 | 0.001 | 0.005 | 0.023 | 0.069 | 0.155 | 0.292 | 0.483 | 0.728 | 1.026 |
| 5 | 0.000 | 0.000 | 0.003 | 0.015 | 0.056 | 0.143 | 0.292 | 0.507 | 0.789 | 1.135 | 1.539 |
| 6 | 0.000 | 0.001 | 0.006 | 0.032 | 0.104 | 0.242 | 0.458 | 0.754 | 1.125 | 1.566 | 2.069 |
| 7 | 0.000 | 0.002 | 0.012 | 0.057 | 0.166 | 0.359 | 0.644 | 1.020 | 1.477 | 2.008 | 2.602 |
| 8 | 0.000 | 0.003 | 0.022 | 0.089 | 0.239 | 0.490 | 0.845 | 1.297 | 1.836 | 2.451 | 3.129 |
| 9 | 0.000 | 0.005 | 0.034 | 0.128 | 0.322 | 0.632 | 1.055 | 1.581 | 2.197 | 2.889 | 3.646 |
| 10 | 0.000 | 0.007 | 0.049 | 0.173 | 0.413 | 0.781 | 1.270 | 1.866 | 2.555 | 3.321 | 4.150 |
| 11 | 0.001 | 0.011 | 0.067 | 0.222 | 0.509 | 0.935 | 1.488 | 2.152 | 2.909 | 3.744 | 4.641 |
| 12 | 0.001 | 0.015 | 0.088 | 0.276 | 0.610 | 1.092 | 1.707 | 2.435 | 3.257 | 4.157 | 5.118 |
| 13 | 0.001 | 0.020 | 0.111 | 0.333 | 0.714 | 1.251 | 1.925 | 2.715 | 3.599 | 4.560 | 5.581 |
| 14 | 0.002 | 0.026 | 0.136 | 0.393 | 0.821 | 1.411 | 2.143 | 2.991 | 3.934 | 4.952 | 6.030 |
| 15 | 0.002 | 0.033 | 0.163 | 0.456 | 0.929 | 1.572 | 2.358 | 3.262 | 4.261 | 5.334 | 6.465 |
| 16 | 0.003 | 0.041 | 0.192 | 0.520 | 1.039 | 1.732 | 2.571 | 3.529 | 4.581 | 5.706 | 6.888 |
| 17 | 0.004 | 0.049 | 0.222 | 0.586 | 1.149 | 1.891 | 2.781 | 3.790 | 4.893 | 6.068 | 7.298 |


| 18 | 0.005 | 0.059 | 0.254 | 0.652 | 1.259 | 2.048 | 2.988 | 4.047 | 5.198 | 6.420 | 7.696 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.006 | 0.068 | 0.287 | 0.720 | 1.369 | 2.204 | 3.191 | 4.298 | 5.495 | 6.763 | 8.083 |
| 20 | 0.007 | 0.079 | 0.320 | 0.788 | 1.479 | 2.359 | 3.392 | 4.543 | 5.786 | 7.097 | 8.458 |
| 21 | 0.008 | 0.090 | 0.354 | 0.857 | 1.587 | 2.511 | 3.588 | 4.784 | 6.069 | 7.422 | 8.824 |
| 22 | 0.010 | 0.101 | 0.389 | 0.925 | 1.696 | 2.661 | 3.781 | 5.019 | 6.346 | 7.739 | 9.179 |
| 23 | 0.011 | 0.113 | 0.425 | 0.994 | 1.803 | 2.810 | 3.971 | 5.250 | 6.617 | 8.048 | 9.525 |
| 24 | 0.013 | 0.125 | 0.460 | 1.062 | 1.909 | 2.956 | 4.157 | 5.476 | 6.881 | 8.349 | 9.861 |
| 25 | 0.014 | 0.138 | 0.496 | 1.130 | 2.014 | 3.099 | 4.340 | 5.696 | 7.139 | 8.643 | 10.189 |
| 26 | 0.016 | 0.151 | 0.532 | 1.198 | 2.118 | 3.241 | 4.519 | 5.913 | 7.391 | 8.929 | 10.508 |
| 27 | 0.018 | 0.164 | 0.569 | 1.266 | 2.220 | 3.380 | 4.695 | 6.124 | 7.637 | 9.209 | 10.820 |
| 28 | 0.020 | 0.177 | 0.605 | 1.333 | 2.322 | 3.517 | 4.867 | 6.332 | 7.878 | 9.482 | 11.123 |
| 29 | 0.022 | 0.191 | 0.641 | 1.399 | 2.422 | 3.651 | 5.036 | 6.535 | 8.114 | 9.748 | 11.419 |
| 30 | 0.024 | 0.204 | 0.677 | 1.465 | 2.520 | 3.784 | 5.202 | 6.733 | 8.344 | 10.009 | 11.708 |

Table B. 14
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 120 /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.057 | 20.217 | 20.451 | 20.742 | 21.077 | 21.450 |
| 2 | 20.000 | 20.000 | 20.000 | 20.011 | 20.214 | 20.585 | 21.063 | 21.617 | 22.225 | 22.876 | 23.559 |
| 3 | 20.000 | 20.000 | 20.000 | 20.167 | 20.625 | 21.246 | 21.969 | 22.761 | 23.604 | 24.484 | 25.391 |
| 4 | 20.000 | 20.000 | 20.020 | 20.407 | 21.077 | 21.903 | 22.826 | 23.812 | 24.843 | 25.907 | 26.995 |
| 5 | 20.000 | 20.000 | 20.097 | 20.676 | 21.529 | 22.531 | 23.622 | 24.773 | 25.964 | 27.184 | 28.425 |
| 6 | 20.000 | 20.000 | 20.205 | 20.954 | 21.967 | 23.122 | 24.361 | 25.656 | 26.987 | 28.344 | 29.719 |
| 7 | 20.000 | 20.000 | 20.330 | 21.231 | 22.387 | 23.678 | 25.050 | 26.474 | 27.931 | 29.410 | 30.905 |
| 8 | 20.000 | 20.000 | 20.464 | 21.501 | 22.787 | 24.203 | 25.695 | 27.235 | 28.806 | 30.397 | 32.000 |
| 9 | 20.000 | 20.001 | 20.601 | 21.764 | 23.168 | 24.698 | 26.301 | 27.948 | 29.624 | 31.317 | 33.020 |
| 10 | 20.000 | 20.013 | 20.740 | 22.018 | 23.532 | 25.167 | 26.873 | 28.620 | 30.392 | 32.180 | 33.975 |
| 11 | 20.000 | 20.034 | 20.877 | 22.263 | 23.879 | 25.613 | 27.414 | 29.254 | 31.117 | 32.992 | 34.872 |
| 12 | 20.000 | 20.061 | 21.013 | 22.499 | 24.211 | 26.037 | 27.928 | 29.855 | 31.803 | 33.760 | 35.720 |
| 13 | 20.000 | 20.092 | 21.146 | 22.726 | 24.528 | 26.442 | 28.417 | 30.427 | 32.454 | 34.488 | 36.523 |
| 14 | 20.000 | 20.127 | 21.277 | 22.946 | 24.833 | 26.829 | 28.884 | 30.971 | 33.074 | 35.181 | 37.286 |
| 15 | 20.000 | 20.165 | 21.404 | 23.158 | 25.126 | 27.200 | 29.331 | 31.492 | 33.665 | 35.841 | 38.014 |
| 17 | 20.000 | 20.204 | 21.529 | 23.362 | 25.407 | 27.556 | 29.760 | 31.990 | 34.231 | 36.473 | 38.709 |
| 17 | 20.000 | 20.244 | 21.650 | 23.560 | 25.678 | 27.899 | 30.171 | 32.467 | 34.773 | 37.078 | 39.375 |


| 18 | 20.000 | 20.285 | 21.768 | 23.751 | 25.940 | 28.228 | 30.566 | 32.926 | 35.294 | 37.658 | 40.013 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 20.000 | 20.326 | 21.883 | 23.935 | 26.192 | 28.545 | 30.946 | 33.367 | 35.794 | 38.216 | 40.626 |
| 20 | 20.000 | 20.368 | 21.994 | 24.114 | 26.436 | 28.851 | 31.312 | 33.793 | 36.276 | 38.753 | 41.216 |
| 21 | 20.000 | 20.409 | 22.103 | 24.287 | 26.671 | 29.147 | 31.666 | 34.203 | 36.741 | 39.271 | 41.784 |
| 22 | 20.000 | 20.450 | 22.209 | 24.455 | 26.899 | 29.432 | 32.008 | 34.599 | 37.190 | 39.771 | 42.332 |
| 23 | 20.000 | 20.491 | 22.312 | 24.618 | 27.119 | 29.709 | 32.339 | 34.983 | 37.624 | 40.253 | 42.861 |
| 24 | 20.000 | 20.532 | 22.413 | 24.776 | 27.333 | 29.977 | 32.659 | 35.353 | 38.044 | 40.720 | 43.373 |
| 25 | 20.000 | 20.572 | 22.511 | 24.930 | 27.540 | 30.236 | 32.969 | 35.713 | 38.451 | 41.172 | 43.868 |
| 26 | 20.000 | 20.612 | 22.606 | 25.079 | 27.741 | 30.488 | 33.270 | 36.061 | 38.845 | 41.609 | 44.347 |
| 27 | 20.000 | 20.651 | 22.699 | 25.224 | 27.936 | 30.732 | 33.562 | 36.399 | 39.227 | 42.034 | 44.811 |
| 28 | 20.000 | 20.690 | 22.790 | 25.364 | 28.126 | 30.970 | 33.846 | 36.728 | 39.598 | 42.446 | 45.262 |
| 29 | 20.000 | 20.728 | 22.878 | 25.501 | 28.311 | 31.201 | 34.122 | 37.047 | 39.959 | 42.846 | 45.699 |
| 30 | 20.000 | 20.765 | 22.964 | 25.634 | 28.490 | 31.425 | 34.390 | 37.357 | 40.309 | 43.234 | 46.123 |

Table B. 15
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 115 /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 15.000 | 15.000 | 15.000 | 15.010 | 15.141 | 15.376 | 15.682 | 16.041 | 16.440 | 16.871 | 17.326 |
| 2 | 15.000 | 15.000 | 15.027 | 15.301 | 15.749 | 16.300 | 16.919 | 17.585 | 18.285 | 19.011 | 19.757 |
| 3 | 15.000 | 15.000 | 15.188 | 15.714 | 16.405 | 17.191 | 18.038 | 18.927 | 19.844 | 20.783 | 21.738 |
| 4 | 15.000 | 15.006 | 15.406 | 16.137 | 17.025 | 18.001 | 19.032 | 20.100 | 21.193 | 22.304 | 23.427 |
| 5 | 15.000 | 15.050 | 15.638 | 16.545 | 17.600 | 18.737 | 19.925 | 21.145 | 22.388 | 23.645 | 24.913 |
| 6 | 15.000 | 15.119 | 15.872 | 16.931 | 18.133 | 19.411 | 20.737 | 22.091 | 23.465 | 24.852 | 26.246 |
| 7 | 15.000 | 15.201 | 16.100 | 17.296 | 18.628 | 20.033 | 21.482 | 22.957 | 24.449 | 25.952 | 27.460 |
| 8 | 15.000 | 15.290 | 16.321 | 17.640 | 19.091 | 20.612 | 22.172 | 23.758 | 25.357 | 26.965 | 28.576 |
| 9 | 15.000 | 15.382 | 16.532 | 17.965 | 19.525 | 21.152 | 22.816 | 24.502 | 26.201 | 27.905 | 29.610 |
| 10 | 15.000 | 15.474 | 16.736 | 18.273 | 19.934 | 21.659 | 23.420 | 25.200 | 26.990 | 28.783 | 30.576 |
| 11 | 15.000 | 15.566 | 16.930 | 18.566 | 20.321 | 22.138 | 23.988 | 25.856 | 27.731 | 29.608 | 31.482 |
| 12 | 15.000 | 15.657 | 17.117 | 18.844 | 20.688 | 22.591 | 24.525 | 26.475 | 28.431 | 30.386 | 32.337 |
| 12 | 15.001 | 16.001 | 17.791 | 19.837 | 21.991 | 24.196 | 26.424 | 28.661 | 30.896 | 33.125 | 35.341 |
| 13 | 15.000 | 15.746 | 17.296 | 19.109 | 21.037 | 23.021 | 25.035 | 27.062 | 29.093 | 31.122 | 33.145 |
| 14 | 15.000 | 15.833 | 17.467 | 19.362 | 21.369 | 23.431 | 25.520 | 27.620 | 29.723 | 31.822 | 33.913 |
| 15 | 15.000 | 15.918 | 17.632 | 19.604 | 21.687 | 23.822 | 25.982 | 28.152 | 30.323 | 32.488 | 34.644 |
| 15.004 | 16.081 | 17.944 | 20.060 | 22.282 | 24.554 | 26.847 | 29.148 | 31.445 | 33.734 | 36.008 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 15.009 | 16.159 | 18.091 | 20.274 | 22.562 | 24.898 | 27.253 | 29.615 | 31.972 | 34.318 | 36.648 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 15.015 | 16.235 | 18.233 | 20.481 | 22.831 | 25.228 | 27.644 | 30.064 | 32.477 | 34.878 | 37.262 |
| 20 | 15.023 | 16.308 | 18.370 | 20.679 | 23.090 | 25.546 | 28.020 | 30.496 | 32.964 | 35.418 | 37.852 |
| 21 | 15.031 | 16.380 | 18.502 | 20.871 | 23.340 | 25.853 | 28.382 | 30.912 | 33.433 | 35.938 | 38.420 |
| 22 | 15.040 | 16.449 | 18.630 | 21.056 | 23.581 | 26.149 | 28.732 | 31.314 | 33.886 | 36.439 | 38.968 |
| 23 | 15.050 | 16.517 | 18.754 | 21.235 | 23.814 | 26.435 | 29.070 | 31.703 | 34.323 | 36.923 | 39.497 |
| 24 | 15.060 | 16.582 | 18.873 | 21.407 | 24.039 | 26.712 | 29.397 | 32.078 | 34.745 | 37.390 | 40.008 |
| 25 | 15.070 | 16.646 | 18.989 | 21.575 | 24.258 | 26.980 | 29.714 | 32.442 | 35.154 | 37.843 | 40.502 |
| 26 | 15.081 | 16.708 | 19.101 | 21.737 | 24.469 | 27.240 | 30.021 | 32.794 | 35.551 | 38.281 | 40.980 |
| 27 | 15.092 | 16.768 | 19.210 | 21.894 | 24.674 | 27.492 | 30.318 | 33.136 | 35.935 | 38.706 | 41.444 |
| 28 | 15.103 | 16.826 | 19.315 | 22.047 | 24.873 | 27.737 | 30.607 | 33.468 | 36.308 | 39.118 | 41.893 |
| 29 | 15.114 | 16.882 | 19.417 | 22.195 | 25.067 | 27.974 | 30.888 | 33.790 | 36.670 | 39.519 | 42.329 |
| 20 | 15.124 | 16.937 | 19.516 | 22.339 | 25.254 | 28.205 | 31.161 | 34.103 | 37.022 | 39.907 | 42.753 |

Table B. 16
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 110 /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 10.000 | 10.000 | 10.087 | 10.340 | 10.685 | 11.089 | 11.534 | 12.007 | 12.502 | 13.014 | 13.538 |
| 2 | 10.000 | 10.084 | 10.490 | 11.055 | 11.703 | 12.401 | 13.133 | 13.886 | 14.656 | 15.438 | 16.228 |
| 3 | 10.000 | 10.274 | 10.920 | 11.712 | 12.580 | 13.491 | 14.429 | 15.386 | 16.355 | 17.334 | 18.318 |
| 4 | 10.003 | 10.482 | 11.322 | 12.298 | 13.342 | 14.425 | 15.532 | 16.654 | 17.786 | 18.925 | 20.068 |
| 5 | 10.031 | 10.689 | 11.691 | 12.823 | 14.018 | 15.248 | 16.499 | 17.763 | 19.035 | 20.312 | 21.590 |
| 6 | 10.075 | 10.887 | 12.031 | 13.300 | 14.627 | 15.987 | 17.365 | 18.754 | 20.150 | 21.548 | 22.947 |
| 7 | 10.127 | 11.074 | 12.346 | 13.737 | 15.183 | 16.660 | 18.153 | 19.655 | 21.162 | 22.669 | 24.175 |
| 8 | 10.182 | 11.251 | 12.638 | 14.140 | 15.695 | 17.278 | 18.877 | 20.482 | 22.089 | 23.696 | 25.300 |
| 9 | 10.238 | 11.419 | 12.911 | 14.515 | 16.171 | 17.853 | 19.547 | 21.247 | 22.948 | 24.647 | 26.342 |
| 10 | 10.294 | 11.577 | 13.166 | 14.866 | 16.615 | 18.388 | 20.173 | 21.961 | 23.749 | 25.533 | 27.312 |
| 11 | 10.350 | 11.726 | 13.407 | 15.196 | 17.032 | 18.891 | 20.759 | 22.631 | 24.500 | 26.364 | 28.221 |
| 12 | 10.404 | 11.868 | 13.634 | 15.507 | 17.425 | 19.364 | 21.312 | 23.261 | 25.207 | 27.147 | 29.077 |
| 12 | 10.457 | 12.003 | 13.850 | 15.801 | 17.797 | 19.812 | 21.835 | 23.858 | 25.876 | 27.887 | 29.886 |
| 13 | 10.508 | 12.132 | 14.054 | 16.080 | 18.149 | 20.237 | 22.331 | 24.425 | 26.512 | 28.589 | 30.653 |
| 15 | 10.557 | 12.255 | 14.249 | 16.345 | 18.485 | 20.642 | 22.804 | 24.964 | 27.116 | 29.257 | 31.384 |
| 17 | 10.605 | 12.372 | 14.435 | 16.599 | 18.805 | 21.028 | 23.255 | 25.479 | 27.693 | 29.895 | 32.080 |
| 17 | 12.652 | 12.484 | 14.612 | 16.841 | 19.111 | 21.397 | 23.687 | 25.971 | 28.245 | 30.504 | 32.746 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 10.697 | 12.591 | 14.781 | 17.072 | 19.404 | 21.751 | 24.100 | 26.443 | 28.774 | 31.089 | 33.384 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 10.740 | 12.694 | 14.944 | 17.294 | 19.685 | 22.091 | 24.497 | 26.896 | 29.282 | 31.649 | 33.996 |
| 20 | 10.782 | 12.792 | 15.099 | 17.508 | 19.956 | 22.418 | 24.879 | 27.332 | 29.770 | 32.189 | 34.584 |
| 21 | 10.821 | 12.886 | 15.249 | 17.713 | 20.216 | 22.732 | 25.247 | 27.752 | 30.240 | 32.708 | 35.150 |
| 22 | 10.860 | 12.977 | 15.393 | 17.911 | 20.467 | 23.036 | 25.602 | 28.157 | 30.694 | 33.208 | 35.696 |
| 23 | 10.896 | 13.064 | 15.532 | 18.102 | 20.710 | 23.329 | 25.945 | 28.548 | 31.132 | 33.691 | 36.222 |
| 24 | 10.931 | 13.148 | 15.666 | 18.286 | 20.944 | 23.612 | 26.276 | 28.926 | 31.555 | 34.158 | 36.731 |
| 25 | 10.965 | 13.229 | 15.795 | 18.464 | 21.170 | 23.886 | 26.597 | 29.292 | 31.965 | 34.610 | 37.222 |
| 26 | 10.998 | 13.307 | 15.920 | 18.636 | 21.389 | 24.151 | 26.907 | 29.646 | 32.361 | 35.047 | 37.698 |
| 27 | 11.029 | 13.382 | 16.041 | 18.803 | 21.602 | 24.409 | 27.208 | 29.990 | 32.746 | 35.471 | 38.159 |
| 28 | 11.059 | 13.455 | 16.158 | 18.964 | 21.807 | 24.658 | 27.500 | 30.323 | 33.119 | 35.881 | 38.606 |
| 29 | 11.088 | 13.525 | 16.271 | 19.121 | 22.007 | 24.900 | 27.784 | 30.647 | 33.481 | 36.280 | 39.040 |
| 20 | 11.116 | 13.593 | 16.381 | 19.273 | 22.201 | 25.136 | 28.059 | 30.961 | 33.833 | 36.667 | 39.460 |

Table B. 17
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 105 / \text { Dividend Rate }=1 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 5.070 | 5.398 | 5.835 | 6.322 | 6.839 | 7.372 | 7.918 | 8.472 | 9.031 | 9.595 | 10.162 |
| 2 | 5.312 | 5.937 | 6.653 | 7.410 | 8.188 | 8.979 | 9.778 | 10.582 | 11.390 | 12.200 | 13.011 |
| 3 | 5.546 | 6.382 | 7.301 | 8.254 | 9.224 | 10.205 | 11.192 | 12.182 | 13.174 | 14.167 | 15.160 |
| 4 | 5.755 | 6.761 | 7.843 | 8.956 | 10.084 | 11.221 | 12.362 | 13.506 | 14.650 | 15.793 | 16.936 |
| 5 | 5.942 | 7.091 | 8.312 | 9.563 | 10.828 | 12.100 | 13.374 | 14.650 | 15.925 | 17.199 | 18.470 |
| 6 | 6.110 | 7.384 | 8.729 | 10.102 | 11.487 | 12.878 | 14.272 | 15.665 | 17.057 | 18.446 | 19.831 |
| 7 | 6.261 | 7.648 | 9.104 | 10.587 | 12.082 | 13.581 | 15.082 | 16.582 | 18.079 | 19.572 | 21.061 |
| 8 | 6.400 | 7.889 | 9.447 | 11.030 | 12.624 | 14.223 | 15.823 | 17.420 | 19.014 | 20.603 | 22.186 |
| 9 | 6.528 | 8.110 | 9.761 | 11.438 | 13.125 | 14.816 | 16.507 | 18.195 | 19.878 | 21.555 | 23.225 |
| 10 | 6.646 | 8.314 | 10.052 | 11.816 | 13.590 | 15.367 | 17.143 | 18.915 | 20.682 | 22.441 | 24.192 |
| 11 | 6.755 | 8.504 | 10.323 | 12.169 | 14.024 | 15.882 | 17.739 | 19.590 | 21.435 | 23.271 | 25.097 |
| 12 | 6.856 | 8.681 | 10.577 | 12.500 | 14.432 | 16.367 | 18.299 | 20.225 | 22.144 | 24.052 | 25.949 |
| 13 | 6.950 | 8.847 | 10.816 | 12.812 | 14.818 | 16.825 | 18.828 | 20.826 | 22.813 | 24.790 | 26.753 |
| 14 | 7.038 | 9.003 | 11.042 | 13.107 | 15.182 | 17.258 | 19.330 | 21.395 | 23.448 | 25.490 | 27.516 |
| 15 | 7.121 | 9.150 | 11.255 | 13.387 | 15.529 | 17.671 | 19.808 | 21.936 | 24.053 | 26.155 | 28.241 |
| 17 | 7.199 | 9.290 | 11.458 | 13.654 | 15.859 | 18.064 | 20.263 | 22.452 | 24.629 | 26.790 | 28.933 |
| 12 | 9.422 | 11.651 | 13.908 | 16.174 | 18.439 | 20.698 | 22.946 | 25.180 | 27.397 | 29.594 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 7.342 | 9.548 | 11.835 | 14.150 | 16.475 | 18.799 | 21.115 | 23.419 | 25.707 | 27.978 | 30.227 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 7.408 | 9.668 | 12.011 | 14.383 | 16.764 | 19.143 | 21.515 | 23.873 | 26.214 | 28.535 | 30.834 |
| 20 | 7.471 | 9.783 | 12.180 | 14.606 | 17.041 | 19.475 | 21.899 | 24.309 | 26.701 | 29.071 | 31.417 |
| 21 | 7.531 | 9.892 | 12.341 | 14.820 | 17.308 | 19.794 | 22.269 | 24.729 | 27.170 | 29.587 | 31.979 |
| 22 | 7.588 | 9.997 | 12.496 | 15.026 | 17.565 | 20.101 | 22.626 | 25.134 | 27.622 | 30.085 | 32.520 |
| 23 | 7.642 | 10.098 | 12.646 | 15.225 | 17.813 | 20.397 | 22.970 | 25.525 | 28.058 | 30.565 | 33.042 |
| 24 | 7.694 | 10.195 | 12.789 | 15.417 | 18.052 | 20.684 | 23.303 | 25.903 | 28.480 | 31.028 | 33.546 |
| 25 | 7.744 | 10.288 | 12.928 | 15.602 | 18.284 | 20.961 | 23.625 | 26.269 | 28.887 | 31.477 | 34.033 |
| 26 | 7.791 | 10.377 | 13.062 | 15.780 | 18.507 | 21.229 | 23.936 | 26.623 | 29.282 | 31.911 | 34.505 |
| 27 | 7.837 | 10.463 | 13.191 | 15.953 | 18.724 | 21.489 | 24.238 | 26.966 | 29.665 | 32.332 | 34.961 |
| 28 | 7.880 | 10.546 | 13.316 | 16.121 | 18.934 | 21.741 | 24.531 | 27.298 | 30.036 | 32.739 | 35.404 |
| 29 | 7.922 | 10.626 | 13.436 | 16.283 | 19.138 | 21.985 | 24.816 | 27.622 | 30.396 | 33.135 | 35.834 |
| 20 | 7.962 | 10.704 | 13.553 | 16.440 | 19.335 | 22.223 | 25.092 | 27.935 | 30.746 | 33.520 | 36.251 |

Table B. 18
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 100 /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 1.551 | 2.121 | 2.692 | 3.264 | 3.837 | 4.409 | 4.982 | 5.554 | 6.126 | 6.698 | 7.270 |
| 2 | 2.103 | 2.903 | 3.705 | 4.510 | 5.315 | 6.120 | 6.925 | 7.730 | 8.534 | 9.338 | 10.140 |
| 3 | 2.496 | 3.467 | 4.445 | 5.425 | 6.406 | 7.387 | 8.368 | 9.349 | 10.328 | 11.306 | 12.283 |
| 4 | 2.806 | 3.921 | 5.043 | 6.170 | 7.297 | 8.425 | 9.553 | 10.679 | 11.803 | 12.926 | 14.046 |
| 5 | 3.066 | 4.304 | 5.553 | 6.806 | 8.061 | 9.317 | 10.571 | 11.824 | 13.075 | 14.322 | 15.567 |
| 6 | 3.289 | 4.638 | 5.999 | 7.366 | 8.735 | 10.104 | 11.472 | 12.838 | 14.201 | 15.560 | 16.915 |
| 7 | 3.486 | 4.935 | 6.398 | 7.868 | 9.341 | 10.813 | 12.284 | 13.752 | 15.217 | 16.677 | 18.131 |
| 8 | 3.662 | 5.202 | 6.759 | 8.324 | 9.892 | 11.460 | 13.026 | 14.588 | 16.146 | 17.698 | 19.244 |
| 9 | 3.820 | 5.446 | 7.090 | 8.743 | 10.400 | 12.056 | 13.709 | 15.359 | 17.003 | 18.641 | 20.270 |
| 10 | 3.965 | 5.670 | 7.396 | 9.131 | 10.871 | 12.610 | 14.345 | 16.076 | 17.801 | 19.518 | 21.226 |
| 11 | 4.098 | 5.877 | 7.680 | 9.493 | 11.310 | 13.127 | 14.940 | 16.747 | 18.547 | 20.339 | 22.120 |
| 12 | 4.220 | 6.070 | 7.945 | 9.832 | 11.723 | 13.613 | 15.499 | 17.379 | 19.250 | 21.111 | 22.961 |
| 13 | 4.334 | 6.250 | 8.194 | 10.151 | 12.112 | 14.072 | 16.027 | 17.975 | 19.914 | 21.841 | 23.755 |
| 14 | 4.440 | 6.420 | 8.429 | 10.452 | 12.480 | 14.507 | 16.528 | 18.540 | 20.543 | 22.533 | 24.508 |
| 15 | 4.539 | 6.579 | 8.651 | 10.738 | 12.830 | 14.920 | 17.003 | 19.078 | 21.141 | 23.191 | 25.224 |
| 16 | 4.632 | 6.730 | 8.862 | 11.010 | 13.163 | 15.313 | 17.457 | 19.591 | 21.712 | 23.818 | 25.907 |
| 17 | 4.720 | 6.873 | 9.063 | 11.269 | 13.480 | 15.689 | 17.890 | 20.081 | 22.258 | 24.418 | 26.559 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 4.803 | 7.009 | 9.254 | 11.516 | 13.784 | 16.049 | 18.305 | 20.550 | 22.780 | 24.992 | 27.184 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 4.881 | 7.138 | 9.436 | 11.753 | 14.075 | 16.394 | 18.704 | 21.001 | 23.282 | 25.543 | 27.783 |
| 20 | 4.955 | 7.261 | 9.611 | 11.980 | 14.354 | 16.725 | 19.086 | 21.434 | 23.764 | 26.073 | 28.359 |
| 21 | 5.025 | 7.379 | 9.778 | 12.198 | 14.623 | 17.044 | 19.455 | 21.851 | 24.228 | 26.583 | 28.913 |
| 22 | 5.091 | 7.491 | 9.939 | 12.407 | 14.882 | 17.351 | 19.810 | 22.253 | 24.676 | 27.075 | 29.447 |
| 23 | 5.155 | 7.599 | 10.093 | 12.609 | 15.131 | 17.648 | 20.153 | 22.641 | 25.107 | 27.549 | 29.962 |
| 24 | 5.215 | 7.703 | 10.242 | 12.804 | 15.372 | 17.934 | 20.484 | 23.016 | 25.525 | 28.007 | 30.459 |
| 25 | 5.273 | 7.802 | 10.385 | 12.992 | 15.604 | 18.211 | 20.804 | 23.378 | 25.928 | 28.450 | 30.940 |
| 26 | 5.328 | 7.898 | 10.523 | 13.173 | 15.829 | 18.479 | 21.115 | 23.730 | 26.319 | 28.879 | 31.405 |
| 27 | 5.381 | 7.990 | 10.657 | 13.349 | 16.047 | 18.739 | 21.415 | 24.070 | 26.698 | 29.295 | 31.856 |
| 28 | 5.432 | 8.078 | 10.785 | 13.519 | 16.258 | 18.991 | 21.707 | 24.400 | 27.066 | 29.698 | 32.293 |
| 29 | 5.480 | 8.164 | 10.910 | 13.683 | 16.463 | 19.235 | 21.990 | 24.721 | 27.422 | 30.089 | 32.717 |
| 20 | 5.526 | 8.246 | 11.031 | 13.843 | 16.662 | 19.472 | 22.265 | 25.032 | 27.769 | 30.469 | 33.128 |

Table B. 19
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 95 /$ Dividend Rate $=\mathbf{1 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.204 | 0.511 | 0.899 | 1.338 | 1.807 | 2.298 | 2.802 | 3.317 | 3.839 | 4.366 | 4.898 |
| 2 | 0.537 | 1.097 | 1.738 | 2.423 | 3.136 | 3.867 | 4.609 | 5.359 | 6.114 | 6.874 | 7.637 |
| 3 | 0.832 | 1.576 | 2.400 | 3.266 | 4.158 | 5.066 | 5.984 | 6.909 | 7.838 | 8.771 | 9.706 |
| 4 | 1.087 | 1.981 | 2.954 | 3.968 | 5.007 | 6.061 | 7.124 | 8.193 | 9.266 | 10.341 | 11.418 |
| 5 | 1.312 | 2.334 | 3.434 | 4.576 | 5.741 | 6.921 | 8.110 | 9.304 | 10.501 | 11.700 | 12.898 |
| 6 | 1.511 | 2.646 | 3.860 | 5.114 | 6.393 | 7.685 | 8.986 | 10.291 | 11.598 | 12.906 | 14.212 |
| 7 | 1.691 | 2.927 | 4.243 | 5.600 | 6.981 | 8.375 | 9.777 | 11.183 | 12.590 | 13.996 | 15.399 |
| 8 | 1.854 | 3.183 | 4.592 | 6.044 | 7.518 | 9.006 | 10.501 | 11.999 | 13.497 | 14.993 | 16.486 |
| 9 | 2.004 | 3.418 | 4.914 | 6.452 | 8.014 | 9.588 | 11.169 | 12.753 | 14.336 | 15.915 | 17.490 |
| 10 | 2.141 | 3.635 | 5.212 | 6.832 | 8.474 | 10.130 | 11.792 | 13.455 | 15.117 | 16.773 | 18.424 |
| 11 | 2.269 | 3.837 | 5.490 | 7.186 | 8.905 | 10.637 | 12.375 | 14.113 | 15.848 | 17.577 | 19.299 |
| 12 | 2.387 | 4.025 | 5.750 | 7.519 | 9.310 | 11.114 | 12.923 | 14.732 | 16.536 | 18.334 | 20.123 |
| 13 | 2.498 | 4.202 | 5.995 | 7.832 | 9.693 | 11.565 | 13.441 | 15.317 | 17.187 | 19.049 | 20.901 |
| 14 | 2.602 | 4.369 | 6.227 | 8.129 | 10.055 | 11.992 | 13.933 | 15.871 | 17.804 | 19.727 | 21.639 |
| 15 | 2.699 | 4.527 | 6.446 | 8.410 | 10.399 | 12.398 | 14.400 | 16.399 | 18.391 | 20.372 | 22.340 |
| 16 | 2.791 | 4.676 | 6.654 | 8.678 | 10.726 | 12.785 | 14.846 | 16.903 | 18.951 | 20.988 | 23.010 |
| 17 | 2.878 | 4.818 | 6.852 | 8.934 | 11.039 | 13.155 | 15.273 | 17.385 | 19.487 | 21.576 | 23.649 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 2.960 | 4.952 | 7.042 | 9.178 | 11.339 | 13.510 | 15.681 | 17.846 | 20.000 | 22.140 | 24.262 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 3.038 | 5.081 | 7.223 | 9.413 | 11.626 | 13.850 | 16.073 | 18.289 | 20.493 | 22.681 | 24.850 |
| 20 | 3.111 | 5.204 | 7.396 | 9.637 | 11.902 | 14.176 | 16.450 | 18.715 | 20.966 | 23.201 | 25.415 |
| 21 | 3.182 | 5.321 | 7.562 | 9.853 | 12.168 | 14.491 | 16.813 | 19.125 | 21.422 | 23.702 | 25.958 |
| 22 | 3.249 | 5.433 | 7.722 | 10.061 | 12.423 | 14.794 | 17.163 | 19.520 | 21.862 | 24.184 | 26.482 |
| 23 | 3.313 | 5.541 | 7.876 | 10.261 | 12.670 | 15.087 | 17.500 | 19.902 | 22.287 | 24.650 | 26.988 |
| 24 | 3.374 | 5.645 | 8.024 | 10.454 | 12.908 | 15.370 | 17.827 | 20.271 | 22.697 | 25.100 | 27.476 |
| 25 | 3.432 | 5.745 | 8.166 | 10.640 | 13.138 | 15.643 | 18.143 | 20.628 | 23.094 | 25.536 | 27.948 |
| 26 | 3.488 | 5.841 | 8.304 | 10.821 | 13.361 | 15.908 | 18.448 | 20.974 | 23.479 | 25.957 | 28.405 |
| 27 | 3.542 | 5.933 | 8.437 | 10.995 | 13.577 | 16.164 | 18.745 | 21.309 | 23.851 | 26.366 | 28.848 |
| 28 | 3.593 | 6.022 | 8.566 | 11.164 | 13.786 | 16.413 | 19.032 | 21.635 | 24.213 | 26.762 | 29.277 |
| 29 | 3.642 | 6.108 | 8.690 | 11.328 | 13.989 | 16.655 | 19.312 | 21.950 | 24.564 | 27.147 | 29.693 |
| 30 | 3.689 | 6.191 | 8.811 | 11.486 | 14.186 | 16.889 | 19.583 | 22.257 | 24.905 | 27.520 | 30.098 |

Table B. 20
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 90 /$ Dividend Rate $=\mathbf{1 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.008 | 0.062 | 0.195 | 0.405 | 0.681 | 1.008 | 1.373 | 1.769 | 2.187 | 2.624 | 3.076 |
| 2 | 0.076 | 0.295 | 0.654 | 1.116 | 1.648 | 2.231 | 2.850 | 3.495 | 4.159 | 4.839 | 5.530 |
| 3 | 0.186 | 0.570 | 1.116 | 1.768 | 2.491 | 3.260 | 4.063 | 4.889 | 5.732 | 6.588 | 7.453 |
| 4 | 0.312 | 0.842 | 1.543 | 2.351 | 3.227 | 4.148 | 5.100 | 6.073 | 7.061 | 8.061 | 9.068 |
| 5 | 0.440 | 1.099 | 1.934 | 2.875 | 3.883 | 4.933 | 6.013 | 7.112 | 8.225 | 9.348 | 10.477 |
| 6 | 0.567 | 1.340 | 2.293 | 3.352 | 4.475 | 5.640 | 6.832 | 8.043 | 9.266 | 10.498 | 11.735 |
| 7 | 0.688 | 1.565 | 2.625 | 3.789 | 5.017 | 6.284 | 7.578 | 8.890 | 10.213 | 11.542 | 12.876 |
| 8 | 0.804 | 1.776 | 2.933 | 4.193 | 5.516 | 6.878 | 8.265 | 9.668 | 11.082 | 12.501 | 13.923 |
| 9 | 0.915 | 1.975 | 3.220 | 4.569 | 5.980 | 7.429 | 8.902 | 10.391 | 11.888 | 13.390 | 14.893 |
| 10 | 1.020 | 2.161 | 3.489 | 4.921 | 6.414 | 7.944 | 9.497 | 11.065 | 12.640 | 14.219 | 15.797 |
| 11 | 1.119 | 2.337 | 3.743 | 5.252 | 6.821 | 8.428 | 10.056 | 11.698 | 13.346 | 14.996 | 16.644 |
| 12 | 1.214 | 2.503 | 3.982 | 5.564 | 7.206 | 8.884 | 10.583 | 12.295 | 14.012 | 15.729 | 17.443 |
| 13 | 1.304 | 2.661 | 4.208 | 5.860 | 7.570 | 9.316 | 11.082 | 12.860 | 14.642 | 16.423 | 18.198 |
| 14 | 1.390 | 2.810 | 4.424 | 6.140 | 7.916 | 9.727 | 11.557 | 13.397 | 15.240 | 17.081 | 18.915 |
| 15 | 1.471 | 2.953 | 4.629 | 6.408 | 8.246 | 10.118 | 12.009 | 13.909 | 15.810 | 17.708 | 19.598 |
| 16 | 1.549 | 3.089 | 4.824 | 6.663 | 8.560 | 10.491 | 12.440 | 14.397 | 16.355 | 18.307 | 20.249 |
| 17 | 1.623 | 3.219 | 5.011 | 6.907 | 8.862 | 10.849 | 12.853 | 14.865 | 16.875 | 18.879 | 20.872 |


| 18 | 1.694 | 3.343 | 5.190 | 7.141 | 9.150 | 11.192 | 13.250 | 15.313 | 17.375 | 19.428 | 21.468 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 1.762 | 3.462 | 5.361 | 7.366 | 9.428 | 11.521 | 13.630 | 15.744 | 17.854 | 19.955 | 22.041 |
| 20 | 1.827 | 3.576 | 5.526 | 7.581 | 9.694 | 11.838 | 13.997 | 16.159 | 18.316 | 20.462 | 22.592 |
| 21 | 1.889 | 3.685 | 5.685 | 7.789 | 9.951 | 12.143 | 14.350 | 16.558 | 18.760 | 20.950 | 23.122 |
| 22 | 1.949 | 3.791 | 5.837 | 7.990 | 10.199 | 12.438 | 14.690 | 16.944 | 19.189 | 21.421 | 23.633 |
| 23 | 2.006 | 3.892 | 5.984 | 8.183 | 10.438 | 12.723 | 15.019 | 17.316 | 19.603 | 21.875 | 24.127 |
| 24 | 2.061 | 3.990 | 6.126 | 8.370 | 10.669 | 12.998 | 15.338 | 17.676 | 20.004 | 22.315 | 24.603 |
| 25 | 2.114 | 4.084 | 6.263 | 8.550 | 10.893 | 13.264 | 15.646 | 18.025 | 20.392 | 22.740 | 25.064 |
| 26 | 2.164 | 4.174 | 6.396 | 8.725 | 11.110 | 13.522 | 15.944 | 18.362 | 20.767 | 23.152 | 25.511 |
| 27 | 2.213 | 4.262 | 6.524 | 8.894 | 11.320 | 13.772 | 16.234 | 18.690 | 21.131 | 23.551 | 25.943 |
| 28 | 2.260 | 4.347 | 6.649 | 9.058 | 11.524 | 14.015 | 16.515 | 19.008 | 21.485 | 23.938 | 26.363 |
| 29 | 2.305 | 4.429 | 6.769 | 9.217 | 11.721 | 14.251 | 16.788 | 19.316 | 21.828 | 24.314 | 26.770 |
| 20 | 2.349 | 4.508 | 6.886 | 9.372 | 11.914 | 14.480 | 17.053 | 19.616 | 22.161 | 24.679 | 27.165 |

Table B. 21
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 85 /$ Dividend Rate $=1 \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.003 | 0.024 | 0084 | 0.193 | 0.355 | 0.566 | 0.819 | 1.108 | 1.427 | 1.771 |
| 2 | 0.005 | 0.052 | 0.187 | 0.423 | 0.750 | 1.151 | 1.610 | 2.116 | 2.657 | 3.227 | 3.820 |
| 3 | 0.026 | 0.155 | 0.431 | 0.839 | 1.352 | 1.942 | 2.591 | 3.284 | 4.010 | 4.762 | 5.534 |
| 4 | 0.062 | 0.288 | 0.700 | 1.259 | 1.928 | 2.674 | 3.477 | 4.321 | 5.196 | 6.095 | 7.012 |
| 5 | 0.110 | 0.435 | 0.971 | 1.664 | 2.467 | 3.346 | 4.281 | 5.254 | 6.256 | 7.280 | 8.320 |
| 6 | 0.166 | 0.586 | 1.236 | 2.048 | 2.970 | 3.967 | 5.016 | 6.103 | 7.217 | 8.351 | 9.499 |
| 7 | 0.226 | 0.737 | 1.492 | 2.411 | 3.440 | 4.542 | 5.695 | 6.884 | 8.098 | 9.330 | 10.575 |
| 8 | 0.289 | 0.886 | 1.737 | 2.755 | 3.881 | 5.079 | 6.326 | 7.608 | 8.913 | 10.235 | 11.568 |
| 9 | 0.353 | 1.032 | 1.972 | 3.080 | 4.295 | 5.582 | 6.916 | 8.284 | 9.673 | 11.077 | 12.490 |
| 10 | 0.417 | 1.172 | 2.196 | 3.388 | 4.687 | 6.056 | 7.471 | 8.917 | 10.385 | 11.865 | 13.353 |
| 11 | 0.480 | 1.309 | 2.410 | 3.681 | 5.058 | 6.504 | 7.994 | 9.515 | 11.055 | 12.607 | 14.165 |
| 12 | 0.543 | 1.440 | 2.615 | 3.960 | 5.411 | 6.928 | 8.490 | 10.080 | 11.689 | 13.307 | 14.931 |
| 13 | 0.604 | 1.567 | 2.812 | 4.227 | 5.746 | 7.332 | 8.961 | 10.617 | 12.290 | 13.972 | 15.657 |
| 14 | 0.664 | 1.689 | 3.000 | 4.481 | 6.067 | 7.718 | 9.410 | 11.129 | 12.862 | 14.604 | 16.347 |
| 15 | 0.722 | 1.807 | 3.181 | 4.725 | 6.373 | 8.086 | 9.839 | 11.617 | 13.409 | 15.207 | 17.005 |
| 17 | 0.779 | 1.921 | 3.355 | 4.959 | 6.667 | 8.439 | 10.249 | 12.084 | 13.931 | 15.783 | 17.633 |
| 14 | 2.030 | 3.522 | 5.184 | 6.949 | 8.777 | 10.643 | 12.532 | 14.432 | 16.335 | 18.234 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.887 | 2.136 | 3.683 | 5.401 | 7.221 | 9.102 | 11.022 | 12.962 | 14.912 | 16.864 | 18.811 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.939 | 2.238 | 3.838 | 5.609 | 7.482 | 9.416 | 11.386 | 13.376 | 15.375 | 17.373 | 19.365 |
| 20 | 0.989 | 2.337 | 3.988 | 5.810 | 7.734 | 9.718 | 11.737 | 13.775 | 15.820 | 17.863 | 19.898 |
| 21 | 1.038 | 2.433 | 4.132 | 6.004 | 7.977 | 10.009 | 12.075 | 14.159 | 16.249 | 18.335 | 20.411 |
| 22 | 1.085 | 2.525 | 4.272 | 6.192 | 8.212 | 10.291 | 12.402 | 14.531 | 16.664 | 18.791 | 20.906 |
| 23 | 1.130 | 2.614 | 4.408 | 6.374 | 8.439 | 10.563 | 12.719 | 14.890 | 17.064 | 19.231 | 21.385 |
| 24 | 1.175 | 2.701 | 4.538 | 6.549 | 8.659 | 10.827 | 13.025 | 15.238 | 17.452 | 19.657 | 21.847 |
| 25 | 1.217 | 2.784 | 4.665 | 6.720 | 8.873 | 11.082 | 13.322 | 15.575 | 17.827 | 20.070 | 22.295 |
| 26 | 1.259 | 2.866 | 4.788 | 6.885 | 9.080 | 11.330 | 13.610 | 15.901 | 18.191 | 20.469 | 22.728 |
| 27 | 1.299 | 2.944 | 4.908 | 7.045 | 9.280 | 11.571 | 13.889 | 16.219 | 18.544 | 20.857 | 23.149 |
| 28 | 1.338 | 3.021 | 5.024 | 7.201 | 9.475 | 11.804 | 14.161 | 16.526 | 18.887 | 21.233 | 23.556 |
| 29 | 1.376 | 3.095 | 5.136 | 7.352 | 9.665 | 12.032 | 14.425 | 16.826 | 19.220 | 21.598 | 23.952 |
| 30 | 1.413 | 3.167 | 5.245 | 7.499 | 9.849 | 12.253 | 14.681 | 17.117 | 19.544 | 21.953 | 24.336 |

Table B. 22
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 80 /$ Dividend Rate $=1 \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.002 | 0.011 | 0.039 | 0.096 | 0.188 | 0.318 | 0.485 | 0.686 | 0.918 |
| 2 | 0.000 | 0.006 | 0.038 | 0.126 | 0.286 | 0.517 | 0.815 | 1.170 | 1.574 | 2.017 | 2.494 |
| 3 | 0.002 | 0.030 | 0.133 | 0.339 | 0.650 | 1.053 | 1.531 | 2.071 | 2.660 | 3.288 | 3.948 |
| 4 | 0.008 | 0.076 | 0.267 | 0.597 | 1.050 | 1.603 | 2.235 | 2.928 | 3.668 | 4.446 | 5.253 |
| 5 | 0.020 | 0.140 | 0.424 | 0.872 | 1.454 | 2.139 | 2.903 | 3.727 | 4.596 | 5.501 | 6.433 |
| 6 | 0.037 | 0.215 | 0.593 | 1.150 | 1.848 | 2.652 | 3.533 | 4.472 | 5.455 | 6.471 | 7.512 |
| 7 | 0.058 | 0.298 | 0.766 | 1.426 | 2.230 | 3.139 | 4.126 | 5.168 | 6.253 | 7.368 | 8.507 |
| 8 | 0.083 | 0.387 | 0.940 | 1.695 | 2.597 | 3.603 | 4.685 | 5.822 | 6.998 | 8.204 | 9.431 |
| 9 | 0.112 | 0.478 | 1.113 | 1.957 | 2.949 | 4.044 | 5.214 | 6.437 | 7.698 | 8.987 | 10.295 |
| 10 | 0.142 | 0.570 | 1.284 | 2.210 | 3.286 | 4.465 | 5.716 | 7.019 | 8.358 | 9.724 | 11.106 |
| 11 | 0.175 | 0.663 | 1.450 | 2.455 | 3.609 | 4.866 | 6.193 | 7.571 | 8.983 | 10.420 | 11.872 |
| 12 | 0.208 | 0.755 | 1.613 | 2.691 | 3.919 | 5.249 | 6.648 | 8.096 | 9.576 | 11.080 | 12.597 |
| 13 | 0.243 | 0.846 | 1.771 | 2.920 | 4.217 | 5.616 | 7.083 | 8.596 | 10.141 | 11.707 | 13.286 |
| 14 | 0.278 | 0.936 | 1.925 | 3.140 | 4.504 | 5.968 | 7.498 | 9.074 | 10.681 | 12.306 | 13.943 |
| 15 | 0.313 | 1.025 | 2.075 | 3.353 | 4.780 | 6.306 | 7.897 | 9.533 | 11.197 | 12.878 | 14.569 |
| 17 | 0.383 | 1.111 | 2.221 | 3.559 | 5.046 | 6.631 | 8.280 | 9.972 | 11.691 | 13.426 | 15.169 |
| 196 | 2.362 | 3.758 | 5.303 | 6.944 | 8.649 | 10.395 | 12.166 | 13.952 | 15.745 |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.418 | 1.279 | 2.499 | 3.951 | 5.551 | 7.246 | 9.004 | 10.801 | 12.623 | 14.458 | 16.297 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.452 | 1.360 | 2.632 | 4.137 | 5.790 | 7.538 | 9.346 | 11.193 | 13.063 | 14.944 | 16.828 |
| 20 | 0.486 | 1.439 | 2.762 | 4.318 | 6.022 | 7.820 | 9.677 | 11.572 | 13.487 | 15.413 | 17.340 |
| 21 | 0.520 | 1.517 | 2.888 | 4.494 | 6.247 | 8.092 | 9.997 | 11.937 | 13.897 | 15.866 | 17.833 |
| 22 | 0.553 | 1.592 | 3.010 | 4.664 | 6.464 | 8.357 | 10.307 | 12.291 | 14.294 | 16.303 | 18.310 |
| 23 | 0.585 | 1.666 | 3.129 | 4.829 | 6.675 | 8.613 | 10.606 | 12.633 | 14.677 | 16.726 | 18.770 |
| 24 | 0.617 | 1.737 | 3.245 | 4.990 | 6.880 | 8.861 | 10.897 | 12.965 | 15.049 | 17.136 | 19.215 |
| 25 | 0.648 | 1.807 | 3.357 | 5.146 | 7.079 | 9.102 | 11.179 | 13.287 | 15.409 | 17.532 | 19.647 |
| 26 | 0.678 | 1.875 | 3.467 | 5.297 | 7.273 | 9.337 | 11.453 | 13.599 | 15.758 | 17.917 | 20.065 |
| 27 | 0.708 | 1.942 | 3.574 | 5.445 | 7.461 | 9.564 | 11.720 | 13.903 | 16.098 | 18.290 | 20.470 |
| 28 | 0.737 | 2.007 | 3.678 | 5.589 | 7.644 | 9.786 | 11.979 | 14.198 | 16.427 | 18.653 | 20.864 |
| 29 | 0.766 | 2.070 | 3.779 | 5.729 | 7.822 | 10.002 | 12.231 | 14.485 | 16.748 | 19.005 | 21.246 |
| 30 | 0.794 | 2.132 | 3.878 | 5.865 | 7.996 | 10.212 | 12.476 | 14.764 | 17.060 | 19.347 | 21.618 |

Table B. 23
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 75 /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.019 | 0.048 | 0.100 | 0.178 | 0.284 | 0.418 |
| 2 | 0.000 | 0.000 | 0.005 | 0.029 | 0.088 | 0.197 | 0.361 | 0.580 | 0.850 | 1.166 | 1.522 |
| 3 | 0.000 | 0.004 | 0.031 | 0.113 | 0.270 | 0.510 | 0.826 | 1.211 | 1.655 | 2.149 | 2.685 |
| 4 | 0.001 | 0.015 | 0.083 | 0.244 | 0.512 | 0.881 | 1.338 | 1.870 | 2.463 | 3.106 | 3.789 |
| 5 | 0.003 | 0.035 | 0.157 | 0.405 | 0.782 | 1.273 | 1.857 | 2.518 | 3.240 | 4.010 | 4.820 |
| 6 | 0.006 | 0.065 | 0.247 | 0.584 | 1.065 | 1.668 | 2.367 | 3.143 | 3.978 | 4.861 | 5.780 |
| 7 | 0.012 | 0.101 | 0.348 | 0.772 | 1.352 | 2.057 | 2.861 | 3.740 | 4.678 | 5.660 | 6.678 |
| 8 | 0.019 | 0.144 | 0.457 | 0.965 | 1.637 | 2.437 | 3.336 | 4.310 | 5.340 | 6.414 | 7.521 |
| 9 | 0.029 | 0.192 | 0.571 | 1.159 | 1.917 | 2.806 | 3.793 | 4.854 | 5.969 | 7.126 | 8.314 |
| 10 | 0.040 | 0.244 | 0.687 | 1.352 | 2.192 | 3.164 | 4.232 | 5.373 | 6.567 | 7.801 | 9.064 |
| 11 | 0.053 | 0.298 | 0.805 | 1.543 | 2.460 | 3.509 | 4.654 | 5.870 | 7.137 | 8.443 | 9.776 |
| 12 | 0.068 | 0.355 | 0.923 | 1.731 | 2.721 | 3.842 | 5.059 | 6.346 | 7.682 | 9.054 | 10.452 |
| 13 | 0.083 | 0.413 | 1.040 | 1.916 | 2.974 | 4.165 | 5.449 | 6.802 | 8.203 | 9.638 | 11.097 |
| 14 | 0.100 | 0.472 | 1.157 | 2.096 | 3.220 | 4.476 | 5.825 | 7.240 | 8.702 | 10.197 | 11.713 |
| 15 | 0.118 | 0.531 | 1.272 | 2.273 | 3.460 | 4.777 | 6.187 | 7.662 | 9.182 | 10.732 | 12.303 |
| 16 | 0.136 | 0.591 | 1.386 | 2.445 | 3.692 | 5.069 | 6.537 | 8.068 | 9.643 | 11.247 | 12.869 |
| 17 | 0.155 | 0.650 | 1.498 | 2.614 | 3.918 | 5.351 | 6.875 | 8.460 | 10.087 | 11.741 | 13.413 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.174 | 0.709 | 1.608 | 2.778 | 4.137 | 5.625 | 7.201 | 8.838 | 10.515 | 12.218 | 13.936 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.194 | 0.768 | 1.716 | 2.939 | 4.350 | 5.890 | 7.517 | 9.203 | 10.928 | 12.678 | 14.440 |
| 20 | 0.214 | 0.826 | 1.822 | 3.095 | 4.557 | 6.147 | 7.823 | 9.557 | 11.328 | 13.121 | 14.927 |
| 21 | 0.234 | 0.884 | 1.926 | 3.247 | 4.759 | 6.397 | 8.120 | 9.899 | 11.714 | 13.550 | 15.396 |
| 22 | 0.254 | 0.941 | 2.027 | 3.396 | 4.955 | 6.640 | 8.408 | 10.231 | 12.089 | 13.965 | 15.850 |
| 23 | 0.274 | 0.997 | 2.127 | 3.542 | 5.146 | 6.876 | 8.688 | 10.553 | 12.451 | 14.367 | 16.290 |
| 24 | 0.294 | 1.052 | 2.224 | 3.683 | 5.332 | 7.105 | 8.959 | 10.866 | 12.803 | 14.757 | 16.715 |
| 25 | 0.314 | 1.107 | 2.320 | 3.822 | 5.513 | 7.328 | 9.224 | 11.169 | 13.145 | 15.135 | 17.128 |
| 26 | 0.334 | 1.160 | 2.413 | 3.957 | 5.690 | 7.546 | 9.481 | 11.465 | 13.477 | 15.502 | 17.528 |
| 27 | 0.354 | 1.213 | 2.505 | 4.089 | 5.862 | 7.758 | 9.731 | 11.752 | 13.799 | 15.858 | 17.916 |
| 28 | 0.374 | 1.264 | 2.594 | 4.218 | 6.030 | 7.964 | 9.974 | 12.031 | 14.113 | 16.205 | 18.293 |
| 29 | 0.393 | 1.315 | 2.682 | 4.343 | 6.194 | 8.165 | 10.212 | 12.303 | 14.419 | 16.542 | 18.660 |
| 20 | 0.412 | 1.365 | 2.768 | 4.467 | 6.354 | 8.362 | 10.443 | 12.569 | 14.716 | 16.870 | 19.016 |

Table B. 24
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 7 0} /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.009 | 0.024 | 0.053 | 0.098 | 0.163 |
| 2 | 0.000 | 0.000 | 0.001 | 0.005 | 0.021 | 0.061 | 0.136 | 0.252 | 0.410 | 0.612 | 0.855 |
| 3 | 0.000 | 0.001 | 0.006 | 0.030 | 0.094 | 0.215 | 0.399 | 0.646 | 0.953 | 1.315 | 1.723 |
| 4 | 0.000 | 0.003 | 0.021 | 0.084 | 0.218 | 0.436 | 0.736 | 1.113 | 1.558 | 2.060 | 2.613 |
| 5 | 0.000 | 0.007 | 0.048 | 0.163 | 0.377 | 0.695 | 1.108 | 1.605 | 2.173 | 2.801 | 3.478 |
| 6 | 0.001 | 0.016 | 0.087 | 0.263 | 0.560 | 0.975 | 1.494 | 2.101 | 2.780 | 3.519 | 4.305 |
| 7 | 0.002 | 0.028 | 0.137 | 0.376 | 0.756 | 1.264 | 1.882 | 2.590 | 3.370 | 4.208 | 5.093 |
| 8 | 0.004 | 0.045 | 0.196 | 0.500 | 0.960 | 1.557 | 2.267 | 3.067 | 3.939 | 4.868 | 5.842 |
| 9 | 0.006 | 0.066 | 0.261 | 0.631 | 1.169 | 1.849 | 2.645 | 3.531 | 4.488 | 5.500 | 6.555 |
| 10 | 0.010 | 0.090 | 0.331 | 0.766 | 1.378 | 2.138 | 3.013 | 3.979 | 5.015 | 6.104 | 7.235 |
| 11 | 0.014 | 0.117 | 0.406 | 0.904 | 1.588 | 2.422 | 3.373 | 4.413 | 5.522 | 6.683 | 7.883 |
| 12 | 0.019 | 0.147 | 0.483 | 1.043 | 1.795 | 2.700 | 3.722 | 4.833 | 6.010 | 7.238 | 8.504 |
| 13 | 0.024 | 0.179 | 0.562 | 1.182 | 2.000 | 2.972 | 4.061 | 5.238 | 6.480 | 7.771 | 9.098 |
| 14 | 0.031 | 0.213 | 0.643 | 1.321 | 2.202 | 3.238 | 4.391 | 5.630 | 6.933 | 8.284 | 9.667 |
| 15 | 0.038 | 0.248 | 0.725 | 1.459 | 2.400 | 3.498 | 4.711 | 6.010 | 7.371 | 8.777 | 10.215 |
| 16 | 0.046 | 0.284 | 0.807 | 1.596 | 2.595 | 3.751 | 5.022 | 6.377 | 7.793 | 9.252 | 10.742 |
| 17 | 0.055 | 0.321 | 0.889 | 1.731 | 2.785 | 3.997 | 5.324 | 6.733 | 8.201 | 9.711 | 11.249 |


| 18 | 0.064 | 0.359 | 0.971 | 1.864 | 2.972 | 4.238 | 5.617 | 7.078 | 8.596 | 10.154 | 11.739 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.073 | 0.398 | 1.053 | 1.995 | 3.155 | 4.472 | 5.902 | 7.412 | 8.978 | 10.582 | 12.211 |
| 20 | 0.083 | 0.437 | 1.134 | 2.125 | 3.334 | 4.701 | 6.180 | 7.737 | 9.348 | 10.997 | 12.668 |
| 21 | 0.093 | 0.476 | 1.215 | 2.252 | 3.509 | 4.924 | 6.449 | 8.052 | 9.708 | 11.398 | 13.110 |
| 22 | 0.104 | 0.515 | 1.294 | 2.376 | 3.681 | 5.141 | 6.712 | 8.359 | 10.056 | 11.787 | 13.538 |
| 23 | 0.115 | 0.554 | 1.373 | 2.499 | 3.848 | 5.354 | 6.968 | 8.656 | 10.395 | 12.165 | 13.953 |
| 24 | 0.126 | 0.594 | 1.451 | 2.619 | 4.012 | 5.561 | 7.217 | 8.946 | 10.724 | 12.531 | 14.355 |
| 25 | 0.137 | 0.633 | 1.528 | 2.738 | 4.172 | 5.763 | 7.460 | 9.229 | 11.044 | 12.887 | 14.745 |
| 26 | 0.149 | 0.671 | 1.603 | 2.854 | 4.329 | 5.960 | 7.697 | 9.504 | 11.355 | 13.234 | 15.125 |
| 27 | 0.160 | 0.710 | 1.678 | 2.967 | 4.483 | 6.153 | 7.928 | 9.771 | 11.658 | 13.570 | 15.493 |
| 28 | 0.172 | 0.748 | 1.751 | 3.079 | 4.633 | 6.342 | 8.153 | 10.033 | 11.954 | 13.898 | 15.851 |
| 29 | 0.183 | 0.786 | 1.823 | 3.188 | 4.781 | 6.526 | 8.374 | 10.287 | 12.241 | 14.217 | 16.200 |
| 20 | 0.195 | 0.824 | 1.895 | 3.296 | 4.925 | 6.706 | 8.589 | 10.536 | 12.522 | 14.528 | 16.539 |

Table B. 25
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 6 5} /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.012 | 0.027 | 0.052 |
| 2 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.015 | 0.042 | 0.093 | 0.173 | 0.286 | 0.434 |
| 3 | 0.000 | 0.000 | 0.001 | 0.006 | 0.027 | 0.077 | 0.168 | 0.309 | 0.500 | 0.742 | 1.032 |
| 4 | 0.000 | 0.000 | 0.004 | 0.024 | 0.079 | 0.190 | 0.365 | 0.608 | 0.916 | 1.284 | 1.706 |
| 5 | 0.000 | 0.001 | 0.012 | 0.056 | 0.160 | 0.342 | 0.607 | 0.954 | 1.373 | 1.857 | 2.398 |
| 6 | 0.000 | 0.003 | 0.026 | 0.102 | 0.263 | 0.522 | 0.877 | 1.322 | 1.846 | 2.436 | 3.083 |
| 7 | 0.000 | 0.007 | 0.046 | 0.162 | 0.384 | 0.719 | 1.163 | 1.701 | 2.320 | 3.008 | 3.752 |
| 8 | 0.001 | 0.012 | 0.072 | 0.232 | 0.517 | 0.929 | 1.456 | 2.082 | 2.790 | 3.566 | 4.398 |
| 9 | 0.001 | 0.019 | 0.104 | 0.310 | 0.659 | 1.145 | 1.752 | 2.460 | 3.251 | 4.109 | 5.022 |
| 10 | 0.002 | 0.029 | 0.141 | 0.396 | 0.807 | 1.365 | 2.047 | 2.832 | 3.701 | 4.635 | 5.623 |
| 11 | 0.003 | 0.040 | 0.183 | 0.486 | 0.959 | 1.586 | 2.340 | 3.198 | 4.139 | 5.144 | 6.201 |
| 12 | 0.005 | 0.053 | 0.228 | 0.581 | 1.114 | 1.807 | 2.629 | 3.556 | 4.564 | 5.637 | 6.758 |
| 13 | 0.006 | 0.068 | 0.276 | 0.678 | 1.270 | 2.026 | 2.914 | 3.905 | 4.978 | 6.113 | 7.295 |
| 14 | 0.008 | 0.085 | 0.326 | 0.777 | 1.427 | 2.243 | 3.193 | 4.246 | 5.379 | 6.573 | 7.813 |
| 15 | 0.011 | 0.103 | 0.379 | 0.878 | 1.583 | 2.458 | 3.467 | 4.578 | 5.769 | 7.019 | 8.313 |
| 17 | 0.014 | 0.122 | 0.433 | 0.979 | 1.738 | 2.669 | 3.735 | 4.902 | 6.147 | 7.450 | 8.795 |
| 17 | 0.017 | 0.143 | 0.488 | 1.081 | 1.892 | 2.877 | 3.997 | 5.218 | 6.515 | 7.868 | 9.262 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.020 | 0.164 | 0.545 | 1.183 | 2.044 | 3.081 | 4.253 | 5.525 | 6.872 | 8.273 | 9.713 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.024 | 0.187 | 0.602 | 1.284 | 2.194 | 3.282 | 4.503 | 5.825 | 7.219 | 8.666 | 10.150 |
| 20 | 0.028 | 0.210 | 0.659 | 1.385 | 2.343 | 3.479 | 4.748 | 6.116 | 7.556 | 9.047 | 10.573 |
| 21 | 0.033 | 0.234 | 0.718 | 1.486 | 2.489 | 3.672 | 4.988 | 6.401 | 7.884 | 9.417 | 10.984 |
| 22 | 0.038 | 0.258 | 0.776 | 1.586 | 2.633 | 3.861 | 5.222 | 6.679 | 8.204 | 9.777 | 11.382 |
| 23 | 0.043 | 0.283 | 0.834 | 1.684 | 2.775 | 4.047 | 5.451 | 6.949 | 8.515 | 10.127 | 11.769 |
| 24 | 0.048 | 0.308 | 0.892 | 1.782 | 2.915 | 4.229 | 5.674 | 7.213 | 8.818 | 10.467 | 12.145 |
| 25 | 0.053 | 0.334 | 0.950 | 1.878 | 3.052 | 4.407 | 5.893 | 7.471 | 9.113 | 10.798 | 12.510 |
| 26 | 0.059 | 0.360 | 1.008 | 1.974 | 3.187 | 4.582 | 6.107 | 7.723 | 9.401 | 11.121 | 12.865 |
| 27 | 0.065 | 0.385 | 1.065 | 2.068 | 3.320 | 4.754 | 6.316 | 7.969 | 9.682 | 11.435 | 13.211 |
| 28 | 0.071 | 0.411 | 1.122 | 2.161 | 3.451 | 4.922 | 6.521 | 8.209 | 9.956 | 11.741 | 13.548 |
| 29 | 0.077 | 0.438 | 1.178 | 2.252 | 3.579 | 5.087 | 6.721 | 8.444 | 10.224 | 12.040 | 13.876 |
| 30 | 0.083 | 0.464 | 1.234 | 2.343 | 3.705 | 5.248 | 6.918 | 8.673 | 10.485 | 12.331 | 14.195 |

Table B. 26
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 6 0} /$ Dividend Rate $=\mathbf{1 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.002 | 0.006 | 0.013 |
| 2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.003 | 0.010 | 0.028 | 0.062 | 0.116 | 0.195 |
| 3 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.023 | 0.060 | 0.129 | 0.234 | 0.380 | 0.567 |
| 4 | 0.000 | 0.000 | 0.001 | 0.005 | 0.024 | 0.071 | 0.160 | 0.299 | 0.493 | 0.742 | 1.042 |
| 5 | 0.000 | 0.000 | 0.003 | 0.016 | 0.058 | 0.148 | 0.300 | 0.520 | 0.806 | 1.157 | 1.565 |
| 6 | 0.000 | 0.001 | 0.007 | 0.034 | 0.108 | 0.251 | 0.472 | 0.773 | 1.151 | 1.598 | 2.106 |
| 7 | 0.000 | 0.002 | 0.013 | 0.060 | 0.173 | 0.373 | 0.665 | 1.048 | 1.512 | 2.050 | 2.650 |
| 8 | 0.000 | 0.003 | 0.023 | 0.094 | 0.251 | 0.510 | 0.873 | 1.334 | 1.881 | 2.503 | 3.188 |
| 9 | 0.000 | 0.005 | 0.036 | 0.136 | 0.338 | 0.657 | 1.090 | 1.626 | 2.252 | 2.953 | 3.717 |
| 10 | 0.001 | 0.008 | 0.053 | 0.183 | 0.434 | 0.813 | 1.314 | 1.922 | 2.620 | 3.395 | 4.233 |
| 11 | 0.001 | 0.012 | 0.072 | 0.236 | 0.536 | 0.974 | 1.540 | 2.217 | 2.985 | 3.829 | 4.735 |
| 12 | 0.001 | 0.017 | 0.095 | 0.294 | 0.643 | 1.139 | 1.768 | 2.510 | 3.344 | 4.253 | 5.223 |
| 13 | 0.002 | 0.023 | 0.121 | 0.356 | 0.753 | 1.307 | 1.996 | 2.800 | 3.697 | 4.667 | 5.697 |
| 14 | 0.002 | 0.030 | 0.148 | 0.421 | 0.867 | 1.475 | 2.223 | 3.066 | 4.042 | 5.071 | 6.157 |
| 15 | 0.003 | 0.038 | 0.179 | 0.488 | 0.982 | 1.644 | 2.448 | 3.368 | 4.380 | 5.464 | 6.604 |
| 16 | 0.004 | 0.046 | 0.211 | 0.558 | 1.098 | 1.812 | 2.671 | 3.645 | 4.710 | 5.847 | 7.038 |
| 17 | 0.005 | 0.056 | 0.244 | 0.629 | 1.216 | 1.980 | 2.890 | 3.916 | 5.033 | 6.219 | 7.459 |


| 18 | 0.006 | 0.067 | 0.280 | 0.702 | 1.333 | 2.146 | 3.107 | 4.183 | 5.349 | 6.582 | 7.868 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.007 | 0.078 | 0.316 | 0.775 | 1.451 | 2.311 | 3.320 | 4.444 | 5.657 | 6.936 | 8.265 |
| 20 | 0.009 | 0.091 | 0.353 | 0.849 | 1.568 | 2.474 | 3.530 | 4.700 | 5.958 | 7.280 | 8.651 |
| 21 | 0.010 | 0.103 | 0.392 | 0.924 | 1.685 | 2.636 | 3.736 | 4.951 | 6.251 | 7.616 | 9.027 |
| 22 | 0.012 | 0.117 | 0.431 | 0.999 | 1.801 | 2.795 | 3.939 | 5.196 | 6.538 | 7.943 | 9.392 |
| 23 | 0.014 | 0.131 | 0.471 | 1.074 | 1.916 | 2.952 | 4.138 | 5.437 | 6.819 | 8.262 | 9.747 |
| 24 | 0.016 | 0.146 | 0.511 | 1.149 | 2.030 | 3.107 | 4.333 | 5.672 | 7.093 | 8.573 | 10.094 |
| 25 | 0.019 | 0.160 | 0.552 | 1.224 | 2.143 | 3.260 | 4.525 | 5.903 | 7.361 | 8.876 | 10.431 |
| 26 | 0.021 | 0.176 | 0.593 | 1.298 | 2.255 | 3.410 | 4.714 | 6.128 | 7.622 | 9.172 | 10.760 |
| 27 | 0.024 | 0.192 | 0.634 | 1.373 | 2.366 | 3.558 | 4.899 | 6.350 | 7.878 | 9.461 | 11.080 |
| 28 | 0.026 | 0.208 | 0.675 | 1.446 | 2.475 | 3.704 | 5.081 | 6.566 | 8.129 | 9.744 | 11.392 |
| 29 | 0.029 | 0.224 | 0.716 | 1.519 | 2.583 | 3.847 | 5.259 | 6.779 | 8.373 | 10.019 | 11.697 |
| 30 | 0.032 | 0.241 | 0.758 | 1.592 | 2.689 | 3.988 | 5.434 | 6.987 | 8.613 | 10.289 | 11.995 |

## Table B. 27

American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 120 / \text { Dividend Rate }=2 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 20.000 | 20.000 | 20.000 | 20.000 | 20.002 | 20.083 | 20.255 | 20.496 | 20.790 | 21.127 | 21.501 |
| 2 | 20.000 | 20.000 | 20.000 | 20.036 | 20.276 | 20.664 | 21.150 | 21.707 | 22.318 | 22.969 | 23.652 |
| 3 | 20.000 | 20.000 | 20.002 | 20.242 | 20.731 | 21.366 | 22.095 | 22.891 | 23.734 | 24.613 | 25.520 |
| 4 | 20.000 | 20.000 | 20.066 | 20.523 | 21.222 | 22.060 | 22.988 | 23.976 | 25.007 | 26.070 | 27.156 |
| 5 | 20.000 | 20.000 | 20.184 | 20.829 | 21.709 | 22.721 | 23.817 | 24.969 | 26.159 | 27.377 | 28.616 |
| 6 | 20.000 | 20.000 | 20.328 | 21.140 | 22.178 | 23.343 | 24.587 | 25.882 | 27.212 | 28.566 | 29.938 |
| 7 | 20.000 | 20.001 | 20.486 | 21.447 | 22.628 | 23.929 | 25.305 | 26.728 | 28.183 | 29.659 | 31.150 |
| 8 | 20.000 | 20.017 | 20.650 | 21.747 | 23.056 | 24.482 | 25.977 | 27.516 | 29.085 | 30.672 | 32.271 |
| 9 | 20.000 | 20.048 | 20.816 | 22.037 | 23.465 | 25.004 | 26.609 | 28.255 | 29.928 | 31.617 | 33.315 |
| 10 | 20.000 | 20.089 | 20.981 | 22.317 | 23.854 | 25.499 | 27.206 | 28.951 | 30.720 | 32.503 | 34.292 |
| 11 | 20.000 | 20.137 | 21.144 | 22.587 | 24.226 | 25.969 | 27.771 | 29.609 | 31.468 | 33.338 | 35.212 |
| 12 | 20.000 | 20.189 | 21.304 | 22.848 | 24.582 | 26.417 | 28.308 | 30.233 | 32.176 | 34.128 | 36.081 |
| 13 | 20.000 | 20.245 | 21.461 | 23.099 | 24.923 | 26.845 | 28.820 | 30.827 | 32.849 | 34.877 | 36.904 |
| 14 | 20.000 | 20.303 | 21.614 | 23.341 | 25.250 | 27.254 | 29.309 | 31.393 | 33.490 | 35.590 | 37.688 |
| 15 | 20.000 | 20.362 | 21.763 | 23.574 | 25.565 | 27.646 | 29.777 | 31.934 | 34.101 | 36.270 | 38.434 |
| 16 | 20.000 | 20.422 | 21.909 | 23.800 | 25.867 | 28.023 | 30.226 | 32.452 | 34.687 | 36.921 | 39.148 |
| 17 | 20.000 | 20.482 | 22.050 | 24.018 | 26.159 | 28.386 | 30.657 | 32.949 | 35.248 | 37.544 | 39.831 |


| 18 | 20.000 | 20.542 | 22.188 | 24.229 | 26.440 | 28.735 | 31.072 | 33.427 | 35.787 | 38.143 | 40.487 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 20.000 | 20.602 | 22.322 | 24.433 | 26.712 | 29.072 | 31.472 | 33.887 | 36.306 | 38.718 | 41.116 |
| 20 | 20.000 | 20.662 | 22.452 | 24.630 | 26.974 | 29.397 | 31.857 | 34.331 | 36.806 | 39.272 | 41.722 |
| 21 | 20.000 | 20.720 | 22.579 | 24.822 | 27.228 | 29.711 | 32.229 | 34.759 | 37.288 | 39.806 | 42.306 |
| 22 | 20.000 | 20.779 | 22.702 | 25.008 | 27.474 | 30.015 | 32.588 | 35.173 | 37.753 | 40.322 | 42.870 |
| 23 | 20.000 | 20.836 | 22.823 | 25.189 | 27.713 | 30.309 | 32.936 | 35.573 | 38.204 | 40.820 | 43.414 |
| 24 | 20.000 | 20.892 | 22.940 | 25.364 | 27.944 | 30.594 | 33.274 | 35.960 | 38.639 | 41.302 | 43.939 |
| 25 | 20.000 | 20.948 | 23.054 | 25.534 | 28.169 | 30.871 | 33.600 | 36.335 | 39.061 | 41.768 | 44.448 |
| 26 | 20.000 | 21.002 | 23.165 | 25.700 | 28.386 | 31.139 | 33.918 | 36.700 | 39.470 | 42.220 | 44.941 |
| 27 | 20.000 | 21.056 | 23.274 | 25.861 | 28.598 | 31.400 | 34.226 | 37.053 | 39.867 | 42.658 | 45.419 |
| 28 | 20.000 | 21.109 | 23.380 | 26.018 | 28.804 | 31.653 | 34.525 | 37.396 | 40.253 | 43.084 | 45.882 |
| 29 | 20.000 | 21.161 | 23.483 | 26.171 | 29.005 | 31.900 | 34.816 | 37.730 | 40.627 | 43.497 | 46.332 |
| 30 | 20.000 | 21.212 | 23.584 | 26.320 | 29.200 | 32.140 | 35.099 | 38.055 | 40.991 | 43.899 | 46.768 |

Table B. 28
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 115 /$ Dividend Rate $=\mathbf{2 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 15.000 | 15.000 | 15.000 | 15.025 | 15.175 | 15.419 | 15.729 | 16.090 | 16.490 | 16.921 | 17.376 |
| 2 | 15.000 | 15.000 | 15.059 | 15.368 | 15.830 | 16.388 | 17.009 | 17.675 | 18.376 | 19.101 | 19.846 |
| 3 | 15.000 | 15.000 | 15.266 | 15.822 | 16.525 | 17.316 | 18.164 | 19.053 | 19.969 | 20.907 | 21.860 |
| 4 | 15.000 | 15.040 | 15.521 | 16.280 | 17.179 | 18.159 | 19.191 | 20.258 | 21.350 | 22.459 | 23.581 |
| 5 | 15.000 | 15.121 | 15.787 | 16.721 | 17.786 | 18.927 | 20.115 | 21.334 | 22.575 | 23.830 | 25.095 |
| 6 | 15.000 | 15.223 | 16.051 | 17.137 | 18.348 | 19.630 | 20.955 | 22.308 | 23.680 | 25.064 | 26.455 |
| 7 | 15.000 | 15.335 | 16.308 | 17.530 | 18.872 | 20.280 | 21.728 | 23.201 | 24.691 | 26.190 | 27.694 |
| 8 | 15.000 | 15.451 | 16.556 | 17.901 | 19.361 | 20.884 | 22.445 | 24.027 | 25.624 | 27.228 | 28.834 |
| 9 | 15.000 | 15.569 | 16.793 | 18.252 | 19.821 | 21.450 | 23.113 | 24.797 | 26.492 | 28.192 | 29.892 |
| 10 | 15.000 | 15.686 | 17.021 | 18.585 | 20.255 | 21.982 | 23.741 | 25.518 | 27.304 | 29.093 | 30.880 |
| 11 | 15.002 | 15.801 | 17.239 | 18.900 | 20.665 | 22.484 | 24.332 | 26.197 | 28.068 | 29.940 | 31.808 |
| 12 | 15.009 | 15.914 | 17.448 | 19.201 | 21.055 | 22.960 | 24.892 | 26.838 | 28.789 | 30.739 | 32.683 |
| 17 | 15.020 | 16.024 | 17.649 | 19.488 | 21.426 | 23.412 | 25.424 | 27.447 | 29.473 | 31.496 | 33.511 |
| 14 | 15.035 | 16.131 | 17.841 | 19.763 | 21.779 | 23.843 | 25.930 | 28.026 | 30.123 | 32.215 | 34.298 |
| 15 | 15.052 | 16.236 | 18.027 | 20.026 | 22.118 | 24.255 | 26.413 | 28.578 | 30.743 | 32.901 | 35.048 |
| 16 | 15.071 | 16.337 | 18.205 | 20.278 | 22.442 | 24.649 | 26.875 | 29.106 | 31.335 | 33.556 | 35.763 |
| 17 | 15.091 | 16.436 | 18.377 | 20.521 | 22.754 | 25.027 | 27.318 | 29.613 | 31.903 | 34.183 | 36.448 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 15.112 | 16.531 | 18.543 | 20.755 | 23.053 | 25.391 | 27.743 | 30.098 | 32.447 | 34.784 | 37.104 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 15.134 | 16.624 | 18.703 | 20.980 | 23.342 | 25.740 | 28.152 | 30.565 | 32.971 | 35.362 | 37.734 |
| 20 | 15.157 | 16.714 | 18.857 | 21.197 | 23.619 | 26.077 | 28.546 | 31.015 | 33.475 | 35.918 | 38.340 |
| 21 | 15.179 | 16.802 | 19.007 | 21.407 | 23.887 | 26.401 | 28.927 | 31.449 | 33.960 | 36.453 | 38.924 |
| 22 | 15.202 | 16.887 | 19.152 | 21.610 | 24.146 | 26.715 | 29.294 | 31.868 | 34.429 | 36.970 | 39.487 |
| 23 | 15.225 | 16.970 | 19.292 | 21.806 | 24.397 | 27.019 | 29.649 | 32.273 | 34.882 | 37.469 | 40.030 |
| 24 | 15.248 | 17.050 | 19.428 | 21.996 | 24.639 | 27.313 | 29.992 | 32.664 | 35.320 | 37.952 | 40.555 |
| 25 | 15.271 | 17.128 | 19.560 | 22.180 | 24.874 | 27.597 | 30.325 | 33.044 | 35.744 | 38.419 | 41.063 |
| 26 | 15.293 | 17.205 | 19.688 | 22.358 | 25.102 | 27.873 | 30.648 | 33.412 | 36.155 | 38.871 | 41.555 |
| 27 | 15.316 | 17.279 | 19.812 | 22.531 | 25.323 | 28.141 | 30.961 | 33.769 | 36.554 | 39.310 | 42.031 |
| 28 | 15.338 | 17.351 | 19.933 | 22.700 | 25.538 | 28.401 | 31.265 | 34.115 | 36.941 | 39.736 | 42.493 |
| 29 | 15.360 | 17.421 | 20.050 | 22.863 | 25.747 | 28.654 | 31.561 | 34.452 | 37.317 | 40.149 | 42.941 |

Table B. 29
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 110 / \text { Dividend Rate }=\mathbf{2 \%}
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 10.000 | 10.000 | 10.117 | 10.382 | 10.731 | 11.137 | 11.582 | 12.055 | 12.550 | 13.061 | 13.585 |
| 2 | 10.000 | 10.131 | 10.564 | 11.137 | 11.789 | 12.488 | 13.219 | 13.972 | 14.740 | 15.521 | 16.310 |
| 3 | 10.001 | 10.359 | 11.029 | 11.830 | 12.700 | 13.611 | 14.549 | 15.504 | 16.472 | 17.449 | 18.432 |
| 4 | 10.034 | 10.600 | 11.463 | 12.447 | 13.493 | 14.576 | 15.682 | 16.802 | 17.933 | 19.070 | 20.211 |
| 5 | 10.093 | 10.836 | 11.862 | 13.002 | 14.199 | 15.428 | 16.678 | 17.940 | 19.210 | 20.484 | 21.761 |
| 6 | 10.165 | 11.061 | 12.230 | 13.506 | 14.835 | 16.195 | 17.571 | 18.959 | 20.352 | 21.748 | 23.143 |
| 7 | 10.241 | 11.274 | 12.570 | 13.969 | 15.418 | 16.894 | 18.385 | 19.885 | 21.389 | 22.893 | 24.396 |
| 8 | 10.320 | 11.475 | 12.887 | 14.397 | 15.955 | 17.538 | 19.134 | 20.737 | 22.341 | 23.945 | 25.545 |
| 9 | 10.398 | 11.665 | 13.183 | 14.797 | 16.455 | 18.136 | 19.829 | 21.526 | 23.224 | 24.919 | 26.609 |
| 10 | 10.474 | 11.845 | 13.462 | 15.171 | 16.922 | 18.695 | 20.478 | 22.263 | 24.047 | 25.827 | 27.601 |
| 11 | 10.549 | 12.016 | 13.724 | 15.523 | 17.362 | 19.220 | 21.087 | 22.955 | 24.820 | 26.679 | 28.531 |
| 12 | 10.622 | 12.178 | 13.973 | 15.855 | 17.777 | 19.716 | 21.661 | 23.607 | 25.548 | 27.482 | 29.407 |
| 12 | 10.692 | 12.333 | 14.209 | 16.171 | 18.170 | 20.185 | 22.206 | 24.225 | 26.238 | 28.242 | 30.235 |
| 13 | 10.889 | 12.756 | 14.852 | 17.029 | 19.240 | 21.462 | 23.686 | 25.904 | 28.112 | 30.306 | 32.484 |
| 14 | 10.760 | 12.480 | 14.433 | 16.471 | 18.544 | 20.631 | 22.723 | 24.811 | 26.893 | 28.964 | 31.021 |
| 15 | 10.826 | 12.621 | 14.647 | 16.756 | 18.900 | 21.056 | 23.215 | 25.370 | 27.517 | 29.651 | 31.770 |
| 17 | 10.950 | 12.885 | 15.048 | 17.290 | 19.565 | 21.851 | 24.136 | 26.415 | 28.682 | 30.934 | 33.166 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 11.009 | 13.009 | 15.236 | 17.541 | 19.877 | 22.223 | 24.569 | 26.905 | 29.229 | 31.535 | 33.821 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 11.067 | 13.128 | 15.416 | 17.781 | 20.177 | 22.582 | 24.984 | 27.376 | 29.754 | 32.112 | 34.449 |
| 20 | 11.122 | 13.243 | 15.589 | 18.013 | 20.466 | 22.926 | 25.383 | 27.829 | 30.259 | 32.667 | 35.052 |
| 21 | 11.175 | 13.353 | 15.756 | 18.236 | 20.744 | 23.259 | 25.769 | 28.266 | 30.745 | 33.202 | 35.633 |
| 22 | 11.227 | 13.460 | 15.917 | 18.451 | 21.012 | 23.579 | 26.140 | 28.687 | 31.215 | 33.718 | 36.193 |
| 23 | 11.277 | 13.562 | 16.072 | 18.658 | 21.271 | 23.889 | 26.500 | 29.095 | 31.668 | 34.216 | 36.734 |
| 24 | 11.325 | 13.661 | 16.222 | 18.859 | 21.522 | 24.189 | 26.847 | 29.488 | 32.107 | 34.697 | 37.256 |
| 25 | 11.371 | 13.757 | 16.367 | 19.053 | 21.765 | 24.479 | 27.184 | 29.870 | 32.531 | 35.163 | 37.762 |
| 26 | 11.416 | 13.849 | 16.508 | 19.241 | 22.000 | 24.760 | 27.510 | 30.239 | 32.942 | 35.614 | 38.251 |
| 27 | 11.460 | 13.938 | 16.644 | 19.424 | 22.228 | 25.033 | 27.826 | 30.597 | 33.341 | 36.051 | 38.724 |
| 28 | 11.501 | 14.025 | 16.775 | 19.601 | 22.449 | 25.298 | 28.133 | 30.945 | 33.727 | 36.475 | 39.183 |
| 29 | 11.542 | 14.109 | 16.903 | 19.772 | 22.664 | 25.555 | 28.431 | 31.283 | 34.103 | 36.887 | 39.629 |
| 29 | 11.581 | 14.190 | 17.027 | 19.939 | 22.873 | 25.805 | 28.721 | 31.611 | 34.468 | 37.287 | 40.062 |

Table B. 30
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 105 /$ Dividend Rate $=\mathbf{2 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 5.098 | 5.439 | 5.879 | 6.367 | 6.883 | 7.416 | 7.961 | 8.514 | 9.073 | 9.637 | 10.203 |
| 2 | 5.375 | 6.012 | 6.732 | 7.489 | 8.267 | 9.057 | 9.855 | 10.659 | 11.465 | 12.275 | 13.085 |
| 3 | 5.640 | 6.488 | 7.410 | 8.363 | 9.334 | 10.314 | 11.299 | 12.289 | 13.280 | 14.272 | 15.264 |
| 4 | 5.875 | 6.894 | 7.980 | 9.094 | 10.222 | 11.358 | 12.499 | 13.641 | 14.784 | 15.927 | 17.068 |
| 5 | 6.086 | 7.250 | 8.476 | 9.728 | 10.993 | 12.264 | 13.538 | 14.813 | 16.086 | 17.358 | 18.628 |
| 6 | 6.276 | 7.567 | 8.918 | 10.292 | 11.678 | 13.069 | 14.462 | 15.853 | 17.244 | 18.631 | 20.014 |
| 7 | 6.449 | 7.854 | 9.317 | 10.803 | 12.298 | 13.797 | 15.297 | 16.795 | 18.290 | 19.781 | 21.268 |
| 8 | 6.608 | 8.117 | 9.682 | 11.269 | 12.865 | 14.464 | 16.062 | 17.657 | 19.249 | 20.835 | 22.415 |
| 9 | 6.754 | 8.359 | 10.019 | 11.700 | 13.389 | 15.079 | 16.769 | 18.455 | 20.135 | 21.810 | 23.476 |
| 10 | 6.890 | 8.584 | 10.332 | 12.101 | 13.876 | 15.653 | 17.428 | 19.198 | 20.961 | 22.717 | 24.464 |
| 11 | 7.017 | 8.794 | 10.625 | 12.475 | 14.333 | 16.190 | 18.045 | 19.894 | 21.735 | 23.568 | 25.389 |
| 12 | 7.136 | 8.991 | 10.899 | 12.828 | 14.762 | 16.696 | 18.627 | 20.550 | 22.465 | 24.369 | 26.260 |
| 13 | 7.248 | 9.176 | 11.158 | 13.160 | 15.168 | 17.175 | 19.176 | 21.170 | 23.154 | 25.126 | 27.084 |
| 14 | 7.353 | 9.350 | 11.403 | 13.475 | 15.553 | 17.628 | 19.698 | 21.759 | 23.808 | 25.844 | 27.865 |
| 15 | 7.452 | 9.516 | 11.636 | 13.775 | 15.919 | 18.060 | 20.195 | 22.319 | 24.431 | 26.528 | 28.608 |
| 17 | 7.545 | 9.673 | 11.857 | 14.060 | 16.268 | 18.472 | 20.669 | 22.854 | 25.025 | 27.180 | 29.317 |
| 10 | 9.822 | 12.068 | 14.333 | 16.602 | 18.866 | 21.122 | 23.366 | 25.594 | 27.804 | 29.994 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 7.718 | 9.965 | 12.270 | 14.594 | 16.921 | 19.244 | 21.557 | 23.856 | 26.139 | 28.402 | 30.643 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 7.798 | 10.101 | 12.463 | 14.844 | 17.228 | 19.607 | 21.975 | 24.328 | 26.662 | 28.976 | 31.266 |
| 20 | 7.875 | 10.232 | 12.649 | 15.085 | 17.523 | 19.956 | 22.376 | 24.781 | 27.165 | 29.527 | 31.864 |
| 21 | 7.948 | 10.357 | 12.827 | 15.316 | 17.807 | 20.292 | 22.763 | 25.217 | 27.650 | 30.059 | 32.440 |
| 22 | 8.018 | 10.477 | 12.999 | 15.539 | 18.081 | 20.616 | 23.136 | 25.638 | 28.118 | 30.571 | 32.995 |
| 23 | 8.085 | 10.593 | 13.164 | 15.754 | 18.346 | 20.929 | 23.497 | 26.045 | 28.569 | 31.065 | 33.531 |
| 24 | 8.149 | 10.704 | 13.323 | 15.962 | 18.601 | 21.231 | 23.845 | 26.438 | 29.005 | 31.543 | 34.049 |
| 25 | 8.211 | 10.812 | 13.477 | 16.163 | 18.848 | 21.524 | 24.183 | 26.819 | 29.428 | 32.006 | 34.549 |
| 26 | 8.270 | 10.915 | 13.626 | 16.357 | 19.088 | 21.808 | 24.510 | 27.187 | 29.837 | 32.453 | 35.034 |
| 27 | 8.327 | 11.015 | 13.770 | 16.545 | 19.320 | 22.083 | 24.827 | 27.545 | 30.233 | 32.887 | 35.503 |
| 28 | 8.382 | 11.112 | 13.910 | 16.728 | 19.545 | 22.350 | 25.134 | 27.892 | 30.618 | 33.308 | 35.958 |
| 29 | 8.436 | 11.205 | 14.045 | 16.905 | 19.764 | 22.609 | 25.433 | 28.229 | 30.991 | 33.716 | 36.399 |
| 20 | 8.487 | 11.295 | 14.176 | 17.077 | 19.976 | 22.861 | 25.723 | 28.556 | 31.354 | 34.113 | 36.827 |

Table B. 31
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 100 / \text { Dividend Rate }=\mathbf{2 \%}
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 1.583 | 2.154 | 2.726 | 3.298 | 3.871 | 4.443 | 5.016 | 5.588 | 6.161 | 6.732 | 7.304 |
| 2 | 2.161 | 2.963 | 3.768 | 4.573 | 5.379 | 6.185 | 6.990 | 7.795 | 8.599 | 9.403 | 10.205 |
| 3 | 2.578 | 3.554 | 4.534 | 5.516 | 6.498 | 7.480 | 8.462 | 9.442 | 10.421 | 11.399 | 12.375 |
| 4 | 2.911 | 4.032 | 5.159 | 6.287 | 7.416 | 8.545 | 9.673 | 10.799 | 11.923 | 13.046 | 14.165 |
| 5 | 3.192 | 4.439 | 5.693 | 6.949 | 8.206 | 9.462 | 10.717 | 11.970 | 13.220 | 14.467 | 15.711 |
| 6 | 3.436 | 4.795 | 6.162 | 7.533 | 8.904 | 10.274 | 11.643 | 13.008 | 14.371 | 15.729 | 17.083 |
| 7 | 3.653 | 5.113 | 6.584 | 8.058 | 9.533 | 11.007 | 12.478 | 13.946 | 15.410 | 16.869 | 18.322 |
| 8 | 3.847 | 5.401 | 6.967 | 8.537 | 10.108 | 11.677 | 13.243 | 14.805 | 16.361 | 17.912 | 19.456 |
| 9 | 4.024 | 5.665 | 7.319 | 8.978 | 10.637 | 12.295 | 13.949 | 15.598 | 17.241 | 18.876 | 20.504 |
| 10 | 4.186 | 5.909 | 7.645 | 9.387 | 11.130 | 12.870 | 14.606 | 16.336 | 18.059 | 19.774 | 21.480 |
| 11 | 4.336 | 6.135 | 7.949 | 9.770 | 11.590 | 13.408 | 15.221 | 17.028 | 18.826 | 20.615 | 22.393 |
| 12 | 4.475 | 6.346 | 8.234 | 10.129 | 12.023 | 13.915 | 15.801 | 17.679 | 19.548 | 21.407 | 23.253 |
| 13 | 4.605 | 6.544 | 8.502 | 10.467 | 12.432 | 14.394 | 16.349 | 18.295 | 20.231 | 22.155 | 24.066 |
| 14 | 4.727 | 6.731 | 8.756 | 10.788 | 12.820 | 14.848 | 16.868 | 18.879 | 20.879 | 22.865 | 24.836 |
| 15 | 4.842 | 6.908 | 8.996 | 11.092 | 13.188 | 15.280 | 17.363 | 19.436 | 21.496 | 23.541 | 25.570 |
| 17 | 4.950 | 7.076 | 9.225 | 11.382 | 13.540 | 15.692 | 17.835 | 19.966 | 22.084 | 24.185 | 26.269 |
| 1052 | 7.235 | 9.442 | 11.659 | 13.875 | 16.085 | 18.286 | 20.474 | 22.647 | 24.802 | 26.937 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 5.149 | 7.387 | 9.650 | 11.924 | 14.197 | 16.463 | 18.719 | 20.961 | 23.186 | 25.392 | 27.577 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 5.241 | 7.531 | 9.850 | 12.178 | 14.505 | 16.825 | 19.134 | 21.428 | 23.704 | 25.959 | 28.192 |
| 20 | 5.328 | 7.670 | 10.041 | 12.422 | 14.801 | 17.174 | 19.533 | 21.877 | 24.202 | 26.504 | 28.782 |
| 21 | 5.412 | 7.803 | 10.224 | 12.656 | 15.087 | 17.509 | 19.918 | 22.310 | 24.681 | 27.029 | 29.351 |
| 22 | 5.491 | 7.930 | 10.401 | 12.882 | 15.362 | 17.833 | 20.289 | 22.728 | 25.144 | 27.535 | 29.898 |
| 23 | 5.568 | 8.053 | 10.571 | 13.100 | 15.627 | 18.145 | 20.648 | 23.131 | 25.591 | 28.024 | 30.427 |
| 24 | 5.641 | 8.170 | 10.734 | 13.310 | 15.864 | 18.447 | 20.994 | 23.521 | 26.023 | 28.496 | 30.937 |
| 25 | 5.711 | 8.284 | 10.893 | 13.514 | 16.132 | 18.740 | 21.330 | 23.898 | 26.440 | 28.952 | 31.431 |
| 26 | 5.778 | 8.393 | 11.045 | 13.710 | 16.372 | 19.023 | 21.655 | 24.264 | 26.845 | 29.395 | 31.909 |
| 27 | 5.843 | 8.499 | 11.193 | 13.901 | 16.605 | 19.297 | 21.970 | 24.618 | 27.237 | 29.823 | 32.372 |
| 28 | 5.905 | 8.601 | 11.337 | 14.086 | 16.831 | 19.564 | 22.276 | 24.962 | 27.618 | 30.239 | 32.821 |
| 29 | 5.965 | 8.699 | 11.475 | 14.265 | 17.051 | 19.822 | 22.573 | 25.296 | 27.988 | 30.642 | 33.256 |
| 20 | 6.022 | 8.795 | 11.610 | 14.439 | 17.264 | 20.074 | 22.862 | 25.621 | 28.347 | 31.034 | 33.679 |

Table B. 32
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 95 / \text { Dividend Rate }=2 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.211 | 0.523 | 0.915 | 1.356 | 1.828 | 2.320 | 2.826 | 3.341 | 3.864 | 4.392 | 4.925 |
| 2 | 0.560 | 1.129 | 1.776 | 2.466 | 3.182 | 3.915 | 4.659 | 5.411 | 6.167 | 6.928 | 7.691 |
| 3 | 0.872 | 1.629 | 2.461 | 3.333 | 4.229 | 5.140 | 6.060 | 6.987 | 7.918 | 8.851 | 9.786 |
| 4 | 1.146 | 2.055 | 3.037 | 4.058 | 5.102 | 6.159 | 7.225 | 8.296 | 9.370 | 10.447 | 11.523 |
| 5 | 1.388 | 2.427 | 3.539 | 4.689 | 5.860 | 7.043 | 8.235 | 9.431 | 10.630 | 11.829 | 13.027 |
| 6 | 1.605 | 2.759 | 3.986 | 5.249 | 6.534 | 7.830 | 9.134 | 10.441 | 11.750 | 13.058 | 14.364 |
| 7 | 1.801 | 3.060 | 4.390 | 5.757 | 7.144 | 8.542 | 9.947 | 11.355 | 12.763 | 14.170 | 15.573 |
| 8 | 1.981 | 3.334 | 4.759 | 6.221 | 7.702 | 9.195 | 10.693 | 12.193 | 13.692 | 15.189 | 16.680 |
| 9 | 2.147 | 3.588 | 5.100 | 6.650 | 8.219 | 9.798 | 11.383 | 12.968 | 14.552 | 16.131 | 17.704 |
| 10 | 2.300 | 3.823 | 5.418 | 7.049 | 8.700 | 10.361 | 12.026 | 13.691 | 15.352 | 17.009 | 18.658 |
| 11 | 2.443 | 4.042 | 5.714 | 7.423 | 9.151 | 10.888 | 12.629 | 14.368 | 16.103 | 17.832 | 19.552 |
| 12 | 2.577 | 4.248 | 5.993 | 7.775 | 9.575 | 11.385 | 13.197 | 15.006 | 16.810 | 18.607 | 20.394 |
| 13 | 2.703 | 4.442 | 6.256 | 8.107 | 9.976 | 11.854 | 13.734 | 15.610 | 17.480 | 19.340 | 21.190 |
| 14 | 2.821 | 4.625 | 6.505 | 8.422 | 10.357 | 12.300 | 14.244 | 16.183 | 18.115 | 20.036 | 21.945 |
| 15 | 2.933 | 4.799 | 6.741 | 8.721 | 10.719 | 12.724 | 14.729 | 16.729 | 18.719 | 20.698 | 22.663 |
| 16 | 3.039 | 4.964 | 6.967 | 9.007 | 11.065 | 13.129 | 15.193 | 17.250 | 19.296 | 21.330 | 23.348 |
| 17 | 3.139 | 5.121 | 7.182 | 9.280 | 11.395 | 13.517 | 15.636 | 17.748 | 19.849 | 21.935 | 24.004 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 3.235 | 5.271 | 7.387 | 9.541 | 11.712 | 13.889 | 16.062 | 18.226 | 20.378 | 22.514 | 24.631 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 3.326 | 5.415 | 7.584 | 9.792 | 12.016 | 14.245 | 16.470 | 18.685 | 20.887 | 23.070 | 25.234 |
| 20 | 3.413 | 5.552 | 7.773 | 10.033 | 12.308 | 14.589 | 16.863 | 19.127 | 21.376 | 23.605 | 25.813 |
| 21 | 3.496 | 5.684 | 7.955 | 10.264 | 12.590 | 14.919 | 17.242 | 19.553 | 21.847 | 24.121 | 26.371 |
| 22 | 3.576 | 5.811 | 8.130 | 10.488 | 12.862 | 15.238 | 17.607 | 19.963 | 22.301 | 24.618 | 26.908 |
| 23 | 3.652 | 5.933 | 8.299 | 10.703 | 13.124 | 15.546 | 17.960 | 20.360 | 22.740 | 25.097 | 27.427 |
| 24 | 3.725 | 6.050 | 8.462 | 10.912 | 13.377 | 15.844 | 18.302 | 20.744 | 23.165 | 25.561 | 27.928 |
| 25 | 3.795 | 6.163 | 8.619 | 11.113 | 13.623 | 16.133 | 18.632 | 21.115 | 23.576 | 26.010 | 28.413 |
| 26 | 3.863 | 6.273 | 8.771 | 11.308 | 13.860 | 16.412 | 18.953 | 21.475 | 23.974 | 26.444 | 28.882 |
| 27 | 3.928 | 6.378 | 8.918 | 11.497 | 14.091 | 16.683 | 19.263 | 21.824 | 24.359 | 26.865 | 29.337 |
| 28 | 3.991 | 6.480 | 9.060 | 11.680 | 14.314 | 16.946 | 19.565 | 22.162 | 24.734 | 27.274 | 29.778 |
| 29 | 4.051 | 6.579 | 9.199 | 11.858 | 14.531 | 17.202 | 19.858 | 22.491 | 25.097 | 27.670 | 30.206 |

Table B. 33
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 90 / \text { Dividend Rate }=2 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.008 | 0.064 | 0.199 | 0.413 | 0.691 | 1.020 | 1.387 | 1.784 | 2.204 | 2.642 | 3.095 |
| 2 | 0.080 | 0.306 | 0.672 | 1.140 | 1.677 | 2.264 | 2.886 | 3.533 | 4.200 | 4.881 | 5.573 |
| 3 | 0.198 | 0.594 | 1.151 | 1.812 | 2.540 | 3.315 | 4.121 | 4.950 | 5.796 | 6.654 | 7.520 |
| 4 | 0.334 | 0.880 | 1.596 | 2.414 | 3.298 | 4.225 | 5.181 | 6.158 | 7.149 | 8.150 | 9.159 |
| 5 | 0.473 | 1.153 | 2.005 | 2.958 | 3.974 | 5.031 | 6.116 | 7.219 | 8.335 | 9.460 | 10.590 |
| 6 | 0.611 | 1.410 | 2.382 | 3.454 | 4.587 | 5.759 | 6.957 | 8.171 | 9.398 | 10.631 | 11.870 |
| 7 | 0.745 | 1.651 | 2.731 | 3.910 | 5.148 | 6.424 | 7.724 | 9.039 | 10.365 | 11.697 | 13.031 |
| 8 | 0.874 | 1.878 | 3.057 | 4.333 | 5.667 | 7.037 | 8.431 | 9.838 | 11.255 | 12.676 | 14.099 |
| 9 | 0.997 | 2.092 | 3.362 | 4.728 | 6.151 | 7.608 | 9.088 | 10.580 | 12.080 | 13.584 | 15.088 |
| 10 | 1.115 | 2.294 | 3.648 | 5.098 | 6.603 | 8.142 | 9.702 | 11.274 | 12.852 | 14.432 | 16.010 |
| 11 | 1.227 | 2.485 | 3.919 | 5.447 | 7.030 | 8.645 | 10.280 | 11.926 | 13.577 | 15.228 | 16.876 |
| 12 | 1.334 | 2.667 | 4.175 | 5.777 | 7.432 | 9.120 | 10.826 | 12.541 | 14.261 | 15.979 | 17.692 |
| 13 | 1.437 | 2.840 | 4.418 | 6.090 | 7.814 | 9.570 | 11.343 | 13.125 | 14.909 | 16.690 | 18.465 |
| 14 | 1.535 | 3.004 | 4.649 | 6.388 | 8.178 | 9.998 | 11.835 | 13.679 | 15.524 | 17.365 | 19.198 |
| 15 | 1.629 | 3.162 | 4.870 | 6.672 | 8.525 | 10.407 | 12.304 | 14.208 | 16.111 | 18.008 | 19.896 |
| 17 | 1.719 | 3.312 | 5.082 | 6.944 | 8.856 | 10.797 | 12.753 | 14.713 | 16.672 | 18.623 | 20.563 |
| 17 | 3.456 | 5.284 | 7.204 | 9.174 | 11.172 | 13.183 | 15.197 | 17.209 | 19.211 | 21.201 |  |
| 105 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 1.888 | 3.594 | 5.478 | 7.454 | 9.479 | 11.531 | 13.595 | 15.662 | 17.724 | 19.775 | 21.812 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 1.967 | 3.727 | 5.665 | 7.694 | 9.773 | 11.877 | 13.992 | 16.108 | 18.218 | 20.317 | 22.400 |
| 20 | 2.044 | 3.855 | 5.845 | 7.926 | 10.055 | 12.209 | 14.374 | 16.538 | 18.695 | 20.838 | 22.964 |
| 21 | 2.118 | 3.978 | 6.018 | 8.149 | 10.327 | 12.530 | 14.742 | 16.953 | 19.154 | 21.340 | 23.508 |
| 22 | 2.188 | 4.097 | 6.185 | 8.364 | 10.590 | 12.840 | 15.098 | 17.353 | 19.597 | 21.825 | 24.032 |
| 23 | 2.257 | 4.211 | 6.346 | 8.572 | 10.845 | 13.140 | 15.442 | 17.740 | 20.025 | 22.293 | 24.539 |
| 24 | 2.323 | 4.322 | 6.502 | 8.773 | 11.091 | 13.430 | 15.775 | 18.114 | 20.439 | 22.746 | 25.028 |
| 25 | 2.386 | 4.429 | 6.653 | 8.968 | 11.329 | 13.711 | 16.097 | 18.476 | 20.840 | 23.184 | 25.501 |
| 26 | 2.448 | 4.532 | 6.799 | 9.157 | 11.560 | 13.983 | 16.410 | 18.828 | 21.229 | 23.608 | 25.960 |
| 27 | 2.507 | 4.632 | 6.941 | 9.340 | 11.784 | 14.247 | 16.713 | 19.168 | 21.606 | 24.020 | 26.404 |
| 28 | 2.564 | 4.729 | 7.079 | 9.518 | 12.002 | 14.504 | 17.007 | 19.499 | 21.972 | 24.419 | 26.835 |
| 29 | 2.620 | 4.823 | 7.212 | 9.691 | 12.213 | 14.753 | 17.293 | 19.821 | 22.327 | 24.807 | 27.253 |
| 20 | 2.674 | 4.915 | 7.342 | 9.859 | 12.419 | 14.996 | 17.572 | 20.133 | 22.673 | 25.183 | 27.659 |

Table B. 34
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 8 5} /$ Dividend Rate $=\mathbf{2 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.003 | 0.025 | 0.085 | 0.197 | 0.360 | 0.573 | 0.827 | 1.118 | 1.438 | 1.784 |
| 2 | 0.006 | 0.054 | 0.193 | 0.434 | 0.765 | 1.170 | 1.634 | 2.142 | 2.687 | 3.259 | 3.854 |
| 3 | 0.028 | 0.163 | 0.447 | 0.863 | 1.383 | 1.979 | 2.633 | 3.330 | 4.060 | 4.814 | 5.589 |
| 4 | 0.067 | 0.304 | 0.728 | 1.298 | 1.976 | 2.729 | 3.538 | 4.388 | 5.267 | 6.169 | 7.088 |
| 5 | 0.120 | 0.460 | 1.012 | 1.719 | 2.533 | 3.421 | 4.362 | 5.341 | 6.347 | 7.375 | 8.417 |
| 6 | 0.181 | 0.622 | 1.292 | 2.119 | 3.053 | 4.060 | 5.117 | 6.210 | 7.328 | 8.465 | 9.616 |
| 7 | 0.248 | 0.785 | 1.562 | 2.499 | 3.541 | 4.654 | 5.815 | 7.010 | 8.229 | 9.464 | 10.712 |
| 8 | 0.319 | 0.946 | 1.822 | 2.859 | 3.999 | 5.209 | 6.465 | 7.753 | 9.063 | 10.388 | 11.723 |
| 9 | 0.391 | 1.103 | 2.071 | 3.200 | 4.432 | 5.730 | 7.073 | 8.447 | 9.841 | 11.249 | 12.665 |
| 10 | 0.463 | 1.257 | 2.310 | 3.525 | 4.840 | 6.222 | 7.646 | 9.099 | 10.571 | 12.055 | 13.546 |
| 11 | 0.535 | 1.405 | 2.539 | 3.834 | 5.229 | 6.687 | 8.187 | 9.714 | 11.259 | 12.814 | 14.374 |
| 12 | 0.607 | 1.550 | 2.759 | 4.129 | 5.598 | 7.129 | 8.700 | 10.297 | 11.910 | 13.532 | 15.157 |
| 13 | 0.677 | 1.689 | 2.970 | 4.412 | 5.950 | 7.550 | 9.188 | 10.851 | 12.529 | 14.213 | 15.900 |
| 14 | 0.746 | 1.824 | 3.173 | 4.682 | 6.287 | 7.952 | 9.654 | 11.379 | 13.118 | 14.862 | 16.606 |
| 15 | 0.814 | 1.954 | 3.369 | 4.941 | 6.610 | 8.336 | 10.099 | 11.884 | 13.680 | 15.480 | 17.278 |
| 16 | 0.880 | 2.081 | 3.557 | 5.191 | 6.919 | 8.705 | 10.526 | 12.367 | 14.218 | 16.072 | 17.922 |
| 17 | 0.945 | 2.203 | 3.738 | 5.431 | 7.217 | 9.060 | 10.936 | 12.831 | 14.735 | 16.639 | 18.537 |


| 18 | 1.008 | 2.321 | 3.913 | 5.662 | 7.504 | 9.401 | 11.330 | 13.276 | 15.230 | 17.183 | 19.128 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 1.069 | 2.435 | 4.082 | 5.885 | 7.780 | 9.729 | 11.709 | 13.705 | 15.707 | 17.706 | 19.696 |
| 20 | 1.128 | 2.546 | 4.245 | 6.101 | 8.047 | 10.046 | 12.075 | 14.119 | 16.167 | 18.210 | 20.243 |
| 21 | 1.186 | 2.654 | 4.404 | 6.309 | 8.305 | 10.352 | 12.429 | 14.518 | 16.610 | 18.696 | 20.769 |
| 22 | 1.243 | 2.758 | 4.557 | 6.511 | 8.555 | 10.649 | 12.770 | 14.904 | 17.039 | 19.165 | 21.278 |
| 23 | 1.298 | 2.859 | 4.705 | 6.707 | 8.796 | 10.935 | 13.101 | 15.277 | 17.453 | 19.619 | 21.769 |
| 24 | 1.351 | 2.958 | 4.849 | 6.896 | 9.030 | 11.213 | 13.421 | 15.639 | 17.854 | 20.057 | 22.243 |
| 25 | 1.403 | 3.053 | 4.989 | 7.080 | 9.258 | 11.483 | 13.732 | 15.989 | 18.242 | 20.482 | 22.703 |
| 26 | 1.454 | 3.146 | 5.125 | 7.259 | 9.478 | 11.744 | 14.033 | 16.329 | 18.619 | 20.894 | 23.148 |
| 27 | 1.503 | 3.236 | 5.257 | 7.432 | 9.692 | 11.998 | 14.326 | 16.659 | 18.984 | 21.293 | 23.579 |
| 28 | 1.551 | 3.324 | 5.385 | 7.601 | 9.901 | 12.245 | 14.611 | 16.980 | 19.339 | 21.681 | 23.998 |
| 29 | 1.598 | 3.409 | 5.510 | 7.765 | 10.104 | 12.486 | 14.887 | 17.291 | 19.684 | 22.057 | 24.405 |
| 30 | 1.643 | 3.492 | 5.632 | 7.925 | 10.301 | 12.720 | 15.157 | 17.594 | 20.020 | 22.424 | 24.800 |

Table B. 35
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 80 /$ Dividend Rate $=\mathbf{2 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.002 | 0.011 | 0.039 | 0.097 | 0.191 | 0.322 | 0.490 | 0.692 | 0.925 |
| 2 | 0.000 | 0.006 | 0.040 | 0.130 | 0.292 | 0.528 | 0.829 | 1.187 | 1.593 | 2.039 | 2.519 |
| 3 | 0.002 | 0.032 | 0.138 | 0.350 | 0.667 | 1.076 | 1.559 | 2.104 | 2.696 | 3.328 | 3.991 |
| 4 | 0.009 | 0.081 | 0.279 | 0.618 | 1.080 | 1.640 | 2.279 | 2.977 | 3.722 | 4.504 | 5.315 |
| 5 | 0.022 | 0.149 | 0.445 | 0.904 | 1.497 | 2.192 | 2.964 | 3.794 | 4.669 | 5.579 | 6.514 |
| 6 | 0.040 | 0.230 | 0.623 | 1.195 | 1.906 | 2.720 | 3.610 | 4.557 | 5.546 | 6.567 | 7.612 |
| 7 | 0.065 | 0.320 | 0.807 | 1.484 | 2.303 | 3.225 | 4.220 | 5.271 | 6.362 | 7.482 | 8.625 |
| 8 | 0.093 | 0.416 | 0.992 | 1.767 | 2.685 | 3.705 | 4.797 | 5.942 | 7.125 | 8.336 | 9.567 |
| 9 | 0.125 | 0.516 | 1.177 | 2.042 | 3.052 | 4.162 | 5.343 | 6.574 | 7.842 | 9.136 | 10.448 |
| 10 | 0.161 | 0.617 | 1.359 | 2.310 | 3.404 | 4.598 | 5.861 | 7.173 | 8.519 | 9.890 | 11.276 |
| 11 | 0.198 | 0.719 | 1.538 | 2.568 | 3.743 | 5.015 | 6.355 | 7.742 | 9.161 | 10.602 | 12.059 |
| 12 | 0.237 | 0.820 | 1.713 | 2.819 | 4.068 | 5.414 | 6.826 | 8.283 | 9.770 | 11.279 | 12.800 |
| 13 | 0.277 | 0.921 | 1.883 | 3.061 | 4.381 | 5.797 | 7.276 | 8.799 | 10.351 | 11.922 | 13.504 |
| 14 | 0.318 | 1.021 | 2.050 | 3.296 | 4.683 | 6.164 | 7.708 | 9.293 | 10.906 | 12.536 | 14.176 |
| 15 | 0.359 | 1.120 | 2.212 | 3.522 | 4.974 | 6.517 | 8.122 | 9.767 | 11.438 | 13.124 | 14.818 |
| 16 | 0.401 | 1.216 | 2.370 | 3.742 | 5.254 | 6.858 | 8.520 | 10.222 | 11.947 | 13.687 | 15.432 |
| 17 | 0.442 | 1.311 | 2.524 | 3.955 | 5.525 | 7.186 | 8.904 | 10.659 | 12.437 | 14.227 | 16.021 |


| 18 | 0.484 | 1.405 | 2.673 | 4.161 | 5.788 | 7.502 | 9.274 | 11.081 | 12.908 | 14.747 | 16.587 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.525 | 1.496 | 2.819 | 4.361 | 6.041 | 7.808 | 9.631 | 11.487 | 13.363 | 15.247 | 17.132 |
| 20 | 0.566 | 1.585 | 2.960 | 4.555 | 6.287 | 8.105 | 9.976 | 11.879 | 13.801 | 15.730 | 17.657 |
| 21 | 0.606 | 1.673 | 3.098 | 4.744 | 6.525 | 8.391 | 10.310 | 12.259 | 14.225 | 16.196 | 18.163 |
| 22 | 0.646 | 1.758 | 3.233 | 4.927 | 6.757 | 8.669 | 10.633 | 12.626 | 14.634 | 16.646 | 18.652 |
| 23 | 0.685 | 1.842 | 3.364 | 5.106 | 6.981 | 8.939 | 10.947 | 12.982 | 15.031 | 17.081 | 19.124 |
| 24 | 0.724 | 1.924 | 3.491 | 5.279 | 7.199 | 9.201 | 11.251 | 13.327 | 15.415 | 17.503 | 19.581 |
| 25 | 0.763 | 2.004 | 3.616 | 5.448 | 7.412 | 9.455 | 11.546 | 13.662 | 15.788 | 17.912 | 20.024 |
| 26 | 0.800 | 2.082 | 3.737 | 5.612 | 7.618 | 9.703 | 11.833 | 13.987 | 16.150 | 18.308 | 20.454 |
| 27 | 0.837 | 2.159 | 3.855 | 5.772 | 7.819 | 9.943 | 12.112 | 14.303 | 16.501 | 18.693 | 20.870 |
| 28 | 0.873 | 2.234 | 3.971 | 5.928 | 8.015 | 10.178 | 12.384 | 14.611 | 16.843 | 19.067 | 21.274 |
| 29 | 0.909 | 2.307 | 4.084 | 6.080 | 8.205 | 10.406 | 12.648 | 14.910 | 17.175 | 19.430 | 21.667 |
| 30 | 0.944 | 2.378 | 4.194 | 6.229 | 8.391 | 10.628 | 12.906 | 15.201 | 17.498 | 19.783 | 22.049 |

Table B. 36
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 7 5} /$ Dividend Rate $=\mathbf{2 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.019 | 0.049 | 0.101 | 0.180 | 0.287 | 0.422 |
| 2 | 0.000 | 0.000 | 0.006 | 0.029 | 0.090 | 0.201 | 0.368 | 0.589 | 0.861 | 1.180 | 1.538 |
| 3 | 0.000 | 0.004 | 0.033 | 0.117 | 0.278 | 0.522 | 0.843 | 1.232 | 1.680 | 2.178 | 2.717 |
| 4 | 0.001 | 0.016 | 0.087 | 0.254 | 0.528 | 0.904 | 1.368 | 1.905 | 2.503 | 3.150 | 3.838 |
| 5 | 0.003 | 0.038 | 0.165 | 0.422 | 0.808 | 1.308 | 1.900 | 2.568 | 3.296 | 4.072 | 4.885 |
| 6 | 0.007 | 0.069 | 0.261 | 0.609 | 1.102 | 1.715 | 2.424 | 3.208 | 4.050 | 4.938 | 5.863 |
| 7 | 0.013 | 0.109 | 0.369 | 0.807 | 1.401 | 2.118 | 2.933 | 3.821 | 4.766 | 5.755 | 6.777 |
| 8 | 0.022 | 0.156 | 0.485 | 1.010 | 1.698 | 2.512 | 3.423 | 4.406 | 5.444 | 6.524 | 7.636 |
| 9 | 0.032 | 0.209 | 0.607 | 1.215 | 1.991 | 2.895 | 3.895 | 4.966 | 6.089 | 7.253 | 8.446 |
| 10 | 0.046 | 0.266 | 0.732 | 1.419 | 2.279 | 3.267 | 4.349 | 5.500 | 6.703 | 7.944 | 9.212 |
| 11 | 0.061 | 0.326 | 0.859 | 1.622 | 2.560 | 3.626 | 4.785 | 6.012 | 7.289 | 8.601 | 9.939 |
| 12 | 0.078 | 0.389 | 0.986 | 1.822 | 2.834 | 3.974 | 5.206 | 6.503 | 7.848 | 9.227 | 10.630 |
| 13 | 0.096 | 0.454 | 1.114 | 2.018 | 3.101 | 4.310 | 5.610 | 6.974 | 8.384 | 9.826 | 11.290 |
| 14 | 0.116 | 0.520 | 1.240 | 2.211 | 3.360 | 4.636 | 6.000 | 7.427 | 8.898 | 10.399 | 11.921 |
| 15 | 0.137 | 0.586 | 1.366 | 2.399 | 3.612 | 4.951 | 6.377 | 7.864 | 9.392 | 10.949 | 12.525 |
| 16 | 0.159 | 0.653 | 1.490 | 2.584 | 3.858 | 5.256 | 6.741 | 8.284 | 9.868 | 11.478 | 13.105 |
| 17 | 0.182 | 0.720 | 1.612 | 2.764 | 4.097 | 5.552 | 7.092 | 8.690 | 10.326 | 11.986 | 13.662 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.205 | 0.787 | 1.732 | 2.940 | 4.329 | 5.839 | 7.433 | 9.082 | 10.767 | 12.476 | 14.198 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.229 | 0.854 | 1.850 | 3.113 | 4.555 | 6.118 | 7.762 | 9.461 | 11.194 | 12.949 | 14.715 |
| 20 | 0.253 | 0.920 | 1.967 | 3.281 | 4.775 | 6.388 | 8.082 | 9.828 | 11.607 | 13.406 | 15.214 |
| 21 | 0.278 | 0.986 | 2.081 | 3.445 | 4.989 | 6.651 | 8.392 | 10.183 | 12.007 | 13.848 | 15.696 |
| 22 | 0.303 | 1.051 | 2.193 | 3.606 | 5.198 | 6.907 | 8.693 | 10.528 | 12.394 | 14.275 | 16.162 |
| 23 | 0.328 | 1.115 | 2.303 | 3.763 | 5.401 | 7.156 | 8.985 | 10.863 | 12.769 | 14.689 | 16.613 |
| 24 | 0.353 | 1.179 | 2.411 | 3.916 | 5.599 | 7.398 | 9.270 | 11.188 | 13.133 | 15.091 | 17.050 |
| 25 | 0.378 | 1.241 | 2.517 | 4.066 | 5.793 | 7.633 | 9.546 | 11.504 | 13.487 | 15.481 | 17.474 |
| 26 | 0.403 | 1.303 | 2.620 | 4.213 | 5.982 | 7.863 | 9.816 | 11.811 | 13.830 | 15.859 | 17.884 |
| 27 | 0.427 | 1.364 | 2.722 | 4.356 | 6.166 | 8.087 | 10.078 | 12.110 | 14.165 | 16.227 | 18.283 |
| 28 | 0.452 | 1.424 | 2.822 | 4.496 | 6.346 | 8.305 | 10.333 | 12.402 | 14.490 | 16.584 | 18.671 |
| 29 | 0.477 | 1.483 | 2.920 | 4.633 | 6.521 | 8.519 | 10.583 | 12.685 | 14.807 | 16.932 | 19.048 |
| 30 | 0.501 | 1.541 | 3.016 | 4.768 | 6.693 | 8.727 | 10.826 | 12.962 | 15.115 | 17.270 | 19.414 |

Table B. 37
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 7 0} /$ Dividend Rate $=\mathbf{2 \%}$

## Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.009 | 0.025 | 0.053 | 0.099 | 0.165 |
| 2 | 0.000 | 0.000 | 0.001 | 0.005 | 0.022 | 0.063 | 0.139 | 0.256 | 0.417 | 0.620 | 0.865 |
| 3 | 0.000 | 0.001 | 0.006 | 0.031 | 0.097 | 0.221 | 0.408 | 0.659 | 0.969 | 1.334 | 1.746 |
| 4 | 0.000 | 0.003 | 0.022 | 0.087 | 0.226 | 0.448 | 0.754 | 1.136 | 1.585 | 2.093 | 2.649 |
| 5 | 0.000 | 0.008 | 0.051 | 0.171 | 0.391 | 0.716 | 1.136 | 1.640 | 2.214 | 2.847 | 3.529 |
| 6 | 0.001 | 0.017 | 0.093 | 0.275 | 0.581 | 1.005 | 1.533 | 2.148 | 2.835 | 3.579 | 4.371 |
| 7 | 0.002 | 0.031 | 0.146 | 0.395 | 0.786 | 1.306 | 1.934 | 2.651 | 3.439 | 4.284 | 5.174 |
| 8 | 0.004 | 0.049 | 0.209 | 0.526 | 1.000 | 1.610 | 2.331 | 3.141 | 4.022 | 4.958 | 5.938 |
| 9 | 0.007 | 0.072 | 0.279 | 0.664 | 1.218 | 1.913 | 2.721 | 3.618 | 4.585 | 5.604 | 6.666 |
| 10 | 0.011 | 0.099 | 0.355 | 0.808 | 1.438 | 2.214 | 3.103 | 4.081 | 5.126 | 6.223 | 7.360 |
| 11 | 0.016 | 0.129 | 0.435 | 0.954 | 1.658 | 2.510 | 3.476 | 4.528 | 5.647 | 6.816 | 8.023 |
| 12 | 0.022 | 0.162 | 0.519 | 1.102 | 1.877 | 2.800 | 3.838 | 4.962 | 6.150 | 7.386 | 8.657 |
| 13 | 0.028 | 0.198 | 0.606 | 1.251 | 2.093 | 3.085 | 4.191 | 5.381 | 6.633 | 7.933 | 9.265 |
| 14 | 0.036 | 0.236 | 0.694 | 1.400 | 2.306 | 3.363 | 4.533 | 5.786 | 7.100 | 8.459 | 9.849 |
| 15 | 0.045 | 0.276 | 0.783 | 1.548 | 2.515 | 3.635 | 4.866 | 6.179 | 7.551 | 8.965 | 10.410 |
| 16 | 0.055 | 0.317 | 0.873 | 1.694 | 2.721 | 3.900 | 5.190 | 6.559 | 7.986 | 9.454 | 10.950 |
| 17 | 0.065 | 0.360 | 0.964 | 1.840 | 2.924 | 4.159 | 5.505 | 6.928 | 8.407 | 9.926 | 11.470 |


| 18 | 0.076 | 0.403 | 1.054 | 1.983 | 3.122 | 4.412 | 5.811 | 7.286 | 8.815 | 10.381 | 11.972 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.088 | 0.447 | 1.144 | 2.125 | 3.316 | 4.659 | 6.108 | 7.633 | 9.210 | 10.822 | 12.457 |
| 20 | 0.100 | 0.492 | 1.233 | 2.264 | 3.507 | 4.900 | 6.398 | 7.970 | 9.593 | 11.249 | 12.925 |
| 21 | 0.113 | 0.537 | 1.322 | 2.401 | 3.693 | 5.134 | 6.680 | 8.298 | 9.964 | 11.662 | 13.379 |
| 22 | 0.126 | 0.582 | 1.411 | 2.536 | 3.876 | 5.364 | 6.955 | 8.617 | 10.325 | 12.063 | 13.819 |
| 23 | 0.140 | 0.627 | 1.498 | 2.669 | 4.054 | 5.588 | 7.223 | 8.927 | 10.676 | 12.453 | 14.245 |
| 24 | 0.154 | 0.673 | 1.584 | 2.800 | 4.230 | 5.807 | 7.484 | 9.228 | 11.016 | 12.831 | 14.658 |
| 25 | 0.168 | 0.718 | 1.670 | 2.928 | 4.401 | 6.020 | 7.739 | 9.522 | 11.348 | 13.198 | 15.059 |
| 26 | 0.183 | 0.763 | 1.754 | 3.054 | 4.569 | 6.229 | 7.987 | 9.809 | 11.670 | 13.555 | 15.449 |
| 27 | 0.197 | 0.808 | 1.837 | 3.178 | 4.734 | 6.434 | 8.230 | 10.088 | 11.985 | 13.902 | 15.828 |
| 28 | 0.212 | 0.853 | 1.920 | 3.300 | 4.895 | 6.633 | 8.466 | 10.360 | 12.291 | 14.241 | 16.196 |
| 29 | 0.227 | 0.897 | 2.001 | 3.420 | 5.053 | 6.829 | 8.698 | 10.626 | 12.589 | 14.570 | 16.554 |
| 30 | 0.242 | 0.942 | 2.081 | 3.537 | 5.208 | 7.020 | 8.924 | 10.885 | 12.880 | 14.891 | 16.903 |

Table B. 38
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 6 5} /$ Dividend Rate $=\mathbf{2 \%}$

## Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.012 | 0.027 | 0.053 |
| 2 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.015 | 0.043 | 0.095 | 0.176 | 0.291 | 0.440 |
| 3 | 0.000 | 0.000 | 0.001 | 0.006 | 0.028 | 0.079 | 0.172 | 0.315 | 0.509 | 0.754 | 1.046 |
| 4 | 0.000 | 0.000 | 0.004 | 0.025 | 0.082 | 0.195 | 0.375 | 0.622 | 0.934 | 1.306 | 1.732 |
| 5 | 0.000 | 0.001 | 0.013 | 0.058 | 0.166 | 0.353 | 0.624 | 0.976 | 1.401 | 1.891 | 2.436 |
| 6 | 0.000 | 0.003 | 0.027 | 0.107 | 0.274 | 0.539 | 0.902 | 1.355 | 1.885 | 2.481 | 3.134 |
| 7 | 0.000 | 0.007 | 0.049 | 0.170 | 0.400 | 0.745 | 1.197 | 1.744 | 2.371 | 3.066 | 3.816 |
| 8 | 0.001 | 0.013 | 0.077 | 0.245 | 0.540 | 0.963 | 1.500 | 2.136 | 2.853 | 3.637 | 4.476 |
| 9 | 0.002 | 0.021 | 0.112 | 0.328 | 0.689 | 1.188 | 1.807 | 2.526 | 3.326 | 4.193 | 5.113 |
| 10 | 0.002 | 0.031 | 0.152 | 0.419 | 0.845 | 1.417 | 2.113 | 2.910 | 3.789 | 4.732 | 5.727 |
| 11 | 0.004 | 0.044 | 0.197 | 0.516 | 1.006 | 1.648 | 2.417 | 3.288 | 4.239 | 5.254 | 6.319 |
| 12 | 0.005 | 0.059 | 0.246 | 0.617 | 1.169 | 1.879 | 2.718 | 3.658 | 4.678 | 5.759 | 6.889 |
| 13 | 0.007 | 0.076 | 0.299 | 0.721 | 1.334 | 2.109 | 3.014 | 4.019 | 5.104 | 6.248 | 7.438 |
| 14 | 0.010 | 0.095 | 0.354 | 0.827 | 1.500 | 2.337 | 3.304 | 4.372 | 5.517 | 6.721 | 7.969 |
| 15 | 0.013 | 0.115 | 0.412 | 0.936 | 1.665 | 2.562 | 3.590 | 4.717 | 5.919 | 7.179 | 8.481 |
| 16 | 0.016 | 0.137 | 0.471 | 1.045 | 1.830 | 2.784 | 3.869 | 5.052 | 6.310 | 7.623 | 8.975 |
| 17 | 0.020 | 0.161 | 0.533 | 1.155 | 1.993 | 3.003 | 4.142 | 5.380 | 6.690 | 8.053 | 9.454 |


| 18 | 0.025 | 0.186 | 0.595 | 1.265 | 2.155 | 3.218 | 4.410 | 5.699 | 7.058 | 8.469 | 9.917 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.029 | 0.212 | 0.658 | 1.375 | 2.316 | 3.429 | 4.672 | 6.010 | 7.417 | 8.874 | 10.365 |
| 20 | 0.035 | 0.239 | 0.722 | 1.484 | 2.474 | 3.637 | 4.928 | 6.314 | 7.766 | 9.267 | 10.800 |
| 21 | 0.040 | 0.266 | 0.787 | 1.593 | 2.630 | 3.841 | 5.179 | 6.609 | 8.106 | 9.649 | 11.222 |
| 22 | 0.046 | 0.295 | 0.852 | 1.701 | 2.784 | 4.041 | 5.424 | 6.898 | 8.437 | 10.019 | 11.631 |
| 23 | 0.053 | 0.324 | 0.917 | 1.809 | 2.936 | 4.237 | 5.664 | 7.180 | 8.759 | 10.380 | 12.028 |
| 24 | 0.060 | 0.353 | 0.982 | 1.915 | 3.085 | 4.430 | 5.898 | 7.455 | 9.073 | 10.731 | 12.415 |
| 25 | 0.067 | 0.383 | 1.046 | 2.020 | 3.233 | 4.619 | 6.128 | 7.724 | 9.379 | 11.073 | 12.790 |
| 26 | 0.074 | 0.413 | 1.111 | 2.124 | 3.378 | 4.804 | 6.353 | 7.986 | 9.678 | 11.406 | 13.156 |
| 27 | 0.082 | 0.444 | 1.176 | 2.227 | 3.520 | 4.986 | 6.573 | 8.243 | 9.969 | 11.730 | 13.511 |
| 28 | 0.090 | 0.475 | 1.240 | 2.329 | 3.660 | 5.164 | 6.788 | 8.494 | 10.253 | 12.047 | 13.858 |
| 29 | 0.098 | 0.506 | 1.303 | 2.429 | 3.798 | 5.339 | 6.999 | 8.739 | 10.531 | 12.355 | 14.195 |
| 20 | 0.106 | 0.537 | 1.366 | 2.528 | 3.934 | 5.511 | 7.205 | 8.978 | 10.802 | 12.656 | 14.524 |

Table B. 39
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 6 0} /$ Dividend Rate $=\mathbf{2 \%}$

## Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.002 | 0.006 | 0.014 |
| 2 | 0000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.003 | 0.011 | 0.029 | 0.063 | 0.118 | 0.198 |
| 3 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.023 | 0.062 | 0.132 | 0.238 | 0.386 | 0.576 |
| 4 | 0.000 | 0.000 | 0.001 | 0.006 | 0.025 | 0.073 | 0.164 | 0.306 | 0.503 | 0.755 | 1.059 |
| 5 | 0.000 | 0.000 | 0.003 | 0.016 | 0.060 | 0.153 | 0.309 | 0.533 | 0.824 | 1.179 | 1.592 |
| 6 | 0.000 | 0.001 | 0.007 | 0.036 | 0.113 | 0.260 | 0.486 | 0.794 | 1.177 | 1.630 | 2.143 |
| 7 | 0.000 | 0.002 | 0.014 | 0.063 | 0.181 | 0.387 | 0.686 | 1.076 | 1.548 | 2.092 | 2.698 |
| 8 | 0.000 | 0.003 | 0.024 | 0.100 | 0.263 | 0.530 | 0.902 | 1.371 | 1.927 | 2.556 | 3.248 |
| 9 | 0.000 | 0.005 | 0.039 | 0.144 | 0.355 | 0.684 | 1.127 | 1.673 | 2.308 | 3.017 | 3.789 |
| 10 | 0.001 | 0.009 | 0.057 | 0.195 | 0.456 | 0.847 | 1.360 | 1.979 | 2.688 | 3.471 | 4.316 |
| 11 | 0.001 | 0.013 | 0.078 | 0.252 | 0.564 | 1.016 | 1.595 | 2.284 | 3.063 | 3.917 | 4.830 |
| 12 | 0.001 | 0.018 | 0.103 | 0.314 | 0.677 | 1.189 | 1.833 | 2.587 | 3.433 | 4.352 | 5.330 |
| 13 | 0.002 | 0.025 | 0.131 | 0.380 | 0.794 | 1.364 | 2.070 | 2.888 | 3.797 | 4.778 | 5.816 |
| 14 | 0.003 | 0.033 | 0.162 | 0.450 | 0.915 | 1.541 | 2.307 | 3.185 | 4.153 | 5.193 | 6.288 |
| 15 | 0.003 | 0.042 | 0.195 | 0.523 | 1.037 | 1.719 | 2.541 | 3.477 | 4.502 | 5.597 | 6.746 |
| 16 | 0.005 | 0.052 | 0.231 | 0.598 | 1.161 | 1.896 | 2.774 | 3.764 | 4.843 | 5.991 | 7.191 |
| 17 | 0.006 | 0.064 | 0.268 | 0.676 | 1.286 | 2.073 | 3.003 | 4.047 | 5.177 | 6.375 | 7.623 |


| 18 | 0.007 | 0.076 | 0.307 | 0.754 | 1.412 | 2.249 | 3.230 | 4.324 | 5.504 | 6.749 | 8.043 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.009 | 0.089 | 0.348 | 0.834 | 1.537 | 2.423 | 3.453 | 4.595 | 5.822 | 7.113 | 8.451 |
| 20 | 0.011 | 0.104 | 0.390 | 0.915 | 1.663 | 2.595 | 3.673 | 4.862 | 6.134 | 7.468 | 8.848 |
| 21 | 0.013 | 0.119 | 0.433 | 0.996 | 1.788 | 2.766 | 3.889 | 5.123 | 6.438 | 7.814 | 9.233 |
| 22 | 0.015 | 0.135 | 0.477 | 1.078 | 1.912 | 2.935 | 4.102 | 5.379 | 6.736 | 8.152 | 9.609 |
| 23 | 0.018 | 0.151 | 0.521 | 1.160 | 2.036 | 3.101 | 4.311 | 5.629 | 7.027 | 8.481 | 9.975 |
| 24 | 0.021 | 0.168 | 0.567 | 1.242 | 2.158 | 3.265 | 4.517 | 5.875 | 7.311 | 8.802 | 10.331 |
| 25 | 0.024 | 0.186 | 0.613 | 1.324 | 2.280 | 3.427 | 4.718 | 6.115 | 7.589 | 9.115 | 10.678 |
| 26 | 0.027 | 0.204 | 0.659 | 1.406 | 2.400 | 3.587 | 4.917 | 6.351 | 7.860 | 9.421 | 11.016 |
| 27 | 0.030 | 0.223 | 0.705 | 1.487 | 2.519 | 3.744 | 5.112 | 6.582 | 8.126 | 9.720 | 11.345 |
| 28 | 0.034 | 0.242 | 0.752 | 1.568 | 2.637 | 3.899 | 5.303 | 6.809 | 8.386 | 10.011 | 11.667 |
| 29 | 0.037 | 0.262 | 0.799 | 1.649 | 2.754 | 4.052 | 5.491 | 7.031 | 8.640 | 10.296 | 11.981 |
| 20 | 0.041 | 0.282 | 0.846 | 1.729 | 2.869 | 4.202 | 5.675 | 7.248 | 8.889 | 10.575 | 12.287 |

Table B. 40
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 120 / \text { Dividend Rate }=3 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 20.000 | 20.000 | 20.000 | 20.000 | 20.012 | 20.114 | 20.297 | 20.543 | 20.840 | 21.179 | 21.553 |
| 2 | 20.000 | 20.000 | 20.000 | 20.074 | 20.346 | 20.748 | 21.241 | 21.801 | 22.413 | 23.064 | 23.746 |
| 3 | 20.000 | 20.000 | 20.026 | 20.331 | 20.847 | 21.493 | 22.227 | 23.024 | 23.868 | 24.746 | 25.651 |
| 4 | 20.000 | 20.000 | 20.140 | 20.655 | 21.377 | 22.225 | 23.156 | 24.145 | 25.175 | 26.236 | 27.320 |
| 5 | 20.000 | 20.000 | 20.300 | 20.999 | 21.900 | 22.921 | 24.019 | 25.170 | 26.359 | 27.575 | 28.810 |
| 6 | 20.000 | 20.009 | 20.482 | 21.345 | 22.403 | 23.575 | 24.820 | 26.114 | 27.442 | 28.793 | 30.161 |
| 7 | 20.000 | 20.045 | 20.674 | 21.684 | 22.884 | 24.192 | 25.568 | 26.989 | 28.441 | 29.914 | 31.400 |
| 8 | 20.000 | 20.097 | 20.870 | 22.014 | 23.342 | 24.773 | 26.268 | 27.805 | 29.370 | 30.952 | 32.546 |
| 9 | 20.000 | 20.161 | 21.066 | 22.334 | 23.778 | 25.322 | 26.927 | 28.571 | 30.239 | 31.922 | 33.615 |
| 10 | 20.000 | 20.233 | 21.259 | 22.641 | 24.195 | 25.844 | 27.550 | 29.292 | 31.056 | 32.832 | 34.616 |
| 11 | 20.000 | 20.310 | 21.450 | 22.938 | 24.593 | 26.340 | 28.140 | 29.974 | 31.827 | 33.691 | 35.558 |
| 12 | 20.000 | 20.389 | 21.636 | 23.224 | 24.974 | 26.812 | 28.702 | 30.621 | 32.558 | 34.503 | 36.448 |
| 13 | 20.000 | 20.471 | 21.818 | 23.500 | 25.339 | 27.264 | 29.237 | 31.238 | 33.253 | 35.273 | 37.293 |
| 14 | 20.000 | 20.554 | 21.995 | 23.765 | 25.690 | 27.696 | 29.748 | 31.826 | 33.915 | 36.007 | 38.096 |
| 15 | 20.000 | 20.637 | 22.167 | 24.022 | 26.027 | 28.111 | 30.238 | 32.388 | 34.548 | 36.708 | 38.862 |
| 16 | 20.000 | 20.720 | 22.335 | 24.270 | 26.352 | 28.510 | 30.708 | 32.927 | 35.153 | 37.378 | 39.594 |
| 17 | 20.000 | 20.802 | 22.498 | 24.510 | 26.665 | 28.893 | 31.160 | 33.445 | 35.734 | 38.020 | 40.295 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 20.000 | 20.883 | 22.657 | 24.742 | 26.967 | 29.263 | 31.595 | 33.943 | 36.292 | 38.636 | 40.968 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 20.000 | 20.964 | 22.812 | 24.967 | 27.259 | 29.620 | 32.014 | 34.422 | 36.830 | 39.229 | 41.615 |
| 20 | 20.001 | 21.043 | 22.962 | 25.184 | 27.541 | 29.965 | 32.419 | 34.884 | 37.347 | 39.801 | 42.237 |
| 21 | 20.003 | 21.122 | 23.109 | 25.396 | 27.815 | 30.298 | 32.810 | 35.330 | 37.847 | 40.351 | 42.837 |
| 22 | 20.008 | 21.199 | 23.252 | 25.601 | 28.080 | 30.621 | 33.188 | 35.761 | 38.329 | 40.883 | 43.416 |
| 23 | 20.014 | 21.274 | 23.391 | 25.800 | 28.337 | 30.934 | 33.554 | 36.179 | 38.796 | 41.397 | 43.975 |
| 24 | 20.022 | 21.348 | 23.526 | 25.994 | 28.587 | 31.237 | 33.908 | 36.583 | 39.248 | 41.894 | 44.515 |
| 25 | 20.030 | 21.421 | 23.658 | 26.182 | 28.829 | 31.531 | 34.252 | 36.975 | 39.685 | 42.375 | 45.038 |
| 26 | 20.040 | 21.493 | 23.787 | 26.366 | 29.065 | 31.817 | 34.586 | 37.355 | 40.110 | 42.842 | 45.544 |
| 27 | 20.050 | 21.563 | 23.913 | 26.544 | 29.294 | 32.094 | 34.911 | 37.724 | 40.522 | 43.295 | 46.035 |
| 28 | 20.061 | 21.632 | 24.035 | 26.718 | 29.517 | 32.364 | 35.226 | 38.083 | 40.922 | 43.734 | 46.511 |
| 29 | 20.073 | 21.700 | 24.155 | 26.888 | 29.734 | 32.627 | 35.533 | 38.432 | 41.311 | 44.160 | 46.974 |
| 30 | 20.085 | 21.766 | 24.272 | 27.053 | 29.946 | 32.883 | 35.831 | 38.771 | 41.689 | 44.575 | 47.423 |

Table B. 41
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 115 / \text { Dividend Rate }=3 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 15.000 | 15.000 | 15.000 | 15.047 | 15.213 | 15.465 | 15.779 | 16.141 | 16.542 | 16.972 | 17.427 |
| 2 | 15.000 | 15.000 | 15.105 | 15.443 | 15.917 | 16.479 | 17.102 | 17.768 | 18.468 | 19.192 | 19.936 |
| 3 | 15.000 | 15.018 | 15.358 | 15.939 | 16.651 | 17.445 | 18.294 | 19.182 | 20.097 | 21.033 | 21.985 |
| 4 | 15.000 | 15.104 | 15.652 | 16.434 | 17.341 | 18.323 | 19.355 | 20.421 | 21.511 | 22.617 | 23.736 |
| 5 | 15.000 | 15.224 | 15.954 | 16.908 | 17.981 | 19.123 | 20.310 | 21.528 | 22.766 | 24.018 | 25.280 |
| 6 | 15.000 | 15.361 | 16.251 | 17.357 | 18.574 | 19.857 | 21.181 | 22.531 | 23.900 | 25.280 | 26.667 |
| 7 | 15.000 | 15.505 | 16.538 | 17.779 | 19.127 | 20.535 | 21.982 | 23.452 | 24.937 | 26.432 | 27.932 |
| 8 | 15.003 | 15.651 | 16.814 | 18.178 | 19.644 | 21.167 | 22.725 | 24.304 | 25.896 | 27.495 | 29.097 |
| 9 | 15.018 | 15.796 | 17.079 | 18.556 | 20.131 | 21.759 | 23.420 | 25.099 | 26.789 | 28.484 | 30.179 |
| 10 | 15.040 | 15.939 | 17.332 | 18.915 | 20.590 | 22.316 | 24.072 | 25.844 | 27.625 | 29.408 | 31.190 |
| 11 | 15.069 | 16.080 | 17.575 | 19.256 | 21.025 | 22.843 | 24.687 | 26.547 | 28.412 | 30.277 | 32.139 |
| 12 | 15.101 | 16.217 | 17.809 | 19.581 | 21.439 | 23.342 | 25.271 | 27.211 | 29.156 | 31.098 | 33.035 |
| 12 | 15.251 | 16.728 | 18.655 | 20.747 | 22.915 | 25.120 | 27.340 | 29.564 | 31.784 | 33.995 | 36.192 |
| 13 | 15.136 | 16.350 | 18.033 | 19.891 | 21.833 | 23.817 | 25.825 | 27.842 | 29.861 | 31.876 | 33.884 |
| 14 | 15.173 | 16.480 | 18.248 | 20.188 | 22.209 | 24.271 | 26.353 | 28.442 | 30.532 | 32.616 | 34.690 |
| 15 | 15.212 | 16.606 | 18.455 | 20.473 | 22.570 | 24.704 | 26.857 | 29.016 | 31.172 | 33.321 | 35.458 |
| 15.291 | 16.847 | 18.847 | 21.011 | 23.247 | 25.519 | 27.803 | 30.090 | 32.370 | 34.640 | 36.894 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 15.331 | 16.962 | 19.033 | 21.265 | 23.567 | 25.902 | 28.248 | 30.595 | 32.933 | 35.259 | 37.568 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 15.371 | 17.074 | 19.213 | 21.510 | 23.876 | 26.271 | 28.676 | 31.080 | 33.475 | 35.854 | 38.214 |
| 20 | 15.411 | 17.183 | 19.387 | 21.746 | 24.173 | 26.627 | 29.089 | 31.548 | 33.996 | 36.427 | 38.836 |
| 21 | 15.450 | 17.288 | 19.555 | 21.975 | 24.460 | 26.971 | 29.488 | 32.000 | 34.499 | 36.979 | 39.436 |
| 22 | 15.490 | 17.391 | 19.719 | 22.197 | 24.738 | 27.303 | 29.873 | 32.436 | 34.984 | 37.512 | 40.013 |
| 23 | 15.528 | 17.491 | 19.877 | 22.412 | 25.007 | 27.624 | 30.245 | 32.858 | 35.453 | 38.026 | 40.571 |
| 24 | 15.567 | 17.588 | 20.030 | 22.619 | 25.267 | 27.936 | 30.606 | 33.266 | 35.907 | 38.524 | 41.111 |
| 25 | 15.604 | 17.683 | 20.180 | 22.821 | 25.520 | 28.238 | 30.955 | 33.661 | 36.347 | 39.005 | 41.632 |
| 26 | 15.641 | 17.775 | 20.325 | 23.017 | 25.765 | 28.530 | 31.295 | 34.045 | 36.773 | 39.472 | 42.137 |
| 27 | 15.678 | 17.865 | 20.466 | 23.208 | 26.003 | 28.815 | 31.624 | 34.417 | 37.186 | 39.925 | 42.627 |
| 28 | 15.714 | 17.952 | 20.603 | 23.393 | 26.234 | 29.091 | 31.944 | 34.779 | 37.587 | 40.364 | 43.102 |
| 29 | 15.749 | 18.038 | 20.737 | 23.573 | 26.460 | 29.360 | 32.255 | 35.130 | 37.977 | 40.790 | 43.562 |
| 20 | 15.784 | 18.121 | 20.867 | 23.748 | 26.679 | 29.622 | 32.557 | 35.472 | 38.356 | 41.204 | 44.010 |

Table B. 42
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 110 / \text { Dividend Rate }=3 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 10.000 | 10.006 | 10.153 | 10.427 | 10.780 | 11.186 | 11.631 | 12.105 | 12.599 | 13.109 | 13.632 |
| 2 | 10.000 | 10.190 | 10.644 | 11.225 | 11.878 | 12.577 | 13.307 | 14.059 | 14.826 | 15.606 | 16.394 |
| 3 | 10.023 | 10.457 | 11.147 | 11.953 | 12.824 | 13.735 | 14.671 | 15.625 | 16.592 | 17.567 | 18.548 |
| 4 | 10.095 | 10.733 | 11.614 | 12.603 | 13.650 | 14.732 | 15.836 | 16.955 | 18.083 | 19.218 | 20.357 |
| 5 | 10.188 | 11.000 | 12.044 | 13.189 | 14.386 | 15.614 | 16.862 | 18.121 | 19.389 | 20.660 | 21.934 |
| 6 | 10.290 | 11.255 | 12.441 | 13.722 | 15.052 | 16.409 | 17.784 | 19.168 | 20.558 | 21.950 | 23.343 |
| 7 | 10.395 | 11.495 | 12.809 | 14.213 | 15.661 | 17.135 | 18.624 | 20.121 | 21.621 | 23.122 | 24.621 |
| 8 | 10.499 | 11.722 | 13.152 | 14.667 | 16.225 | 17.805 | 19.398 | 20.998 | 22.598 | 24.198 | 25.794 |
| 9 | 10.601 | 11.937 | 13.474 | 15.092 | 16.750 | 18.429 | 20.118 | 21.812 | 23.505 | 25.195 | 26.881 |
| 10 | 10.701 | 12.141 | 13.777 | 15.491 | 17.242 | 19.012 | 20.791 | 22.572 | 24.351 | 26.126 | 27.895 |
| 11 | 10.797 | 12.335 | 14.063 | 15.866 | 17.705 | 19.561 | 21.424 | 23.287 | 25.146 | 27.000 | 28.846 |
| 12 | 10.891 | 12.519 | 14.334 | 16.222 | 18.143 | 20.080 | 22.021 | 23.961 | 25.897 | 27.824 | 29.742 |
| 16 | 11.234 | 13.178 | 15.297 | 17.482 | 19.692 | 21.911 | 24.129 | 26.340 | 28.540 | 30.726 | 32.894 |
| 13 | 10.981 | 12.695 | 14.592 | 16.559 | 18.559 | 20.571 | 22.587 | 24.600 | 26.607 | 28.605 | 30.590 |
| 14 | 11.069 | 12.863 | 14.838 | 16.881 | 18.954 | 21.039 | 23.125 | 25.208 | 27.282 | 29.346 | 31.395 |
| 15 | 11.153 | 13.024 | 15.073 | 17.188 | 19.332 | 21.485 | 23.638 | 25.787 | 27.925 | 30.051 | 32.162 |
| 1.313 | 13.326 | 15.513 | 17.764 | 20.038 | 22.320 | 24.599 | 26.870 | 29.129 | 31.371 | 33.594 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 11.389 | 13.469 | 15.721 | 18.034 | 20.370 | 22.712 | 25.051 | 27.379 | 29.693 | 31.989 | 34.265 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 11.462 | 13.606 | 15.920 | 18.294 | 20.690 | 23.090 | 25.485 | 27.868 | 30.236 | 32.584 | 34.909 |
| 20 | 11.534 | 13.739 | 16.113 | 18.545 | 20.997 | 23.453 | 25.903 | 28.339 | 30.758 | 33.155 | 35.528 |
| 21 | 11.602 | 13.867 | 16.298 | 18.786 | 21.294 | 23.804 | 26.306 | 28.793 | 31.261 | 33.706 | 36.124 |
| 22 | 11.669 | 13.990 | 16.477 | 19.020 | 21.580 | 24.142 | 26.695 | 29.231 | 31.747 | 34.237 | 36.699 |
| 23 | 11.734 | 14.110 | 16.650 | 19.245 | 21.858 | 24.470 | 27.071 | 29.655 | 32.216 | 34.750 | 37.254 |
| 24 | 11.796 | 14.225 | 16.817 | 19.463 | 22.126 | 24.787 | 27.435 | 30.065 | 32.670 | 35.246 | 37.790 |
| 25 | 11.857 | 14.337 | 16.979 | 19.675 | 22.386 | 25.094 | 27.788 | 30.462 | 33.109 | 35.726 | 38.309 |
| 26 | 11.916 | 14.446 | 17.137 | 19.880 | 22.638 | 25.391 | 28.130 | 30.846 | 33.535 | 36.191 | 38.811 |
| 27 | 11.973 | 14.551 | 17.289 | 20.079 | 22.882 | 25.680 | 28.462 | 31.220 | 33.948 | 36.642 | 39.298 |
| 28 | 12.029 | 14.653 | 17.437 | 20.272 | 23.120 | 25.961 | 28.784 | 31.582 | 34.349 | 37.079 | 39.769 |
| 29 | 12.083 | 14.752 | 17.581 | 20.460 | 23.351 | 26.234 | 29.097 | 31.934 | 34.738 | 37.504 | 40.227 |
| 20 | 12.135 | 14.848 | 17.721 | 20.643 | 23.575 | 26.499 | 29.402 | 32.277 | 35.116 | 37.916 | 40.672 |

Table B. 43
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 105 / \text { Dividend Rate }=3 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 5.131 | 5.483 | 5.924 | 6.413 | 6.928 | 7.461 | 8.005 | 8.558 | 9.116 | 9.679 | 10.245 |
| 2 | 5.447 | 6.093 | 6.813 | 7.570 | 8.348 | 9.137 | 9.934 | 10.736 | 11.542 | 12.351 | 13.160 |
| 3 | 5.743 | 6.601 | 7.524 | 8.477 | 9.446 | 10.425 | 11.410 | 12.398 | 13.388 | 14.379 | 15.370 |
| 4 | 6.007 | 7.036 | 8.124 | 9.237 | 10.365 | 11.500 | 12.639 | 13.780 | 14.921 | 16.062 | 17.201 |
| 5 | 6.244 | 7.419 | 8.648 | 9.900 | 11.164 | 12.433 | 13.706 | 14.979 | 16.251 | 17.521 | 18.789 |
| 6 | 6.459 | 7.762 | 9.116 | 10.491 | 11.876 | 13.266 | 14.656 | 16.046 | 17.434 | 18.819 | 20.200 |
| 7 | 6.656 | 8.074 | 9.541 | 11.027 | 12.522 | 14.019 | 15.517 | 17.013 | 18.506 | 19.994 | 21.478 |
| 8 | 6.837 | 8.361 | 9.931 | 11.519 | 13.114 | 14.711 | 16.307 | 17.900 | 19.489 | 21.072 | 22.648 |
| 9 | 7.005 | 8.626 | 10.291 | 11.974 | 13.662 | 15.351 | 17.038 | 18.721 | 20.398 | 22.069 | 23.731 |
| 10 | 7.161 | 8.873 | 10.628 | 12.398 | 14.173 | 15.948 | 17.720 | 19.487 | 21.246 | 22.998 | 24.740 |
| 11 | 7.308 | 9.104 | 10.943 | 12.795 | 14.652 | 16.508 | 18.360 | 20.205 | 22.042 | 23.870 | 25.686 |
| 12 | 7.446 | 9.322 | 11.239 | 13.170 | 15.104 | 17.036 | 18.963 | 20.882 | 22.792 | 24.691 | 26.577 |
| 16 | 7.928 | 10.084 | 12.279 | 14.486 | 16.693 | 18.895 | 21.087 | 23.266 | 25.430 | 27.578 | 29.706 |
| 13 | 7.576 | 9.528 | 11.519 | 13.524 | 15.531 | 17.536 | 19.534 | 21.523 | 23.502 | 25.468 | 27.420 |
| 14 | 7.700 | 9.723 | 11.785 | 13.860 | 15.937 | 18.010 | 20.076 | 22.132 | 24.176 | 26.205 | 28.219 |
| 15 | 7.817 | 9.908 | 12.038 | 14.180 | 16.324 | 18.463 | 20.593 | 22.712 | 24.817 | 26907 | 28.980 |
| 16 | 8.034 | 10.252 | 12.510 | 14.778 | 17.046 | 19.308 | 21.559 | 23.796 | 26.017 | 28.219 | 30.400 |


| 18 | 8.135 | 10.413 | 12.731 | 15.059 | 17.385 | 19.705 | 22.012 | 24.305 | 26.579 | 28.834 | 31.065 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 8.232 | 10.568 | 12.943 | 15.328 | 17.711 | 20.086 | 22.448 | 24.794 | 27.120 | 29.424 | 31.704 |
| 20 | 8.325 | 10.716 | 13.146 | 15.587 | 18.025 | 20.453 | 22.867 | 25.264 | 27.640 | 29 | 992 |
| 32.318 |  |  |  |  |  |  |  |  |  |  |  |
| 21 | 8.414 | 10.858 | 13.342 | 15.836 | 18.327 | 20.807 | 23.272 | 25.717 | 28.141 | 30.539 | 32.909 |
| 22 | 8.499 | 10.995 | 13.532 | 16.077 | 18.618 | 21.148 | 23.662 | 26.155 | 28.624 | 31.066 | 33.478 |
| 23 | 8.581 | 11.128 | 13.714 | 16.309 | 18.900 | 21.478 | 24.039 | 26.578 | 29.091 | 31.575 | 34.028 |
| 24 | 8.660 | 11.255 | 13.890 | 16.534 | 19.173 | 21.798 | 24.404 | 26.987 | 29.542 | 32.068 | 34.559 |
| 25 | 8.736 | 11.378 | 14.061 | 16.752 | 19.437 | 22.107 | 24.757 | 27.383 | 29.979 | 32.544 | 35.073 |
| 26 | 8.809 | 11.497 | 14.226 | 16.963 | 19.692 | 22.407 | 25.100 | 27.766 | 30.403 | 33.005 | 35.570 |
| 27 | 8.880 | 11.613 | 14.386 | 17.167 | 19.941 | 22.698 | 25.432 | 28.139 | 30.813 | 33.452 | 36.052 |
| 28 | 8.949 | 11.725 | 14.542 | 17.366 | 20.182 | 22.980 | 25.755 | 28.500 | 31.212 | 33.886 | 36.519 |
| 29 | 9.015 | 11.833 | 14.692 | 17.559 | 20.416 | 23.254 | 26.068 | 28.851 | 31.599 | 34.307 | 36.973 |
| 30 | 9.079 | 11.938 | 14.839 | 17.746 | 20.643 | 23.521 | 26.373 | 29.192 | 31.975 | 34.716 | 37.413 |

Table B. 44
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 100 /$ Dividend Rate $=\mathbf{3 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 1.615 | 2.187 | 2.760 | 3.333 | 3.905 | 4.478 | 5.051 | 5.623 | 6.195 | 6.767 | 7.339 |
| 2 | 2.222 | 3.026 | 3.832 | 4.638 | 5.445 | 6.251 | 7.056 | 7.861 | 8.665 | 9.468 | 10.271 |
| 3 | 2.664 | 3.644 | 4.627 | 5.610 | 6.593 | 7.575 | 8.557 | 9.537 | 10.516 | 11.494 | 12.470 |
| 4 | 3.022 | 4.149 | 5.278 | 6.409 | 7.539 | 8.668 | 9.795 | 10.922 | 12.046 | 13.167 | 14.286 |
| 5 | 3.327 | 4.580 | 5.838 | 7.096 | 8.354 | 9.611 | 10.866 | 12.119 | 13.368 | 14.615 | 15.858 |
| 6 | 3.593 | 4.960 | 6.332 | 7.706 | 9.078 | 10.449 | 11.817 | 13.182 | 14.544 | 15.901 | 17.254 |
| 7 | 3.831 | 5.302 | 6.778 | 8.255 | 9.732 | 11.206 | 12.677 | 14.144 | 15.607 | 17.064 | 18.516 |
| 8 | 4.046 | 5.612 | 7.184 | 8.758 | 10.330 | 11.899 | 13.465 | 15.026 | 16.581 | 18.130 | 19.672 |
| 9 | 4.243 | 5.897 | 7.559 | 9.221 | 10.883 | 12.541 | 14.194 | 15.842 | 17.483 | 19.116 | 20.741 |
| 10 | 4.425 | 6.162 | 7.907 | 9.653 | 11.397 | 13.138 | 14.873 | 16.602 | 18.323 | 20.035 | 21.737 |
| 11 | 4.594 | 6.409 | 8.232 | 10.057 | 11.880 | 13.698 | 15.510 | 17.315 | 19.111 | 20.896 | 22.671 |
| 12 | 4.751 | 6.640 | 8.538 | 10.437 | 12.334 | 14.226 | 16.111 | 17.987 | 19.853 | 21.708 | 23.550 |
| 13 | 4.899 | 6.858 | 8.826 | 10.797 | 12.764 | 14.725 | 16.679 | 18.623 | 20.555 | 22.475 | 24.381 |
| 14 | 5.039 | 7.064 | 9.100 | 11.137 | 13.172 | 15.199 | 17.218 | 19.227 | 21.222 | 23.204 | 25.170 |
| 15 | 5.170 | 7.259 | 9.360 | 11.462 | 13.560 | 15.651 | 17.732 | 19.802 | 21.857 | 23.897 | 25.920 |
| 16 | 5.295 | 7.445 | 9.607 | 11.771 | 13.930 | 16.082 | 18.223 | 20.351 | 22.464 | 24.559 | 26.636 |
| 17 | 5.413 | 7.622 | 9.844 | 12.067 | 14.285 | 16.495 | 18.693 | 20.877 | 23.044 | 25.193 | 27.321 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 5.526 | 7.791 | 10.070 | 12.350 | 14.625 | 16.891 | 19.143 | 21.381 | 23.600 | 25.800 | 27.977 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 5.634 | 7.953 | 10.287 | 12.622 | 14.952 | 17.271 | 19.576 | 21.865 | 24.135 | 26.383 | 28.607 |
| 20 | 5.737 | 8.109 | 10.496 | 12.884 | 15.266 | 17.637 | 19.993 | 22.331 | 24.649 | 26.943 | 29.212 |
| 21 | 5.836 | 8.258 | 10.697 | 13.136 | 15.569 | 17.990 | 20.395 | 22.781 | 25.144 | 27.483 | 29.795 |
| 22 | 5.930 | 8.402 | 10.890 | 13.379 | 15.861 | 18.330 | 20.782 | 23.214 | 25.622 | 28.004 | 30.357 |
| 23 | 6.021 | 8.540 | 11.077 | 13.614 | 16.144 | 18.659 | 21.157 | 23.633 | 26.084 | 28.507 | 30.899 |
| 24 | 6.108 | 8.674 | 11.257 | 13.841 | 16.417 | 18.978 | 21.520 | 24.038 | 26.531 | 28.993 | 31.423 |
| 25 | 6.193 | 8.803 | 11.431 | 14.061 | 16.681 | 19.286 | 21.871 | 24.431 | 26.963 | 29.464 | 31.930 |
| 26 | 6.274 | 8.927 | 11.600 | 14.274 | 16.937 | 19.585 | 22.211 | 24.811 | 27.382 | 29.919 | 32.420 |
| 27 | 6.352 | 9.048 | 11.764 | 14.480 | 17.186 | 19.875 | 22.541 | 25.180 | 27.788 | 30.361 | 32.896 |
| 28 | 6.427 | 9.164 | 11.922 | 14.680 | 17.427 | 20.156 | 22.861 | 25.538 | 28.182 | 30.789 | 33.356 |
| 29 | 6.500 | 9.278 | 12.076 | 14.875 | 17.662 | 20.430 | 23.173 | 25.886 | 28.565 | 31.205 | 33.803 |
| 20 | 6.571 | 9.387 | 12.226 | 15.064 | 17.890 | 20.696 | 23.476 | 26.224 | 28.937 | 31.609 | 34.238 |

Table B. 45
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 95 / \text { Dividend Rate }=3 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.219 | 0.535 | 0.931 | 1.375 | 1.849 | 2.343 | 2.850 | 3.366 | 3.890 | 4.419 | 4.952 |
| 2 | 0.585 | 1.162 | 1.815 | 2.510 | 3.229 | 3.965 | 4.710 | 5.463 | 6.221 | 6.983 | 7.746 |
| 3 | 0.915 | 1.684 | 2.524 | 3.402 | 4.302 | 5.215 | 6.138 | 7.066 | 7.998 | 8.932 | 9.868 |
| 4 | 1.207 | 2.132 | 3.124 | 4.151 | 5.199 | 6.260 | 7.328 | 8.401 | 9.476 | 10.553 | 11.630 |
| 5 | 1.468 | 2.525 | 3.648 | 4.805 | 5.981 | 7.169 | 8.363 | 9.561 | 10.760 | 11.960 | 13.158 |
| 6 | 1.704 | 2.878 | 4.117 | 5.389 | 6.679 | 7.979 | 9.285 | 10.594 | 11.904 | 13.212 | 14.518 |
| 7 | 1.919 | 3.199 | 4.543 | 5.919 | 7.312 | 8.714 | 10.122 | 11.532 | 12.940 | 14.347 | 15.749 |
| 8 | 2.117 | 3.494 | 4.934 | 6.405 | 7.893 | 9.389 | 10.890 | 12.392 | 13.891 | 15.387 | 16.878 |
| 9 | 2.301 | 3.767 | 5.296 | 6.855 | 8.431 | 10.015 | 11.602 | 13.188 | 14.772 | 16.350 | 17.923 |
| 10 | 2.472 | 4.021 | 5.633 | 7.276 | 8.933 | 10.599 | 12.266 | 13.932 | 15.593 | 17.248 | 18.896 |
| 11 | 2.632 | 4.260 | 5.950 | 7.670 | 9.405 | 11.147 | 12.889 | 14.629 | 16.364 | 18.091 | 19.809 |
| 12 | 2.782 | 4.484 | 6.248 | 8.042 | 9.850 | 11.663 | 13.477 | 15.287 | 17.090 | 18.885 | 20.670 |
| 13 | 2.925 | 4.696 | 6.530 | 8.394 | 10.271 | 12.153 | 14.034 | 15.910 | 17.778 | 19.637 | 21.483 |
| 14 | 3.059 | 4.897 | 6.798 | 8.728 | 10.671 | 12.618 | 14.563 | 16.502 | 18.432 | 20.350 | 22.256 |
| 15 | 3.187 | 5.089 | 7.053 | 9.046 | 11.052 | 13.061 | 15.067 | 17.066 | 19.054 | 21.030 | 22.991 |
| 16 | 3.308 | 5.271 | 7.296 | 9.350 | 11.416 | 13.485 | 15.549 | 17.605 | 19.649 | 21.679 | 23.692 |
| 17 | 3.424 | 5.445 | 7.529 | 9.641 | 11.765 | 13.890 | 16.010 | 18.121 | 20.218 | 22.300 | 24.364 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 3.535 | 5.612 | 7.752 | 9.920 | 12.100 | 14.280 | 16.453 | 18.616 | 20.764 | 22.895 | 25.007 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 3.641 | 5.772 | 7.966 | 10.188 | 12.421 | 14.654 | 16.879 | 19.091 | 21.289 | 23.467 | 25.624 |
| 20 | 3.742 | 5.925 | 8.172 | 10.447 | 12.731 | 15.014 | 17.288 | 19.550 | 21.794 | 24.017 | 26.218 |
| 21 | 3.840 | 6.073 | 8.371 | 10.695 | 13.030 | 15.361 | 17.683 | 19.991 | 22.280 | 24.547 | 26.790 |
| 22 | 3.934 | 6.216 | 8.562 | 10.935 | 13.318 | 15.697 | 18.065 | 20.417 | 22.750 | 25.059 | 27.341 |
| 23 | 4.024 | 6.353 | 8.747 | 11.168 | 13.596 | 16.021 | 18.434 | 20.829 | 23.203 | 25.553 | 27.873 |
| 24 | 4.111 | 6.485 | 8.925 | 11.392 | 13.866 | 16.335 | 18.790 | 21.228 | 23.642 | 26.030 | 28.388 |
| 25 | 4.195 | 6.614 | 9.098 | 11.609 | 14.127 | 16.639 | 19.136 | 21.614 | 24.067 | 26.492 | 28.885 |
| 26 | 4.275 | 6.738 | 9.266 | 11.820 | 14.380 | 16.933 | 19.471 | 21.988 | 24.479 | 26.940 | 29.367 |
| 27 | 4.354 | 6858 | 9.428 | 12.024 | 14.626 | 17.219 | 19.796 | 22.351 | 24.878 | 27.373 | 29.833 |
| 28 | 4.429 | 6.974 | 9.585 | 12.223 | 14.865 | 17.497 | 20.112 | 22.703 | 25.266 | 27.794 | 30.286 |
| 29 | 4.502 | 7.087 | 9.738 | 12.415 | 15.097 | 17.767 | 20.419 | 23.046 | 25.642 | 28.203 | 30.725 |

Table B. 46
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 90 /$ Dividend Rate $=\mathbf{3 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.009 | 0.066 | 0.204 | 0.420 | 0.701 | 1.032 | 1.401 | 1.800 | 2.222 | 2.661 | 3.114 |
| 2 | 0.084 | 0.318 | 0.691 | 1.164 | 1.707 | 2.298 | 2.923 | 3.573 | 4.241 | 4.924 | 5.618 |
| 3 | 0.211 | 0.620 | 1.187 | 1.856 | 2.591 | 3.371 | 4.181 | 5.013 | 5.861 | 6.721 | 7.589 |
| 4 | 0.357 | 0.921 | 1.650 | 2.479 | 3.370 | 4.303 | 5.264 | 6.244 | 7.237 | 8.241 | 9.251 |
| 5 | 0.509 | 1.210 | 2.078 | 3.043 | 4.068 | 5.132 | 6.221 | 7.328 | 8.446 | 9.573 | 10.705 |
| 6 | 0.660 | 1.484 | 2.474 | 3.559 | 4.702 | 5.881 | 7.084 | 8.302 | 9.531 | 10.767 | 12.007 |
| 7 | 0.807 | 1.742 | 2.843 | 4.036 | 5.284 | 6.567 | 7.872 | 9.192 | 10.520 | 11.854 | 13.190 |
| 8 | 0.949 | 1.986 | 3.187 | 4.479 | 5.824 | 7.202 | 8.600 | 10.012 | 11.431 | 12.854 | 14.277 |
| 9 | 1.086 | 2.217 | 3.510 | 4.893 | 6.327 | 7.793 | 9.278 | 10.774 | 12.277 | 13.782 | 15.286 |
| 10 | 1.218 | 2.436 | 3.815 | 5.282 | 6.800 | 8.347 | 9.912 | 11.488 | 13.068 | 14.649 | 16.227 |
| 11 | 1.344 | 2.644 | 4.104 | 5.650 | 7.245 | 8.869 | 10.510 | 12.159 | 13.812 | 15.464 | 17.112 |
| 12 | 1.465 | 2.842 | 4.378 | 5.999 | 7.667 | 9.363 | 11.074 | 12.794 | 14.515 | 16.233 | 17.946 |
| 13 | 1.582 | 3.031 | 4.639 | 6.330 | 8.068 | 9.832 | 11.611 | 13.395 | 15.181 | 16.962 | 18.735 |
| 14 | 1.694 | 3.211 | 4.887 | 6.646 | 8.450 | 10.279 | 12.121 | 13.968 | 15.814 | 17.654 | 19.485 |
| 15 | 1.801 | 3.384 | 5.125 | 6.948 | 8.815 | 10.705 | 12.608 | 14.515 | 16.418 | 18.314 | 20.200 |
| 17 | 2.005 | 3.710 | 5.573 | 7.515 | 9.499 | 11.505 | 13.521 | 15.538 | 17.549 | 19.549 | 21.536 |
| 1.905 | 3.551 | 5.354 | 7.237 | 9.164 | 11.114 | 13.074 | 15.037 | 16.995 | 18.945 | 20.883 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 2.101 | 3.864 | 5.783 | 7.781 | 9.821 | 11.882 | 13.951 | 16.019 | 18.080 | 20.128 | 22.162 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 2.193 | 4.012 | 5.986 | 8.038 | 10.131 | 12.244 | 14.364 | 16.481 | 18.590 | 20.685 | 22.764 |
| 20 | 2.283 | 4.155 | 6.182 | 8.286 | 10.430 | 12.593 | 14.762 | 16.927 | 19.082 | 21.222 | 23.343 |
| 21 | 2.369 | 4.292 | 6.371 | 8.525 | 10.719 | 12.930 | 15.146 | 17.357 | 19.556 | 21.738 | 23.900 |
| 22 | 2.453 | 4.426 | 6.553 | 8.757 | 10.998 | 13.256 | 15.518 | 17.772 | 20.014 | 22.237 | 24.438 |
| 23 | 2.534 | 4.555 | 6.730 | 8.980 | 11.268 | 13.571 | 15.877 | 18.174 | 20.456 | 22.719 | 24.957 |
| 24 | 2.612 | 4.679 | 6.901 | 9.197 | 11.530 | 13.877 | 16.224 | 18.562 | 20.884 | 23.185 | 25.459 |
| 25 | 2.688 | 4.800 | 7.067 | 9.407 | 11.783 | 14.173 | 16.561 | 18.939 | 21.299 | 23.636 | 25.945 |
| 26 | 2.762 | 4.918 | 7.228 | 9.611 | 12.029 | 14.460 | 16.888 | 19.304 | 21.701 | 24.073 | 26.416 |
| 27 | 2.834 | 5.032 | 7.384 | 9.809 | 12.268 | 14.739 | 17.206 | 19.659 | 22.091 | 24.497 | 26.872 |
| 28 | 2.903 | 5.142 | 7.536 | 10.002 | 12.501 | 15.010 | 17.514 | 20.003 | 22.470 | 24.908 | 27.314 |
| 29 | 2.970 | 5.250 | 7.683 | 10.189 | 12.727 | 15.274 | 17.814 | 20.338 | 22.838 | 25.308 | 27.743 |
| 20 | 3.036 | 5.354 | 7.827 | 10.371 | 12.946 | 15.530 | 18.106 | 20.663 | 23.195 | 25.696 | 28.160 |

Table B. 47
American-Style Put Premiums as a Function of Time and Volatility

$$
\text { Stock Price }=\$ 100 / \text { Strike Price }=\$ 85 / \text { Dividend Rate }=3 \%
$$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.003 | 0.026 | 0.087 | 0.200 | 0.366 | 0.580 | 0.836 | 1.128 | 1.450 | 1.797 |
| 2 | 0.006 | 0.057 | 0.199 | 0.445 | 0.781 | 1.191 | 1.658 | 2.169 | 2.716 | 3.291 | 3.888 |
| 3 | 0.029 | 0.171 | 0.463 | 0.888 | 1.415 | 2.017 | 2.676 | 3.377 | 4.110 | 4.868 | 5.645 |
| 4 | 0.073 | 0.321 | 0.757 | 1.339 | 2.025 | 2.786 | 3.601 | 4.455 | 5.339 | 6.244 | 7.166 |
| 5 | 0.130 | 0.487 | 1.056 | 1.776 | 2.600 | 3.497 | 4.445 | 5.429 | 6.440 | 7.470 | 8.515 |
| 6 | 0.198 | 0.661 | 1.350 | 2.193 | 3.139 | 4.155 | 5.220 | 6.318 | 7.441 | 8.582 | 9.735 |
| 7 | 0.273 | 0.836 | 1.635 | 2.590 | 3.645 | 4.768 | 5.937 | 7.138 | 8.362 | 9.601 | 10.851 |
| 8 | 0.352 | 1.010 | 1.911 | 2.967 | 4.122 | 5.342 | 6.607 | 7.901 | 9.216 | 10.544 | 11.882 |
| 9 | 0.432 | 1.180 | 2.176 | 3.326 | 4.572 | 5.882 | 7.234 | 8.614 | 10.013 | 11.424 | 12.842 |
| 10 | 0.514 | 1.347 | 2.431 | 3.667 | 4.999 | 6.392 | 7.825 | 9.285 | 10.761 | 12.248 | 13.741 |
| 11 | 0.596 | 1.509 | 2.676 | 3.994 | 5.405 | 6.876 | 8.385 | 9.919 | 11.468 | 13.026 | 14.587 |
| 12 | 0.678 | 1.667 | 2.911 | 4.306 | 5.792 | 7.336 | 8.916 | 10.520 | 12.137 | 13.761 | 15.387 |
| 13 | 0.758 | 1.820 | 3.138 | 4.605 | 6.162 | 7.774 | 9.422 | 11.091 | 12.772 | 14.459 | 16.146 |
| 14 | 0.838 | 1.969 | 3.356 | 4.892 | 6.516 | 8.194 | 9.905 | 11.636 | 13.378 | 15.124 | 16.868 |
| 15 | 0.916 | 2.113 | 3.567 | 5.168 | 6.855 | 8.595 | 10.367 | 12.158 | 13.957 | 15.759 | 17.557 |
| 17 | 0.993 | 2.253 | 3.770 | 5.433 | 7.182 | 8.981 | 10.811 | 12.658 | 14.512 | 16.366 | 18.215 |
| 1.068 | 2.388 | 3.967 | 5.689 | 7.496 | 9.352 | 11.237 | 13.137 | 15.044 | 16.949 | 18.846 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 1.142 | 2.520 | 4.157 | 5.936 | 7.798 | 9.709 | 11.647 | 13.599 | 15.555 | 17.508 | 19.451 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 1.214 | 2.648 | 4.341 | 6.175 | 8.091 | 10.053 | 12.042 | 14.043 | 16.047 | 18.046 | 20.033 |
| 20 | 1.284 | 2.772 | 4.519 | 6.406 | 8.373 | 10.386 | 12.424 | 14.472 | 16.522 | 18.564 | 20.593 |
| 21 | 1.353 | 2.893 | 4.692 | 6.630 | 8.647 | 10.708 | 12.792 | 14.886 | 16.979 | 19.064 | 21.134 |
| 22 | 1.420 | 3.011 | 4.859 | 6.847 | 8.911 | 11.019 | 13.149 | 15.287 | 17.422 | 19.546 | 21.655 |
| 23 | 1.486 | 3.125 | 5.022 | 7.057 | 9.168 | 11.321 | 13.494 | 15.674 | 17.850 | 20.013 | 22.158 |
| 24 | 1.550 | 3.236 | 5.180 | 7.261 | 9.417 | 11.613 | 13.829 | 16.050 | 18.264 | 20.465 | 22.645 |
| 25 | 1.612 | 3.344 | 5.334 | 7.459 | 9.659 | 11.897 | 14.154 | 16.414 | 18.666 | 20.902 | 23.117 |
| 26 | 1.673 | 3.450 | 5.483 | 7.652 | 9.894 | 12.173 | 14.470 | 16.767 | 19.055 | 21.326 | 23.574 |
| 27 | 1.733 | 3.552 | 5.629 | 7.840 | 10.122 | 12.442 | 14.776 | 17.111 | 19.434 | 21.738 | 24.017 |
| 28 | 1.791 | 3.652 | 5.771 | 8.022 | 10.345 | 12.703 | 15.074 | 17.444 | 19.801 | 22.137 | 24.447 |
| 29 | 1.848 | 3.750 | 5.909 | 8.200 | 10.561 | 12.956 | 15.364 | 17.768 | 20.158 | 22.525 | 24.864 |
| 20 | 1.904 | 3.845 | 6.044 | 8.374 | 10.772 | 13.204 | 15.647 | 18.084 | 20.506 | 22.903 | 25.270 |

Table B. 48
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 80 /$ Dividend Rate $=\mathbf{3 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.002 | 0.011 | 0.040 | 0.099 | 0.194 | 0.326 | 0.495 | 0.699 | 0.933 |
| 2 | 0.000 | 0.006 | 0.041 | 0.134 | 0.299 | 0.538 | 0.842 | 1.204 | 1.613 | 2.062 | 2.543 |
| 3 | 0.003 | 0.033 | 0.144 | 0.362 | 0.685 | 1.099 | 1.588 | 2.137 | 2.734 | 3.369 | 4.034 |
| 4 | 0.010 | 0.086 | 0.292 | 0.640 | 1.110 | 1.679 | 2.324 | 3.028 | 3.778 | 4.564 | 5.378 |
| 5 | 0.024 | 0.159 | 0.466 | 0.938 | 1.542 | 2.246 | 3.026 | 3.863 | 4.743 | 5.657 | 6.596 |
| 6 | 0.044 | 0.246 | 0.655 | 1.242 | 1.966 | 2.791 | 3.690 | 4.644 | 5.639 | 6.664 | 7.713 |
| 7 | 0.072 | 0.344 | 0.850 | 1.545 | 2.379 | 3.312 | 4.318 | 5.376 | 6.473 | 7.598 | 8.744 |
| 8 | 0.104 | 0.448 | 1.047 | 1.842 | 2.776 | 3.809 | 4.912 | 6.065 | 7.254 | 8.470 | 9.705 |
| 9 | 0.141 | 0.557 | 1.244 | 2.132 | 3.159 | 4.283 | 5.475 | 6.715 | 7.989 | 9.288 | 10.603 |
| 10 | 0.181 | 0.667 | 1.439 | 2.414 | 3.528 | 4.736 | 6.011 | 7.331 | 8.684 | 10.059 | 11.449 |
| 11 | 0.224 | 0.779 | 1.631 | 2.687 | 3.882 | 5.170 | 6.521 | 7.917 | 9.342 | 10.789 | 12.248 |
| 12 | 0.269 | 0.891 | 1.819 | 2.953 | 4.223 | 5.585 | 7.009 | 8.475 | 9.969 | 11.481 | 13.006 |
| 13 | 0.315 | 1.003 | 2.002 | 3.210 | 4.552 | 5.984 | 7.476 | 9.008 | 10.566 | 12.141 | 13.726 |
| 14 | 0.363 | 1.113 | 2.182 | 3.459 | 4.869 | 6.367 | 7.923 | 9.518 | 11.137 | 12.771 | 14.413 |
| 15 | 0.411 | 1.223 | 2.358 | 3.700 | 5.175 | 6.736 | 8.354 | 10.007 | 11.684 | 13.374 | 15.070 |
| 16 | 0.460 | 1.330 | 2.529 | 3.934 | 5.471 | 7.092 | 8.768 | 10.478 | 12.209 | 13.952 | 15.699 |
| 17 | 0.509 | 1.437 | 2.696 | 4.162 | 5.757 | 7.436 | 9.167 | 10.931 | 12.714 | 14.507 | 16.303 |


| 18 | 0.558 | 1.541 | 2.858 | 4.382 | 6.035 | 7.768 | 9.552 | 11.367 | 13.200 | 15.042 | 16.883 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.607 | 1.644 | 3.017 | 4.597 | 6.303 | 8.089 | 9.924 | 11.788 | 13.669 | 15.556 | 17.441 |
| 20 | 0.656 | 1.744 | 3.172 | 4.805 | 6.564 | 8.400 | 10.284 | 12.195 | 14.122 | 16.052 | 17.979 |
| 21 | 0.704 | 1.843 | 3.323 | 5.008 | 6.816 | 8.701 | 10.632 | 12.589 | 14.559 | 16.532 | 18.498 |
| 22 | 0.752 | 1.940 | 3.471 | 5.205 | 7.062 | 8.993 | 10.970 | 12.971 | 14.983 | 16.995 | 18.999 |
| 23 | 0.800 | 2.035 | 3.614 | 5.397 | 7.301 | 9.277 | 11.297 | 13.340 | 15.393 | 17.443 | 19.484 |
| 24 | 0.847 | 2.128 | 3.755 | 5.584 | 7.533 | 9.553 | 11.615 | 13.699 | 15.790 | 17.878 | 19.953 |
| 25 | 0.893 | 2.219 | 3.892 | 5.766 | 7.759 | 9.821 | 11.924 | 14.047 | 16.176 | 18.298 | 20.408 |
| 26 | 0.939 | 2.309 | 4.026 | 5.944 | 7.979 | 10.082 | 12.225 | 14.385 | 16.550 | 18.707 | 20.849 |
| 27 | 0.984 | 2.396 | 4.157 | 6.117 | 8.193 | 10.336 | 12.517 | 14.714 | 16.914 | 19.103 | 21.276 |
| 28 | 1.029 | 2.482 | 4.285 | 6.286 | 8.402 | 10.584 | 12.801 | 15.034 | 17.267 | 19.489 | 21.691 |
| 29 | 1.073 | 2.566 | 4.410 | 6.451 | 8.606 | 10.825 | 13.079 | 15.346 | 17.611 | 19.863 | 22.095 |
| 20 | 1.116 | 2.649 | 4.532 | 6.612 | 8.805 | 11.061 | 13.349 | 15.649 | 17.946 | 20.228 | 22.487 |

Table B. 49
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 75 /$ Dividend Rate $=\mathbf{3 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.019 | 0.050 | 0.103 | 0.182 | 0.290 | 0.426 |
| 2 | 0.000 | 0.000 | 0.006 | 0.030 | 0.093 | 0.206 | 0.375 | 0.598 | 0.873 | 1.194 | 1.555 |
| 3 | 0.000 | 0.005 | 0.034 | 0.121 | 0.286 | 0.535 | 0.860 | 1.254 | 1.706 | 2.207 | 2.749 |
| 4 | 0.001 | 0.017 | 0.092 | 0.264 | 0.544 | 0.927 | 1.398 | 1.941 | 2.544 | 3.196 | 3.887 |
| 5 | 0.003 | 0.040 | 0.174 | 0.440 | 0.835 | 1.343 | 1.944 | 2.619 | 3.353 | 4.134 | 4.952 |
| 6 | 0.007 | 0.075 | 0.276 | 0.636 | 1.141 | 1.765 | 2.483 | 3.275 | 4.124 | 5.018 | 5.947 |
| 7 | 0.014 | 0.118 | 0.391 | 0.844 | 1.451 | 2.182 | 3.006 | 3.903 | 4.856 | 5.850 | 6.878 |
| 8 | 0.024 | 0.170 | 0.515 | 1.058 | 1.762 | 2.590 | 3.512 | 4.505 | 5.551 | 6.637 | 7.754 |
| 9 | 0.037 | 0.227 | 0.645 | 1.274 | 2.068 | 2.988 | 4.000 | 5.080 | 6.212 | 7.382 | 8.580 |
| 10 | 0.052 | 0.290 | 0.780 | 1.490 | 2.370 | 3.374 | 4.469 | 5.631 | 6.842 | 8.089 | 9.362 |
| 11 | 0.069 | 0.357 | 0.916 | 1.705 | 2.664 | 3.748 | 4.921 | 6.159 | 7.443 | 8.762 | 10.105 |
| 12 | 0.089 | 0.427 | 1.054 | 1.917 | 2.952 | 4.110 | 5.356 | 6.665 | 8.018 | 9.404 | 10.812 |
| 13 | 0.111 | 0.498 | 1.192 | 2.126 | 3.233 | 4.461 | 5.776 | 7.151 | 8.570 | 10.018 | 11.486 |
| 14 | 0.134 | 0.572 | 1.329 | 2.331 | 3.506 | 4.801 | 6.181 | 7.620 | 9.099 | 10.606 | 12.132 |
| 15 | 0.159 | 0.646 | 1.465 | 2.532 | 3.772 | 5.131 | 6.572 | 8.071 | 9.608 | 11.171 | 12.750 |
| 16 | 0.185 | 0.722 | 1.600 | 2.729 | 4.031 | 5.451 | 6.951 | 8.506 | 10.098 | 11.714 | 13.344 |
| 17 | 0.213 | 0.797 | 1.733 | 2.923 | 4.284 | 5.761 | 7.317 | 8.926 | 10.570 | 12.236 | 13.915 |


| 18 | 0.241 | 0.873 | 1.865 | 3.112 | 4.529 | 6.062 | 7.671 | 9.332 | 11.026 | 12.740 | 14.465 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.270 | 0.948 | 1.994 | 3.297 | 4.769 | 6.354 | 8.015 | 9.725 | 11.467 | 13.226 | 14.995 |
| 20 | 0.299 | 1.023 | 2.122 | 3.478 | 5.002 | 6.639 | 8.348 | 10.106 | 11.893 | 13.696 | 15.507 |
| 21 | 0.329 | 1.098 | 2.247 | 3.655 | 5.230 | 6.915 | 8.672 | 10.475 | 12.306 | 14.151 | 16.001 |
| 22 | 0.359 | 1.172 | 2.371 | 3.828 | 5.452 | 7.184 | 8.987 | 10.833 | 12.706 | 14.591 | 16.479 |
| 23 | 0.389 | 1.245 | 2.492 | 3.997 | 5.668 | 7.446 | 9.292 | 11.181 | 13.094 | 15.018 | 16.942 |
| 24 | 0.420 | 1.318 | 2.611 | 4.163 | 5.880 | 7.701 | 9.590 | 11.519 | 13.471 | 15.432 | 17.391 |
| 25 | 0.451 | 1.390 | 2.728 | 4.325 | 6.086 | 7.950 | 9.879 | 11.848 | 13.837 | 15.833 | 17.825 |
| 26 | 0.482 | 1.461 | 2.843 | 4.484 | 6.287 | 8.193 | 10.162 | 12.168 | 14.193 | 16.223 | 18.247 |
| 27 | 0.513 | 1.531 | 2.956 | 4.639 | 6.484 | 8.429 | 10.436 | 12.479 | 14.539 | 16.602 | 18.657 |
| 28 | 0.543 | 1.600 | 3.067 | 4.792 | 6.676 | 8.660 | 10.704 | 12.782 | 14.876 | 16.970 | 19.055 |
| 29 | 0.574 | 1.669 | 3.176 | 4.941 | 6.864 | 8.886 | 10.966 | 13.078 | 15.204 | 17.329 | 19.442 |
| 30 | 0.605 | 1.736 | 3.283 | 5.087 | 7.048 | 9.106 | 11.221 | 13.366 | 15.524 | 17.678 | 19.819 |

Table B. 50
American-Style Put Premiums as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 7 0} /$ Dividend Rate $=\mathbf{3 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.009 | 0.025 | 0.054 | 0.100 | 0.166 |
| 2 | 0.000 | 0.000 | 0.001 | 0.005 | 0.022 | 0.064 | 0.142 | 0.260 | 0.423 | 0.629 | 0.875 |
| 3 | 0.000 | 0.001 | 0.006 | 0.032 | 0.101 | 0.226 | 0.417 | 0.671 | 0.985 | 1.353 | 1.769 |
| 4 | 0.000 | 0.003 | 0.023 | 0.091 | 0.233 | 0.461 | 0.772 | 1.159 | 1.614 | 2.126 | 2.686 |
| 5 | 0.000 | 0.008 | 0.053 | 0.178 | 0.405 | 0.737 | 1.165 | 1.676 | 2.256 | 2.894 | 3.581 |
| 6 | 0.001 | 0.018 | 0.098 | 0.288 | 0.603 | 1.037 | 1.574 | 2.197 | 2.890 | 3.641 | 4.438 |
| 7 | 0.002 | 0.033 | 0.155 | 0.415 | 0.817 | 1.348 | 1.987 | 2.713 | 3.509 | 4.360 | 5.257 |
| 8 | 0.005 | 0.053 | 0.223 | 0.553 | 1.041 | 1.664 | 2.397 | 3.217 | 4.107 | 5.050 | 6.036 |
| 9 | 0.008 | 0.079 | 0.298 | 0.700 | 1.270 | 1.980 | 2.801 | 3.709 | 4.684 | 5.711 | 6.779 |
| 10 | 0.012 | 0.108 | 0.380 | 0.852 | 1.501 | 2.293 | 3.196 | 4.185 | 5.240 | 6.345 | 7.488 |
| 11 | 0.018 | 0.142 | 0.468 | 1.008 | 1.732 | 2.601 | 3.582 | 4.647 | 5.776 | 6.953 | 8.166 |
| 12 | 0.025 | 0.179 | 0.559 | 1.166 | 1.962 | 2.905 | 3.958 | 5.094 | 6.292 | 7.536 | 8.814 |
| 13 | 0.033 | 0.220 | 0.653 | 1.324 | 2.190 | 3.202 | 4.324 | 5.527 | 6.790 | 8.097 | 9.436 |
| 14 | 0.042 | 0.262 | 0.749 | 1.483 | 2.415 | 3.493 | 4.680 | 5.947 | 7.271 | 8.637 | 10.034 |
| 15 | 0.053 | 0.307 | 0.846 | 1.642 | 2.636 | 3.778 | 5.027 | 6.353 | 7.735 | 9.158 | 10.608 |
| 16 | 0.064 | 0.354 | 0.945 | 1.799 | 2.854 | 4.056 | 5.364 | 6.747 | 8.185 | 9.660 | 11.161 |
| 17 | 0.077 | 0.402 | 1.044 | 1.955 | 3.068 | 4.328 | 5.692 | 7.129 | 8.619 | 10.145 | 11.694 |


| 18 | 0.090 | 0.451 | 1.143 | 2.109 | 3.279 | 4.593 | 6.011 | 7.500 | 9.040 | 10.614 | 12.209 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.105 | 0.501 | 1.242 | 2.261 | 3.485 | 4.853 | 6.321 | 7.861 | 9.448 | 11.067 | 12.706 |
| 20 | 0.120 | 0.552 | 1.340 | 2.412 | 3.687 | 5.106 | 6.624 | 8.211 | 9.844 | 11.507 | 13.187 |
| 21 | 0.136 | 0.604 | 1.439 | 2.560 | 3.886 | 5.354 | 6.919 | 8.551 | 10.228 | 11.932 | 13.653 |
| 22 | 0.152 | 0.656 | 1.536 | 2.706 | 4.080 | 5.595 | 7.206 | 8.882 | 10.601 | 12.345 | 14.104 |
| 23 | 0.169 | 0.708 | 1.633 | 2.850 | 4.271 | 5.832 | 7.487 | 9.205 | 10.963 | 12.746 | 14.542 |
| 24 | 0.187 | 0.761 | 1.729 | 2.992 | 4.458 | 6.063 | 7.760 | 9.519 | 11.316 | 13.136 | 14.966 |
| 25 | 0.204 | 0.813 | 1.824 | 3.131 | 4.641 | 6.288 | 8.027 | 9.824 | 11.659 | 13.515 | 15.378 |
| 26 | 0.223 | 0.865 | 1.918 | 3.268 | 4.821 | 6.509 | 8.287 | 10.123 | 11.993 | 13.883 | 15.779 |
| 27 | 0.241 | 0.918 | 2.010 | 3.403 | 4.997 | 6.725 | 8.541 | 10.414 | 12.319 | 14.241 | 16.168 |
| 28 | 0.260 | 0.970 | 2.102 | 3.535 | 5.170 | 6.937 | 8.790 | 10.697 | 12.636 | 14.590 | 16.546 |
| 29 | 0.279 | 1.022 | 2.193 | 3.666 | 5.339 | 7.144 | 9.033 | 10.974 | 12.946 | 14.930 | 16.915 |
| 30 | 0.298 | 1.073 | 2.282 | 3.794 | 5.505 | 7.346 | 9.270 | 11.245 | 13.248 | 15.262 | 17.273 |

Table B. 51
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\$ 100 /$ Strike Price $=\$ 65 /$ Dividend Rate $=3 \%$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.012 | 0.028 | 0.054 |
| 2 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.016 | 0.044 | 0.096 | 0.179 | 0.295 | 0.446 |
| 3 | 0.000 | 0.000 | 0.001 | 0.007 | 0.029 | 0.081 | 0.177 | 0.322 | 0.518 | 0.766 | 1.061 |
| 4 | 0.000 | 0.000 | 0.004 | 0.026 | 0.085 | 0.201 | 0.384 | 0.636 | 0.952 | 1.328 | 1.758 |
| 5 | 0.000 | 0.001 | 0.013 | 0.061 | 0.172 | 0.365 | 0.641 | 0.999 | 1.430 | 1.925 | 2.475 |
| 6 | 0.000 | 0.004 | 0.029 | 0.113 | 0.285 | 0.558 | 0.928 | 1.388 | 1.925 | 2.528 | 3.186 |
| 7 | 0.000 | 0.008 | 0.052 | 0.179 | 0.417 | 0.771 | 1.233 | 1.788 | 2.424 | 3.125 | 3.881 |
| 8 | 0.001 | 0.014 | 0.083 | 0.258 | 0.564 | 0.998 | 1.546 | 2.192 | 2.918 | 3.710 | 4.555 |
| 9 | 0.002 | 0.023 | 0.120 | 0.347 | 0.721 | 1.233 | 1.864 | 2.594 | 3.404 | 4.279 | 5.205 |
| 10 | 0.003 | 0.034 | 0.164 | 0.444 | 0.885 | 1.472 | 2.181 | 2.991 | 3.879 | 4.831 | 5.833 |
| 11 | 0.004 | 0.048 | 0.213 | 0.547 | 1.054 | 1.713 | 2.497 | 3.381 | 4.343 | 5.366 | 6.438 |
| 12 | 0.006 | 0.065 | 0.266 | 0.655 | 1.227 | 1.955 | 2.809 | 3.763 | 4.794 | 5.885 | 7.021 |
| 13 | 0.008 | 0.084 | 0.323 | 0.767 | 1.401 | 2.196 | 3.117 | 4.137 | 5.233 | 6.386 | 7.584 |
| 14 | 0.011 | 0.106 | 0.384 | 0.881 | 1.577 | 2.435 | 3.420 | 4.502 | 5.659 | 6.872 | 8.127 |
| 15 | 0.015 | 0.129 | 0.448 | 0.997 | 1.752 | 2.671 | 3.717 | 4.859 | 6.074 | 7.343 | 8.652 |
| 16 | 0.019 | 0.154 | 0.513 | 1.115 | 1.927 | 2.904 | 4.008 | 5.207 | 6.477 | 7.799 | 9.159 |
| 17 | 0.024 | 0.181 | 0.581 | 1.233 | 2.100 | 3.134 | 4.293 | 5.547 | 6.869 | 8.241 | 9.650 |


| 18 | 0.029 | 0.210 | 0.650 | 1.352 | 2.273 | 3.360 | 4.573 | 5.878 | 7.250 | 8.670 | 10.125 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.035 | 0.240 | 0.720 | 1.471 | 2.443 | 3.583 | 4.847 | 6.201 | 7.621 | 9.087 | 10.585 |
| 20 | 0.042 | 0.271 | 0.791 | 1.590 | 2.612 | 3.802 | 5.115 | 6.516 | 7.982 | 9.492 | 11.031 |
| 21 | 0.049 | 0.303 | 0.862 | 1.708 | 2.778 | 4.017 | 5.377 | 6.824 | 8.333 | 9.885 | 11.464 |
| 22 | 0.057 | 0.336 | 0.934 | 1.825 | 2.943 | 4.228 | 5.634 | 7.125 | 8.676 | 10.267 | 11.885 |
| 23 | 0.065 | 0.369 | 1.007 | 1.942 | 3.105 | 4.436 | 5.885 | 7.418 | 9.009 | 10.639 | 12.293 |
| 24 | 0.073 | 0.404 | 1.079 | 2.057 | 3.265 | 4.639 | 6.131 | 7.705 | 9.335 | 11.001 | 12.690 |
| 25 | 0.082 | 0.439 | 1.152 | 2.172 | 3.423 | 4.839 | 6.372 | 7.985 | 9.652 | 11.354 | 13.076 |
| 26 | 0.092 | 0.474 | 1.224 | 2.285 | 3.578 | 5.035 | 6.607 | 8.258 | 9.961 | 11.697 | 13.451 |
| 27 | 0.101 | 0.510 | 1.296 | 2.398 | 3.731 | 5.228 | 6.838 | 8.526 | 10.263 | 12.032 | 13.817 |
| 28 | 0.112 | 0.546 | 1.368 | 2.509 | 3.882 | 5.417 | 7.064 | 8.787 | 10.558 | 12.359 | 14.173 |
| 29 | 0.122 | 0.582 | 1.440 | 2.619 | 4.030 | 5.603 | 7.286 | 9.043 | 10.846 | 12.677 | 14.520 |
| 30 | 0.133 | 0.619 | 1.511 | 2.727 | 4.176 | 5.785 | 7.503 | 9.293 | 11.128 | 12.988 | 14.859 |

Table B. 52
American-Style Put Premiums as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 60 /$ Dividend Rate $=\mathbf{3 \%}$

## Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.002 | 0.006 | 0.014 |
| 2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.003 | 0.011 | 0.029 | 0.064 | 0.120 | 0.201 |
| 3 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.024 | 0.063 | 0.134 | 0.243 | 0.393 | 0.585 |
| 4 | 0.000 | 0.000 | 0.001 | 0.006 | 0.026 | 0.075 | 0.169 | 0.314 | 0.514 | 0.769 | 1.077 |
| 5 | 0.000 | 0.000 | 0.003 | 0.017 | 0.063 | 0.159 | 0.318 | 0.547 | 0.842 | 1.202 | 1.619 |
| 6 | 0.000 | 0.001 | 0.007 | 0.037 | 0.118 | 0.269 | 0.502 | 0.815 | 1.205 | 1.663 | 2.181 |
| 7 | 0.000 | 0.002 | 0.015 | 0.067 | 0.189 | 0.402 | 0.709 | 1.106 | 1.585 | 2.136 | 2.748 |
| 8 | 0.000 | 0.003 | 0.026 | 0.105 | 0.275 | 0.551 | 0.932 | 1.410 | 1.974 | 2.611 | 3.310 |
| 9 | 0.000 | 0.006 | 0.041 | 0.153 | 0.372 | 0.712 | 1.166 | 1.722 | 2.366 | 3.083 | 3.862 |
| 10 | 0.001 | 0.009 | 0.061 | 0.207 | 0.479 | 0.882 | 1.407 | 2.037 | 2.756 | 3.549 | 4.402 |
| 11 | 0.001 | 0.014 | 0.085 | 0.268 | 0.593 | 1.059 | 1.652 | 2.353 | 3.143 | 4.006 | 4.928 |
| 12 | 0.001 | 0.020 | 0.112 | 0.335 | 0.713 | 1.241 | 1.899 | 2.667 | 3.524 | 4.454 | 5.440 |
| 13 | 0.002 | 0.028 | 0.143 | 0.406 | 0.837 | 1.425 | 2.147 | 2.979 | 3.899 | 4.891 | 5.937 |
| 14 | 0.003 | 0.037 | 0.177 | 0.482 | 0.965 | 1.611 | 2.393 | 3.286 | 4.267 | 5.317 | 6.421 |
| 15 | 0.004 | 0.047 | 0.213 | 0.560 | 1.095 | 1.798 | 2.638 | 3.589 | 4.627 | 5.733 | 6.891 |
| 17 | 0.007 | 0.072 | 0.294 | 0.725 | 1.361 | 2.171 | 3.121 | 4.181 | 5.325 | 6.534 | 7.790 |
| 105 | 0.059 | 0.253 | 0.642 | 1.228 | 1.984 | 2.881 | 3.888 | 4.980 | 6.139 | 7.347 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.009 | 0.086 | 0.338 | 0.811 | 1.495 | 2.356 | 3.358 | 4.469 | 5.663 | 6.919 | 8.221 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.011 | 0.102 | 0.383 | 0.897 | 1.629 | 2.540 | 3.592 | 4.751 | 5.993 | 7.294 | 8.640 |
| 20 | 0.013 | 0.118 | 0.430 | 0.985 | 1.763 | 2.722 | 3.822 | 5.029 | 6.315 | 7.660 | 9.048 |
| 21 | 0.016 | 0.136 | 0.478 | 1.074 | 1.897 | 2.902 | 4.049 | 5.300 | 6.630 | 8.017 | 9.444 |
| 22 | 0.019 | 0.155 | 0.527 | 1.163 | 2.030 | 3.081 | 4.272 | 5.567 | 6.939 | 8.365 | 9.830 |
| 23 | 0.022 | 0.174 | 0.577 | 1.252 | 2.162 | 3.257 | 4.491 | 5.828 | 7.240 | 8.705 | 10.206 |
| 24 | 0.026 | 0.194 | 0.628 | 1.342 | 2.294 | 3.431 | 4.707 | 6.084 | 7.534 | 9.036 | 10.572 |
| 25 | 0.029 | 0.215 | 0.679 | 1.431 | 2.424 | 3.603 | 4.919 | 6.335 | 7.823 | 9.360 | 10.929 |
| 26 | 0.034 | 0.237 | 0.731 | 1.521 | 2.554 | 3.772 | 5.127 | 6.581 | 8.105 | 9.675 | 11.277 |
| 27 | 0.038 | 0.259 | 0.784 | 1.610 | 2.682 | 3.939 | 5.332 | 6.822 | 8.380 | 9.984 | 11.616 |
| 28 | 0.043 | 0.282 | 0.837 | 1.699 | 2.809 | 4.104 | 5.534 | 7.059 | 8.650 | 10.285 | 11.947 |
| 29 | 0.048 | 0.305 | 0.890 | 1.787 | 2.934 | 4.266 | 5.731 | 7.291 | 8.914 | 10.580 | 12.270 |
| 30 | 0.053 | 0.329 | 0.943 | 1.875 | 3.058 | 4.426 | 5.926 | 7.518 | 9.173 | 10.868 | 12.585 |

## APPENDIX C- <br> IN-THE-MONEY PROBABILITIES

The tables that follow show the probability of a put option winding up in the money by the expiration date, based upon Equations 13.2 and 13.13. They are based on a stock price of $\$ 100$ and exercise (strike) prices ranging from $\$ 120$ down to $\$ 80$ in steps of $\$ 5$. Annual earnings growth rates of 0 percent, 5 percent, 10 percent, 15 percent, and 20 percent are considered. Each table is presented in matrix format, with volatilities ranging from a low of 0.150 through a high of 0.650 . Time to expiration ranges from 1 month to a maximum of 30 months. The dividend rate is zero and risk-free interest rate is 6 percent in all instances.

For example, suppose you wanted to know the probability of winding up in the money for an at-the-money LEAP put with stock and strike price of $\$ 100$, volatility of 0.40 , with an expiration date of 24 months away, no dividend, and risk-free interest rate of 6 percent. From Table C.5, we see that for a zero growth in earnings (and accompanying stock price), the associated probability is 0.310 . For a 5 percent growth rate in earnings, Table C. 14 shows this probability to fall to 0.251 . For a 10 percent growth rate in earnings, Table C. 23 shows this probability to fall to 0.198 . For a 15 percent growth rate in earnings, Table C. 32 shows this probability to fall to 0.153 . And for a 20 percent growth rate in earnings, Table C. 41 shows this probability to fall to just 0.115 . These probabilities hold independently of whether a European- or American-style pricing formula is used to determine premiums.

Table C. 2
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 115 /$ Annual Growth Rate $=0 \%$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.999 | 0.989 | 0.966 | 0.935 | 0.900 | 0.866 | 0.835 | 0.806 | 0.779 | 0.755 | 0.734 |
| 2 | 0.982 | 0.939 | 0.889 | 0.841 | 0.799 | 0.762 | 0.731 | 0.703 | 0.679 | 0.658 | 0.639 |
| 3 | 0.948 | 0.884 | 0.825 | 0.775 | 0.734 | 0.700 | 0.671 | 0.646 | 0.624 | 0.605 | 0.588 |
| 4 | 0.910 | 0.836 | 0.776 | 0.727 | 0.688 | 0.657 | 0.630 | 0.607 | 0.586 | 0.568 | 0.552 |
| 5 | 0.872 | 0.795 | 0.736 | 0.690 | 0.654 | 0.624 | 0.599 | 0.577 | 0.558 | 0.541 | 0.525 |
| 6 | 0.837 | 0.760 | 0.703 | 0.660 | 0.625 | 0.597 | 0.574 | 0.553 | 0.535 | 0.519 | 0.504 |
| 7 | 0.804 | 0.729 | 0.675 | 0.634 | 0.602 | 0.575 | 0.553 | 0.533 | 0.516 | 0.500 | 0.485 |
| 8 | 0.774 | 0.702 | 0.650 | 0.612 | 0.582 | 0.557 | 0.535 | 0.516 | 0.499 | 0.484 | 0.469 |
| 9 | 0.747 | 0.677 | 0.629 | 0.593 | 0.564 | 0.540 | 0.519 | 0.501 | 0.484 | 0.469 | 0.455 |
| 10 | 0.721 | 0.656 | 0.610 | 0.576 | 0.548 | 0.525 | 0.505 | 0.487 | 0.471 | 0.456 | 0.442 |
| 11 | 0.698 | 0.636 | 0.593 | 0.560 | 0.534 | 0.512 | 0.493 | 0.475 | 0.459 | 0.444 | 0.431 |
| 12 | 0.676 | 0.617 | 0.577 | 0.546 | 0.521 | 0.500 | 0.481 | 0.464 | 0.448 | 0.434 | 0.420 |
| 13 | 0.656 | 0.601 | 0.562 | 0.533 | 0.509 | 0.489 | 0.470 | 0.454 | 0.438 | 0.424 | 0.410 |
| 14 | 0.637 | 0.585 | 0.549 | 0.521 | 0.498 | 0.478 | 0.460 | 0.444 | 0.429 | 0.414 | 0.401 |
| 15 | 0.619 | 0.571 | 0.537 | 0.510 | 0.488 | 0.469 | 0.451 | 0.435 | 0.420 | 0.406 | 0.392 |
| 16 | 0.602 | 0.557 | 0.525 | 0.500 | 0.478 | 0.460 | 0.442 | 0.427 | 0.412 | 0.397 | 0.384 |
| 17 | 0.586 | 0.544 | 0.514 | 0.490 | 0.469 | 0.451 | 0.434 | 0.419 | 0.404 | 0.390 | 0.376 |


| 18 | 0.571 | 0.532 | 0.504 | 0.481 | 0.461 | 0.443 | 0.426 | 0.411 | 0.396 | 0.382 | 0.369 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.557 | 0.521 | 0.494 | 0.472 | 0.453 | 0.435 | 0.419 | 0.404 | 0.389 | 0.375 | 0.362 |
| 20 | 0.543 | 0.510 | 0.485 | 0.464 | 0.445 | 0.428 | 0.412 | 0.397 | 0.382 | 0.368 | 0.355 |
| 21 | 0.530 | 0.500 | 0.476 | 0.456 | 0.438 | 0.421 | 0.405 | 0.390 | 0.376 | 0.362 | 0.348 |
| 22 | 0.518 | 0.490 | 0.468 | 0.448 | 0.431 | 0.415 | 0.399 | 0.384 | 0.370 | 0.356 | 0.342 |
| 23 | 0.506 | 0.480 | 0.460 | 0.441 | 0.424 | 0.408 | 0.393 | 0.378 | 0.364 | 0.350 | 0.336 |
| 24 | 0.495 | 0.471 | 0.452 | 0.434 | 0.418 | 0.402 | 0.387 | 0.372 | 0.358 | 0.344 | 0.331 |
| 25 | 0.484 | 0.463 | 0.445 | 0.428 | 0.412 | 0.396 | 0.381 | 0.367 | 0.353 | 0.339 | 0.325 |
| 26 | 0.474 | 0.455 | 0.437 | 0.421 | 0.406 | 0.391 | 0.376 | 0.361 | 0.347 | 0.333 | 0.320 |
| 27 | 0.464 | 0.447 | 0.431 | 0.415 | 0.400 | 0.385 | 0.371 | 0.356 | 0.342 | 0.328 | 0.315 |
| 28 | 0.454 | 0.439 | 0.424 | 0.409 | 0.394 | 0.380 | 0.365 | 0.351 | 0.337 | 0.323 | 0.310 |
| 29 | 0.445 | 0.432 | 0.418 | 0.403 | 0.389 | 0.375 | 0.360 | 0.346 | 0.332 | 0.318 | 0.305 |
| 30 | 0.436 | 0.424 | 0.412 | 0.398 | 0.384 | 0.370 | 0.356 | 0.342 | 0.328 | 0.314 | 0.300 |

Table C. 3
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 110 /$ Annual Growth Rate $=0 \%$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.980 | 0.938 | 0.888 | 0.841 | 0.800 | 0.766 | 0.736 | 0.710 | 0.688 | 0.668 | 0.651 |
| 2 | 0.913 | 0.842 | 0.784 | 0.737 | 0.700 | 0.670 | 0.645 | 0.624 | 0.606 | 0.589 | 0.575 |
| 3 | 0.849 | 0.774 | 0.719 | 0.677 | 0.645 | 0.619 | 0.597 | 0.578 | 0.561 | 0.547 | 0.534 |
| 4 | 0.796 | 0.724 | 0.673 | 0.636 | 0.607 | 0.583 | 0.564 | 0.546 | 0.531 | 0.518 | 0.505 |
| 5 | 0.751 | 0.684 | 0.639 | 0.605 | 0.579 | 0.557 | 0.539 | 0.523 | 0.508 | 0.495 | 0.483 |
| 6 | 0.713 | 0.652 | 0.611 | 0.580 | 0.556 | 0.536 | 0.518 | 0.503 | 0.489 | 0.477 | 0.465 |
| 7 | 0.681 | 0.625 | 0.587 | 0.559 | 0.537 | 0.518 | 0.501 | 0.487 | 0.473 | 0.461 | 0.450 |
| 8 | 0.652 | 0.601 | 0.567 | 0.541 | 0.520 | 0.502 | 0.487 | 0.473 | 0.460 | 0.447 | 0.436 |
| 9 | 0.626 | 0.581 | 0.549 | 0.525 | 0.506 | 0.489 | 0.474 | 0.460 | 0.447 | 0.435 | 0.424 |
| 10 | 0.604 | 0.562 | 0.534 | 0.511 | 0.493 | 0.477 | 0.462 | 0.449 | 0.436 | 0.424 | 0.413 |
| 11 | 0.583 | 0.546 | 0.519 | 0.499 | 0.481 | 0.466 | 0.451 | 0.438 | 0.426 | 0.414 | 0.403 |
| 12 | 0.564 | 0.531 | 0.506 | 0.487 | 0.470 | 0.456 | 0.442 | 0.429 | 0.417 | 0.405 | 0.393 |
| 13 | 0.546 | 0.517 | 0.495 | 0.476 | 0.461 | 0.446 | 0.433 | 0.420 | 0.408 | 0.396 | 0.385 |
| 14 | 0.530 | 0.504 | 0.484 | 0.467 | 0.451 | 0.437 | 0.424 | 0.412 | 0.400 | 0.388 | 0.376 |
| 15 | 0.515 | 0.492 | 0.473 | 0.457 | 0.443 | 0.429 | 0.416 | 0.404 | 0.392 | 0.380 | 0.369 |
| 16 | 0.501 | 0.480 | 0.464 | 0.449 | 0.435 | 0.422 | 0.409 | 0.397 | 0.385 | 0.373 | 0.361 |
| 17 | 0.487 | 0.470 | 0.455 | 0.441 | 0.427 | 0.414 | 0.402 | 0.390 | 0.378 | 0.366 | 0.354 |


| 18 | 0.475 | 0.460 | 0.446 | 0.433 | 0.420 | 0.407 | 0.395 | 0.383 | 0.371 | 0.359 | 0.348 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.463 | 0.450 | 0.438 | 0.425 | 0.413 | 0.401 | 0.389 | 0.377 | 0.365 | 0.353 | 0.341 |
| 20 | 0.452 | 0.441 | 0.430 | 0.418 | 0.407 | 0.395 | 0.383 | 0.371 | 0.359 | 0.347 | 0.335 |
| 21 | 0.441 | 0.433 | 0.423 | 0.412 | 0.400 | 0.389 | 0.377 | 0.365 | 0.353 | 0.341 | 0.330 |
| 22 | 0.431 | 0.425 | 0.416 | 0.405 | 0.394 | 0.383 | 0.371 | 0.359 | 0.348 | 0.336 | 0.324 |
| 23 | 0.421 | 0.417 | 0.409 | 0.399 | 0.389 | 0.377 | 0.366 | 0.354 | 0.342 | 0.330 | 0.319 |
| 24 | 0.412 | 0.410 | 0.403 | 0.393 | 0.383 | 0.372 | 0.361 | 0.349 | 0.337 | 0.325 | 0.313 |
| 25 | 0.403 | 0.402 | 0.396 | 0.388 | 0.378 | 0.367 | 0.356 | 0.344 | 0.332 | 0.320 | 0.308 |
| 26 | 0.395 | 0.395 | 0.390 | 0.382 | 0.373 | 0.362 | 0.351 | 0.339 | 0.327 | 0.315 | 0.303 |
| 27 | 0.386 | 0.389 | 0.385 | 0.377 | 0.368 | 0.357 | 0.346 | 0.334 | 0.323 | 0.311 | 0.299 |
| 28 | 0.378 | 0.382 | 0.379 | 0.372 | 0.363 | 0.352 | 0.341 | 0.330 | 0.318 | 0.306 | 0.294 |
| 29 | 0.371 | 0.376 | 0.374 | 0.367 | 0.358 | 0.348 | 0.337 | 0.325 | 0.314 | 0.302 | 0.290 |
| 20 | 0.363 | 0.370 | 0.368 | 0.362 | 0.354 | 0.344 | 0.333 | 0.321 | 0.309 | 0.297 | 0.285 |

Table C. 4
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 105 /$ Annual Growth Rate $=0 \%$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.839 | 0.767 | 0.716 | 0.678 | 0.649 | 0.626 | 0.607 | 0.591 | 0.578 | 0.566 | 0.556 |
| 2 | 0.727 | 0.668 | 0.629 | 0.601 | 0.579 | 0.562 | 0.547 | 0.535 | 0.524 | 0.514 | 0.505 |
| 3 | 0.660 | 0.613 | 0.582 | 0.560 | 0.542 | 0.527 | 0.515 | 0.504 | 0.494 | 0.485 | 0.477 |
| 4 | 0.614 | 0.576 | 0.551 | 0.532 | 0.517 | 0.504 | 0.492 | 0.482 | 0.473 | 0.464 | 0.456 |
| 5 | 0.578 | 0.548 | 0.527 | 0.510 | 0.497 | 0.485 | 0.475 | 0.465 | 0.456 | 0.447 | 0.439 |
| 6 | 0.549 | 0.525 | 0.507 | 0.493 | 0.481 | 0.470 | 0.460 | 0.451 | 0.442 | 0.433 | 0.425 |
| 7 | 0.525 | 0.506 | 0.491 | 0.478 | 0.467 | 0.457 | 0.448 | 0.438 | 0.430 | 0.421 | 0.413 |
| 8 | 0.504 | 0.489 | 0.476 | 0.465 | 0.455 | 0.446 | 0.437 | 0.428 | 0.419 | 0.410 | 0.402 |
| 9 | 0.486 | 0.474 | 0.464 | 0.454 | 0.445 | 0.436 | 0.427 | 0.418 | 0.409 | 0.400 | 0.392 |
| 10 | 0.469 | 0.461 | 0.452 | 0.444 | 0.435 | 0.426 | 0.417 | 0.409 | 0.400 | 0.391 | 0.383 |
| 11 | 0.454 | 0.449 | 0.442 | 0.434 | 0.426 | 0.418 | 0.409 | 0.400 | 0.392 | 0.383 | 0.374 |
| 12 | 0.440 | 0.438 | 0.433 | 0.426 | 0.418 | 0.410 | 0.401 | 0.393 | 0.384 | 0.375 | 0.366 |
| 13 | 0.428 | 0.428 | 0.424 | 0.418 | 0.410 | 0.402 | 0.394 | 0.385 | 0.377 | 0.368 | 0.359 |
| 14 | 0.416 | 0.418 | 0.415 | 0.410 | 0.403 | 0.395 | 0.387 | 0.379 | 0.370 | 0.361 | 0.352 |
| 15 | 0.405 | 0.409 | 0.408 | 0.403 | 0.396 | 0.389 | 0.381 | 0.372 | 0.363 | 0.354 | 0.345 |
| 16 | 0.395 | 0.401 | 0.400 | 0.396 | 0.390 | 0.383 | 0.375 | 0.366 | 0.357 | 0.348 | 0.338 |
| 17 | 0.385 | 0.393 | 0.393 | 0.390 | 0.384 | 0.377 | 0.369 | 0.360 | 0.351 | 0.342 | 0.332 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.376 | 0.386 | 0.387 | 0.384 | 0.378 | 0.371 | 0.363 | 0.354 | 0.345 | 0.336 | 0.326 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.367 | 0.378 | 0.380 | 0.378 | 0.373 | 0.366 | 0.358 | 0.349 | 0.340 | 0.330 | 0.321 |
| 20 | 0.359 | 0.372 | 0.374 | 0.372 | 0.367 | 0.360 | 0.352 | 0.344 | 0.335 | 0.325 | 0.315 |
| 21 | 0.351 | 0.365 | 0.369 | 0.367 | 0.362 | 0.355 | 0.348 | 0.339 | 0.330 | 0.320 | 0.310 |
| 22 | 0.344 | 0.359 | 0.363 | 0.362 | 0.357 | 0.351 | 0.343 | 0.334 | 0.325 | 0.315 | 0.305 |
| 23 | 0.336 | 0.353 | 0.358 | 0.357 | 0.352 | 0.346 | 0.338 | 0.329 | 0.320 | 0.310 | 0.300 |
| 24 | 0.329 | 0.347 | 0.353 | 0.352 | 0.348 | 0.341 | 0.334 | 0.325 | 0.315 | 0.306 | 0.296 |
| 25 | 0.323 | 0.342 | 0.348 | 0.347 | 0.343 | 0.337 | 0.329 | 0.320 | 0.311 | 0.301 | 0.291 |
| 26 | 0.316 | 0.336 | 0.343 | 0.343 | 0.339 | 0.333 | 0.325 | 0.316 | 0.307 | 0.297 | 0.287 |
| 27 | 0.310 | 0.331 | 0.338 | 0.339 | 0.335 | 0.329 | 0.321 | 0.312 | 0.303 | 0.293 | 0.282 |
| 28 | 0.304 | 0.326 | 0.334 | 0.334 | 0.331 | 0.325 | 0.317 | 0.308 | 0.299 | 0.289 | 0.278 |
| 29 | 0.298 | 0.321 | 0.329 | 0.330 | 0.327 | 0.321 | 0.313 | 0.304 | 0.295 | 0.285 | 0.274 |
| 30 | 0.293 | 0.316 | 0.325 | 0.326 | 0.323 | 0.317 | 0.309 | 0.300 | 0.291 | 0.281 | 0.270 |

Table C. 5
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 100 /$ Annual Growth Rate $=\mathbf{0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.445 | 0.454 | 0.458 | 0.460 | 0.460 | 0.460 | 0.459 | 0.457 | 0.456 | 0.454 | 0.452 |
| 2 | 0.423 | 0.435 | 0.441 | 0.443 | 0.444 | 0.443 | 0.442 | 0.440 | 0.438 | 0.435 | 0.432 |
| 3 | 0.406 | 0.421 | 0.428 | 0.431 | 0.431 | 0.431 | 0.429 | 0.427 | 0.424 | 0.421 | 0.417 |
| 4 | 0.392 | 0.409 | 0.417 | 0.420 | 0.421 | 0.420 | 0.418 | 0.415 | 0.412 | 0.409 | 0.405 |
| 5 | 0.380 | 0.398 | 0.407 | 0.411 | 0.412 | 0.411 | 0.409 | 0.406 | 0.402 | 0.398 | 0.394 |
| 6 | 0.368 | 0.389 | 0.398 | 0.402 | 0.403 | 0.402 | 0.400 | 0.397 | 0.393 | 0.389 | 0.384 |
| 7 | 0.358 | 0.380 | 0.390 | 0.395 | 0.396 | 0.395 | 0.392 | 0.389 | 0.385 | 0.380 | 0.375 |
| 8 | 0.349 | 0.372 | 0.383 | 0.388 | 0.389 | 0.388 | 0.385 | 0.381 | 0.377 | 0.372 | 0.367 |
| 9 | 0.340 | 0.365 | 0.376 | 0.381 | 0.382 | 0.381 | 0.378 | 0.374 | 0.370 | 0.365 | 0.359 |
| 10 | 0.332 | 0.358 | 0.369 | 0.375 | 0.376 | 0.375 | 0.372 | 0.368 | 0.363 | 0.358 | 0.352 |
| 11 | 0.325 | 0351 | 0.363 | 0.369 | 0.370 | 0.369 | 0.366 | 0.362 | 0.357 | 0.351 | 0.345 |
| 12 | 0.317 | 0.345 | 0.358 | 0.363 | 0.365 | 0.363 | 0.360 | 0.356 | 0.350 | 0.345 | 0.338 |
| 13 | 0.311 | 0.339 | 0.352 | 0.358 | 0.359 | 0.358 | 0.355 | 0.350 | 0.345 | 0.339 | 0.332 |
| 14 | 0.304 | 0.333 | 0.347 | 0.353 | 0.354 | 0.353 | 0.349 | 0.345 | 0.339 | 0.333 | 0.326 |
| 15 | 0.298 | 0.327 | 0.342 | 0.348 | 0.349 | 0.348 | 0.344 | 0.340 | 0.334 | 0.327 | 0.320 |
| 16 | 0.292 | 0.322 | 0.337 | 0.343 | 0.345 | 0.343 | 0.340 | 0.335 | 0.329 | 0.322 | 0.315 |
| 17 | 0.286 | 0.317 | 0.332 | 0.339 | 0.340 | 0.339 | 0.335 | 0.330 | 0.324 | 0.317 | 0.310 |


| 18 | 0.280 | 0.312 | 0.327 | 0.334 | 0.336 | 0.334 | 0.330 | 0.325 | 0.319 | 0.312 | 0.305 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.275 | 0.307 | 0.323 | 0.330 | 0.331 | 0.330 | 0.326 | 0.321 | 0.314 | 0.307 | 0.300 |
| 20 | 0.270 | 0.303 | 0.319 | 0.326 | 0.327 | 0.326 | 0.322 | 0.316 | 0.310 | 0.303 | 0.295 |
| 21 | 0.265 | 0.298 | 0.315 | 0.322 | 0.323 | 0.322 | 0.318 | 0.312 | 0.306 | 0.298 | 0.290 |
| 22 | 0.260 | 0.294 | 0.311 | 0.318 | 0.320 | 0.318 | 0.314 | 0.308 | 0.302 | 0.294 | 0.286 |
| 23 | 0.255 | 0.290 | 0.307 | 0.314 | 0.316 | 0.314 | 0.310 | 0.304 | 0.297 | 0.290 | 0.282 |
| 24 | 0.251 | 0.286 | 0.303 | 0.310 | 0.312 | 0.310 | 0.306 | 0.300 | 0.294 | 0.286 | 0.278 |
| 25 | 0.246 | 0.282 | 0.299 | 0.307 | 0.309 | 0.307 | 0.303 | 0.297 | 0.290 | 0.282 | 0.273 |
| 26 | 0.242 | 0.278 | 0.296 | 0.303 | 0.305 | 0.303 | 0.299 | 0.293 | 0.286 | 0.278 | 0.270 |
| 27 | 0.238 | 0.274 | 0.292 | 0.300 | 0.302 | 0.300 | 0.295 | 0.289 | 0.282 | 0.274 | 0.266 |
| 28 | 0.234 | 0.271 | 0.289 | 0.296 | 0.298 | 0.296 | 0.292 | 0.286 | 0.279 | 0.271 | 0.262 |
| 29 | 0.230 | 0.267 | 0.285 | 0.293 | 0.295 | 0.293 | 0.289 | 0.283 | 0.275 | 0.267 | 0.258 |
| 30 | 0.226 | 0.264 | 0.282 | 0.290 | 0.292 | 0.290 | 0.286 | 0.279 | 0.272 | 0.264 | 0.255 |

Table C. 6
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 95 /$ Annual Growth Rate $=\mathbf{0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.093 | 0.158 | 0.207 | 0.244 | 0.272 | 0.293 | 0.309 | 0.322 | 0.332 | 0.340 | 0.347 |
| 2 | 0.151 | 0.214 | 0.257 | 0.287 | 0.308 | 0.324 | 0.335 | 0.344 | 0.350 | 0.355 | 0.358 |
| 3 | 0.178 | 0.238 | 0.277 | 0.303 | 0.321 | 0.333 | 0.342 | 0.348 | 0.353 | 0.355 | 0.357 |
| 4 | 0.193 | 0.250 | 0.286 | 0.309 | 0.325 | 0.336 | 0.343 | 0.348 | 0.351 | 0.352 | 0.353 |
| 5 | 0.201 | 0.256 | 0.290 | 0.312 | 0.326 | 0.336 | 0.342 | 0.345 | 0.347 | 0.348 | 0.348 |
| 6 | 0.206 | 0.259 | 0.292 | 0.312 | 0.326 | 0.334 | 0.339 | 0.342 | 0.343 | 0.343 | 0.342 |
| 7 | 0.209 | 0.261 | 0.292 | 0.312 | 0.324 | 0.332 | 0.336 | 0.338 | 0.339 | 0.338 | 0.337 |
| 8 | 0.210 | 0.261 | 0.291 | 0.310 | 0.322 | 0.329 | 0.333 | 0.334 | 0.334 | 0.333 | 0.331 |
| 9 | 0.210 | 0.260 | 0.290 | 0.308 | 0.319 | 0.326 | 0.329 | 0.330 | 0.330 | 0.328 | 0.325 |
| 10 | 0.209 | 0.259 | 0.288 | 0.306 | 0.317 | 0.323 | 0.326 | 0.326 | 0.325 | 0.323 | 0.320 |
| 11 | 0.208 | 0.258 | 0.286 | 0.304 | 0.314 | 0.320 | 0.322 | 0.322 | 0.321 | 0.318 | 0.315 |
| 12 | 0.207 | 0.256 | 0.284 | 0.301 | 0.311 | 0.316 | 0.318 | 0.318 | 0.317 | 0.314 | 0.310 |
| 16 | 0.205 | 0.254 | 0.282 | 0.299 | 0.308 | 0.313 | 0.315 | 0.314 | 0.312 | 0.309 | 0.305 |
| 17 | 0.203 | 0.252 | 0.280 | 0.296 | 0.305 | 0.310 | 0.311 | 0.310 | 0.308 | 0.305 | 0.300 |
| 17 | 0.197 | 0.245 | 0.272 | 0.288 | 0.296 | 0.300 | 0.301 | 0.299 | 0.296 | 0.292 | 0.287 |
| 15 | 0.249 | 0.277 | 0.293 | 0.302 | 0.306 | 0.308 | 0.307 | 0.304 | 0.300 | 0.296 |  |
| 17 | 0.275 | 0.290 | 0.299 | 0.303 | 0.304 | 0.303 | 0.300 | 0.296 | 0.291 |  |  |


| 18 | 0.195 | 0.242 | 0.269 | 0.285 | 0.293 | 0.297 | 0.297 | 0.296 | 0.292 | 0.288 | 0.282 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.192 | 0.240 | 0.267 | 0.282 | 0.290 | 0.294 | 0.294 | 0.292 | 0.289 | 0.284 | 0.278 |
| 20 | 0.190 | 0.237 | 0.264 | 0.280 | 0.287 | 0.291 | 0.291 | 0.289 | 0.285 | 0.280 | 0.274 |
| 21 | 0.188 | 0.235 | 0.262 | 0.277 | 0.285 | 0.288 | 0.288 | 0.285 | 0.281 | 0.276 | 0.270 |
| 22 | 0.185 | 0.232 | 0.259 | 0.274 | 0.282 | 0.285 | 0.285 | 0.282 | 0.278 | 0.273 | 0.267 |
| 23 | 0.183 | 0.230 | 0.257 | 0.272 | 0.279 | 0.282 | 0.282 | 0.279 | 0.275 | 0.269 | 0.263 |
| 24 | 0.180 | 0.228 | 0.254 | 0.269 | 0.276 | 0.279 | 0.278 | 0.276 | 0.271 | 0.266 | 0.259 |
| 25 | 0.178 | 0.225 | 0.252 | 0.266 | 0.274 | 0.276 | 0.276 | 0.273 | 0.268 | 0.262 | 0.256 |
| 26 | 0.176 | 0.223 | 0.249 | 0.264 | 0.271 | 0.273 | 0.273 | 0.270 | 0.265 | 0.259 | 0.252 |
| 27 | 0.173 | 0.220 | 0.247 | 0.261 | 0.269 | 0.271 | 0.270 | 0.267 | 0.262 | 0.256 | 0.249 |
| 28 | 0.171 | 0.218 | 0.245 | 0.259 | 0.266 | 0.268 | 0.267 | 0.264 | 0.259 | 0.252 | 0.245 |
| 29 | 0.169 | 0.216 | 0.242 | 0.257 | 0.263 | 0.265 | 0.264 | 0.261 | 0.256 | 0.249 | 0.242 |
| 20 | 0.167 | 0.213 | 0.240 | 0.254 | 0.261 | 0.263 | 0.262 | 0.258 | 0.253 | 0.246 | 0.239 |

Table C. 7
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 90 /$ Annual Growth Rate $=\mathbf{0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.005 | 0.026 | 0.059 | 0.094 | 0.127 | 0.155 | 0.180 | 0.201 | 0.219 | 0.235 | 0.248 |
| 2 | 0.028 | 0.073 | 0.119 | 0.158 | 0.190 | 0.215 | 0.236 | 0.252 | 0.266 | 0.276 | 0.285 |
| 3 | 0.050 | 0.105 | 0.153 | 0.190 | 0.219 | 0.241 | 0.259 | 0.272 | 0.283 | 0.291 | 0.297 |
| 4 | 0.068 | 0.126 | 0.173 | 0.209 | 0.235 | 0.255 | 0.270 | 0.281 | 0.290 | 0.296 | 0.301 |
| 5 | 0.082 | 0.141 | 0.187 | 0.221 | 0.245 | 0.263 | 0.276 | 0.286 | 0.293 | 0.298 | 0.301 |
| 6 | 0.092 | 0.152 | 0.197 | 0.228 | 0.251 | 0.268 | 0.279 | 0.288 | 0.294 | 0.298 | 0.300 |
| 7 | 0.100 | 0.160 | 0.203 | 0.234 | 0.255 | 0.270 | 0.281 | 0.288 | 0.293 | 0.296 | 0.298 |
| 8 | 0.106 | 0.166 | 0.208 | 0.237 | 0.257 | 0.271 | 0.281 | 0.288 | 0.292 | 0.294 | 0.295 |
| 9 | 0.111 | 0.170 | 0.211 | 0.239 | 0.259 | 0.272 | 0.281 | 0.286 | 0.290 | 0.291 | 0.292 |
| 10 | 0.114 | 0.173 | 0.213 | 0.241 | 0.259 | 0.272 | 0.280 | 0.285 | 0.288 | 0.289 | 0.288 |
| 11 | 0.117 | 0.175 | 0.215 | 0.241 | 0.259 | 0.271 | 0.278 | 0.283 | 0.285 | 0.286 | 0.285 |
| 12 | 0.120 | 0.177 | 0.216 | 0.242 | 0.259 | 0.270 | 0.277 | 0.281 | 0.282 | 0.282 | 0.281 |
| 13 | 0.121 | 0.178 | 0.216 | 0.241 | 0.258 | 0.269 | 0.275 | 0.278 | 0.280 | 0.279 | 0.278 |
| 14 | 0.122 | 0.179 | 0.216 | 0.241 | 0.257 | 0.267 | 0.273 | 0.276 | 0.277 | 0.276 | 0.274 |
| 15 | 0.123 | 0.179 | 0.216 | 0.240 | 0.256 | 0.265 | 0.271 | 0.274 | 0.274 | 0.273 | 0.270 |
| 16 | 0.124 | 0.179 | 0.216 | 0.239 | 0.254 | 0.264 | 0.269 | 0.271 | 0.271 | 0.270 | 0.267 |
| 17 | 0.124 | 0.179 | 0.215 | 0.238 | 0.253 | 0.262 | 0.267 | 0.268 | 0.268 | 0.266 | 0.263 |


| 18 | 0.124 | 0.179 | 0.214 | 0.237 | 0.251 | 0.260 | 0.264 | 0.266 | 0.265 | 0.263 | 0.260 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.124 | 0.178 | 0.214 | 0.236 | 0.250 | 0.258 | 0.262 | 0.263 | 0.263 | 0.260 | 0.257 |
| 20 | 0.124 | 0.178 | 0.213 | 0.235 | 0.248 | 0.256 | 0.260 | 0.261 | 0.260 | 0.257 | 0.253 |
| 21 | 0.123 | 0.177 | 0.211 | 0.233 | 0.246 | 0.254 | 0.258 | 0.258 | 0.257 | 0.254 | 0.250 |
| 22 | 0.123 | 0.176 | 0.210 | 0.232 | 0.245 | 0.252 | 0.255 | 0.256 | 0.254 | 0.251 | 0.247 |
| 23 | 0.122 | 0.175 | 0.209 | 0.230 | 0.243 | 0.250 | 0.253 | 0.253 | 0.251 | 0.248 | 0.244 |
| 24 | 0.121 | 0.174 | 0.208 | 0.229 | 0.241 | 0.248 | 0.251 | 0.251 | 0.249 | 0.245 | 0.240 |
| 25 | 0.121 | 0.173 | 0.206 | 0.227 | 0.239 | 0.246 | 0.248 | 0.248 | 0.246 | 0.242 | 0.237 |
| 26 | 0.120 | 0.172 | 0.205 | 0.225 | 0.237 | 0.244 | 0.246 | 0.246 | 0.243 | 0.239 | 0.234 |
| 27 | 0.119 | 0.171 | 0.204 | 0.224 | 0.236 | 0.242 | 0.244 | 0.243 | 0.241 | 0.237 | 0.231 |
| 28 | 0.118 | 0.170 | 0.202 | 0.222 | 0.234 | 0.240 | 0.242 | 0.241 | 0.238 | 0.234 | 0.229 |
| 29 | 0.117 | 0.168 | 0.201 | 0.221 | 0.232 | 0.238 | 0.240 | 0.239 | 0.236 | 0.231 | 0.226 |
| 30 | 0.116 | 0.167 | 0.199 | 0.219 | 0.230 | 0.236 | 0.237 | 0.236 | 0.233 | 0.229 | 0.223 |

Table C. 8
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 85 /$ Annual Growth Rate $=0 \%$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.002 | 0.009 | 0.024 | 0.044 | 0.066 | 0.088 | 0.109 | 0.128 | 0.146 | 0.162 |
| 2 | 0.002 | 0.016 | 0.041 | 0.071 | 0.100 | 0.128 | 0.151 | 0.172 | 0.189 | 0.204 | 0.217 |
| 3 | 0.008 | 0.034 | 0.069 | 0.104 | 0.135 | 0.162 | 0.184 | 0.202 | 0.217 | 0.229 | 0.239 |
| 4 | 0.016 | 0.051 | 0.091 | 0.127 | 0.158 | 0.183 | 0.203 | 0.219 | 0.232 | 0.242 | 0.250 |
| 5 | 0.024 | 0.065 | 0.107 | 0.143 | 0.173 | 0.196 | 0.215 | 0.229 | 0.240 | 0.249 | 0.256 |
| 6 | 0.031 | 0.076 | 0.119 | 0.155 | 0.184 | 0.206 | 0.222 | 0.235 | 0.245 | 0.253 | 0.258 |
| 7 | 0.037 | 0.085 | 0.129 | 0.164 | 0.191 | 0.212 | 0.228 | 0.239 | 0.248 | 0.255 | 0.259 |
| 8 | 0.043 | 0.093 | 0.137 | 0.171 | 0.197 | 0.217 | 0.231 | 0.242 | 0.250 | 0.255 | 0.259 |
| 9 | 0.048 | 0.099 | 0.143 | 0.177 | 0.202 | 0.220 | 0.234 | 0.243 | 0.250 | 0.255 | 0.258 |
| 10 | 0.053 | 0.105 | 0.148 | 0.181 | 0.205 | 0.222 | 0.235 | 0.244 | 0.250 | 0.254 | 0.256 |
| 11 | 0.056 | 0.109 | 0.152 | 0.184 | 0.207 | 0.224 | 0.236 | 0.244 | 0.249 | 0.253 | 0.254 |
| 12 | 0.060 | 0.113 | 0.155 | 0.186 | 0.209 | 0.225 | 0.236 | 0.244 | 0.248 | 0.251 | 0.252 |
| 13 | 0.062 | 0.116 | 0.158 | 0.188 | 0.210 | 0.225 | 0.236 | 0.243 | 0.247 | 0.249 | 0.250 |
| 14 | 0.065 | 0.118 | 0.160 | 0.190 | 0.211 | 0.225 | 0.235 | 0.242 | 0.246 | 0.247 | 0.248 |
| 15 | 0.067 | 0.120 | 0.161 | 0.191 | 0.211 | 0.225 | 0.235 | 0.241 | 0.244 | 0.245 | 0.245 |
| 16 | 0.069 | 0.122 | 0.162 | 0.191 | 0.211 | 0.225 | 0.234 | 0.239 | 0.242 | 0.243 | 0.242 |
| 17 | 0.070 | 0.123 | 0.163 | 0.192 | 0.211 | 0.224 | 0.233 | 0.238 | 0.240 | 0.241 | 0.240 |


| 18 | 0.071 | 0.124 | 0.164 | 0.192 | 0.211 | 0.224 | 0.232 | 0.236 | 0.238 | 0.239 | 0.237 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.072 | 0.125 | 0.165 | 0.192 | 0.210 | 0.223 | 0.230 | 0.235 | 0.236 | 0.236 | 0.235 |
| 20 | 0.073 | 0.126 | 0.165 | 0.192 | 0.210 | 0.222 | 0.229 | 0.233 | 0.234 | 0.234 | 0.232 |
| 21 | 0.074 | 0.126 | 0.165 | 0.191 | 0.209 | 0.221 | 0.228 | 0.231 | 0.232 | 0.232 | 0.229 |
| 22 | 0.074 | 0.127 | 0.165 | 0.191 | 0.208 | 0.219 | 0.226 | 0.229 | 0.230 | 0.229 | 0.227 |
| 23 | 0.075 | 0.127 | 0.165 | 0.191 | 0.208 | 0.218 | 0.225 | 0.228 | 0.228 | 0.227 | 0.224 |
| 24 | 0.075 | 0.127 | 0.165 | 0.190 | 0.207 | 0.217 | 0.223 | 0.226 | 0.226 | 0.224 | 0.222 |
| 25 | 0.075 | 0.127 | 0.164 | 0.189 | 0.206 | 0.216 | 0.221 | 0.224 | 0.224 | 0.222 | 0.219 |
| 26 | 0.076 | 0.127 | 0.164 | 0.189 | 0.205 | 0.214 | 0.220 | 0.222 | 0.222 | 0.220 | 0.216 |
| 27 | 0.076 | 0.127 | 0.163 | 0.188 | 0.203 | 0.213 | 0.218 | 0.220 | 0.220 | 0.218 | 0.214 |
| 28 | 0.076 | 0.127 | 0.163 | 0.187 | 0.202 | 0.212 | 0.217 | 0.218 | 0.218 | 0.215 | 0.212 |
| 29 | 0.076 | 0.126 | 0.162 | 0.186 | 0.201 | 0.210 | 0.215 | 0.216 | 0.216 | 0.213 | 0.209 |
| 30 | 0.075 | 0.126 | 0.162 | 0.185 | 0.200 | 0.209 | 0.213 | 0.215 | 0.214 | 0.211 | 0.207 |

Table C. 9
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 80 /$ Annual Growth Rate $=\mathbf{0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.001 | 0.004 | 0.010 | 0.021 | 0.034 | 0.049 | 0.065 | 0.080 | 0.095 |
| 2 | 0.000 | 0.002 | 0.010 | 0.025 | 0.044 | 0.066 | 0.087 | 0.107 | 0.125 | 0.141 | 0.156 |
| 3 | 0.001 | 0.008 | 0.025 | 0.048 | 0.074 | 0.098 | 0.121 | 0.141 | 0.158 | 0.173 | 0.185 |
| 4 | 0.002 | 0.015 | 0.039 | 0.068 | 0.096 | 0.121 | 0.143 | 0.162 | 0.178 | 0.191 | 0.202 |
| 5 | 0.005 | 0.023 | 0.053 | 0.084 | 0.113 | 0.138 | 0.159 | 0.176 | 0.190 | 0.202 | 0.212 |
| 6 | 0.007 | 0.031 | 0.064 | 0.097 | 0.126 | 0.150 | 0.170 | 0.186 | 0.199 | 0.209 | 0.218 |
| 7 | 0.010 | 0.039 | 0.074 | 0.107 | 0.136 | 0.159 | 0.178 | 0.193 | 0.205 | 0.214 | 0.221 |
| 8 | 0.014 | 0.045 | 0.082 | 0.116 | 0.144 | 0.166 | 0.184 | 0.198 | 0.209 | 0.217 | 0.223 |
| 9 | 0.017 | 0.051 | 0.089 | 0.123 | 0.150 | 0.172 | 0.189 | 0.202 | 0.212 | 0.219 | 0.224 |
| 10 | 0.020 | 0.056 | 0.095 | 0.128 | 0.155 | 0.176 | 0.192 | 0.204 | 0.213 | 0.220 | 0.225 |
| 11 | 0.022 | 0.061 | 0.100 | 0.133 | 0.159 | 0.179 | 0.195 | 0.206 | 0.214 | 0.220 | 0.224 |
| 12 | 0.025 | 0.065 | 0.104 | 0.137 | 0.163 | 0.182 | 0.196 | 0.207 | 0.215 | 0.220 | 0.223 |
| 13 | 0.027 | 0.068 | 0.108 | 0.140 | 0.165 | 0.184 | 0.198 | 0.208 | 0.215 | 0.220 | 0.222 |
| 14 | 0.029 | 0.071 | 0.111 | 0.143 | 0.167 | 0.186 | 0.199 | 0.208 | 0.215 | 0.219 | 0.221 |
| 15 | 0.031 | 0.074 | 0.114 | 0.145 | 0.169 | 0.187 | 0.199 | 0.208 | 0.214 | 0.218 | 0.220 |
| 16 | 0.033 | 0.077 | 0.116 | 0.147 | 0.171 | 0.187 | 0.200 | 0.208 | 0.213 | 0.217 | 0.218 |
| 17 | 0.035 | 0.079 | 0.118 | 0.149 | 0.172 | 0.188 | 0.200 | 0.207 | 0.212 | 0.215 | 0.216 |


| 18 | 0.036 | 0.081 | 0.120 | 0.150 | 0.172 | 0.188 | 0.199 | 0.207 | 0.211 | 0.214 | 0.214 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.038 | 0.082 | 0.121 | 0.151 | 0.173 | 0.188 | 0.199 | 0.206 | 0.210 | 0.212 | 0.212 |
| 20 | 0.039 | 0.084 | 0.122 | 0.152 | 0.173 | 0.188 | 0.199 | 0.205 | 0.209 | 0.211 | 0.211 |
| 21 | 0.040 | 0.085 | 0.124 | 0.153 | 0.174 | 0.188 | 0.198 | 0.204 | 0.208 | 0.209 | 0.209 |
| 22 | 0.041 | 0.086 | 0.124 | 0.153 | 0.174 | 0.188 | 0.197 | 0.203 | 0.206 | 0.207 | 0.207 |
| 23 | 0.042 | 0.087 | 0.125 | 0.153 | 0.174 | 0.187 | 0.196 | 0.202 | 0.205 | 0.205 | 0.204 |
| 24 | 0.042 | 0.088 | 0.126 | 0.154 | 0.173 | 0.187 | 0.196 | 0.201 | 0.203 | 0.204 | 0.202 |
| 25 | 0.043 | 0.088 | 0.126 | 0.154 | 0.173 | 0.186 | 0.195 | 0.200 | 0.202 | 0.202 | 0.200 |
| 26 | 0.044 | 0.089 | 0.126 | 0.154 | 0.173 | 0.186 | 0.194 | 0.198 | 0.200 | 0.200 | 0.198 |
| 27 | 0.044 | 0.089 | 0.127 | 0.154 | 0.172 | 0.185 | 0.193 | 0.197 | 0.199 | 0.198 | 0.196 |
| 28 | 0.045 | 0.090 | 0.127 | 0.153 | 0.172 | 0.184 | 0.192 | 0.196 | 0.197 | 0.196 | 0.194 |
| 29 | 0.045 | 0.090 | 0.127 | 0.153 | 0.171 | 0.183 | 0.191 | 0.194 | 0.195 | 0.195 | 0.192 |
| 30 | 0.045 | 0.090 | 0.127 | 0.153 | 0.171 | 0.182 | 0.189 | 0.193 | 0.194 | 0.193 | 0.190 |

Table C. 10
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 120 /$ Annual Growth Rate $=\mathbf{5 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.000 | 0.999 | 0.991 | 0.975 | 0.952 | 0.925 | 0.898 | 0.870 | 0.844 | 0.819 | 0.796 |
| 2 | 0.996 | 0.975 | 0.940 | 0.899 | 0.859 | 0.822 | 0.788 | 0.758 | 0.732 | 0.708 | 0.686 |
| 3 | 0.979 | 0.933 | 0.880 | 0.831 | 0.787 | 0.750 | 0.718 | 0.689 | 0.665 | 0.643 | 0.623 |
| 4 | 0.949 | 0.886 | 0.826 | 0.775 | 0.732 | 0.697 | 0.667 | 0.641 | 0.618 | 0.598 | 0.579 |
| 5 | 0.913 | 0.840 | 0.778 | 0.728 | 0.688 | 0.655 | 0.627 | 0.603 | 0.582 | 0.563 | 0.546 |
| 6 | 0.874 | 0.797 | 0.736 | 0.689 | 0.652 | 0.621 | 0.595 | 0.573 | 0.553 | 0.535 | 0.519 |
| 7 | 0.835 | 0.757 | 0.700 | 0.656 | 0.621 | 0.593 | 0.568 | 0.547 | 0.528 | 0.511 | 0.496 |
| 8 | 0.796 | 0.721 | 0.667 | 0.626 | 0.594 | 0.568 | 0.545 | 0.525 | 0.507 | 0.491 | 0.476 |
| 9 | 0.759 | 0.688 | 0.638 | 0.600 | 0.571 | 0.546 | 0.524 | 0.506 | 0.489 | 0.473 | 0.459 |
| 10 | 0.724 | 0.657 | 0.611 | 0.577 | 0.549 | 0.526 | 0.506 | 0.488 | 0.472 | 0.457 | 0.443 |
| 11 | 0.690 | 0.629 | 0.587 | 0.556 | 0.530 | 0.508 | 0.490 | 0.472 | 0.457 | 0.442 | 0.428 |
| 12 | 0.658 | 0.603 | 0.565 | 0.536 | 0.513 | 0.492 | 0.474 | 0.458 | 0.443 | 0.429 | 0.415 |
| 13 | 0.628 | 0.579 | 0.545 | 0.518 | 0.496 | 0.477 | 0.460 | 0.445 | 0.430 | 0.416 | 0.403 |
| 14 | 0.600 | 0.556 | 0.526 | 0.502 | 0.482 | 0.464 | 0.448 | 0.432 | 0.418 | 0.405 | 0.392 |
| 15 | 0.573 | 0.535 | 0.508 | 0.486 | 0.468 | 0.451 | 0.435 | 0.421 | 0.407 | 0.394 | 0.381 |
| 16 | 0.547 | 0.516 | 0.492 | 0.472 | 0.455 | 0.439 | 0.424 | 0.410 | 0.397 | 0.384 | 0.372 |
| 17 | 0.524 | 0.497 | 0.476 | 0.458 | 0.442 | 0.428 | 0.414 | 0.400 | 0.387 | 0.374 | 0.362 |


| 18 | 0.501 | 0.479 | 0.462 | 0.446 | 0.431 | 0.417 | 0.404 | 0.391 | 0.378 | 0.365 | 0.353 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.480 | 0.463 | 0.448 | 0.434 | 0.420 | 0.407 | 0.394 | 0.381 | 0.369 | 0.357 | 0.345 |
| 20 | 0.459 | 0.447 | 0.435 | 0.422 | 0.410 | 0.397 | 0.385 | 0.373 | 0.361 | 0.349 | 0.337 |
| 21 | 0.440 | 0.432 | 0.422 | 0.411 | 0.400 | 0.388 | 0.376 | 0.365 | 0.353 | 0.341 | 0.329 |
| 22 | 0.422 | 0.418 | 0.410 | 0.401 | 0.391 | 0.380 | 0.368 | 0.357 | 0.345 | 0.334 | 0.322 |
| 23 | 0.405 | 0.405 | 0.399 | 0.391 | 0.382 | 0.371 | 0.360 | 0.349 | 0.338 | 0.326 | 0.315 |
| 24 | 0.388 | 0.392 | 0.388 | 0.382 | 0.373 | 0.363 | 0.353 | 0.342 | 0.331 | 0.320 | 0.308 |
| 25 | 0.373 | 0.380 | 0.378 | 0.373 | 0.365 | 0.356 | 0.346 | 0.335 | 0.324 | 0.313 | 0.302 |
| 26 | 0.358 | 0.368 | 0.368 | 0.364 | 0.357 | 0.348 | 0.339 | 0.328 | 0.318 | 0.307 | 0.296 |
| 27 | 0.344 | 0.357 | 0.359 | 0.356 | 0.350 | 0.341 | 0.332 | 0.322 | 0.312 | 0.301 | 0.290 |
| 28 | 0.330 | 0.346 | 0.350 | 0.348 | 0.342 | 0.335 | 0.326 | 0.316 | 0.306 | 0.295 | 0.284 |
| 29 | 0.318 | 0.336 | 0.341 | 0.340 | 0.335 | 0.328 | 0.319 | 0.310 | 0.300 | 0.289 | 0.278 |
| 20 | 0.305 | 0.326 | 0.333 | 0.333 | 0.328 | 0.322 | 0.313 | 0.304 | 0.294 | 0.284 | 0.273 |

Table C. 11
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 115 /$ Annual Growth Rate $=5 \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 8 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.999 | 0.987 | 0.962 | 0.929 | 0.893 | 0.858 | 0.826 | 0.797 | 0.771 | 0.748 | 0.726 |
| 2 | 0.975 | 0.926 | 0.873 | 0.824 | 0.782 | 0.746 | 0.715 | 0.689 | 0.666 | 0.646 | 0.627 |
| 3 | 0.928 | 0.858 | 0.798 | 0.750 | 0.710 | 0.678 | 0.650 | 0.627 | 0.607 | 0.589 | 0.573 |
| 4 | 0.874 | 0.798 | 0.740 | 0.694 | 0.659 | 0.630 | 0.605 | 0.584 | 0.566 | 0.550 | 0.535 |
| 5 | 0.822 | 0.746 | 0.692 | 0.651 | 0.619 | 0.593 | 0.571 | 0.552 | 0.535 | 0.519 | 0.506 |
| 6 | 0.772 | 0.701 | 0.652 | 0.615 | 0.587 | 0.563 | 0.543 | 0.525 | 0.509 | 0.495 | 0.482 |
| 7 | 0.727 | 0.662 | 0.618 | 0.585 | 0.559 | 0.538 | 0.519 | 0.503 | 0.488 | 0.474 | 0.462 |
| 8 | 0.685 | 0.627 | 0.588 | 0.559 | 0.536 | 0.516 | 0.499 | 0.483 | 0.469 | 0.456 | 0.444 |
| 9 | 0.646 | 0.596 | 0.562 | 0.536 | 0.515 | 0.497 | 0.481 | 0.466 | 0.453 | 0.441 | 0.429 |
| 10 | 0.611 | 0.568 | 0.539 | 0.515 | 0.496 | 0.480 | 0.465 | 0.451 | 0.438 | 0.426 | 0.415 |
| 11 | 0.579 | 0.543 | 0.517 | 0.497 | 0.480 | 0.464 | 0.450 | 0.437 | 0.425 | 0.413 | 0.402 |
| 12 | 0.549 | 0.519 | 0.498 | 0.480 | 0.464 | 0.450 | 0.437 | 0.424 | 0.413 | 0.401 | 0.390 |
| 13 | 0.521 | 0.498 | 0.480 | 0.464 | 0.450 | 0.437 | 0.425 | 0.413 | 0.401 | 0.390 | 0.379 |
| 14 | 0.496 | 0.478 | 0.463 | 0.450 | 0.437 | 0.425 | 0.413 | 0.402 | 0.391 | 0.380 | 0.369 |
| 15 | 0.472 | 0.459 | 0.448 | 0.436 | 0.425 | 0.413 | 0.402 | 0.391 | 0.381 | 0.370 | 0.359 |
| 16 | 0.450 | 0.442 | 0.433 | 0.423 | 0.413 | 0.403 | 0.392 | 0.382 | 0.371 | 0.361 | 0.350 |
| 17 | 0.429 | 0.426 | 0.420 | 0.412 | 0.403 | 0.393 | 0.383 | 0.373 | 0.362 | 0.352 | 0.342 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.409 | 0.411 | 0.407 | 0.400 | 0.392 | 0.383 | 0.374 | 0.364 | 0.354 | 0.344 | 0.334 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.391 | 0.396 | 0.395 | 0.390 | 0.383 | 0.374 | 0.365 | 0.356 | 0.346 | 0.336 | 0.326 |
| 20 | 0.374 | 0.383 | 0.383 | 0.380 | 0.374 | 0.366 | 0.357 | 0.348 | 0.339 | 0.329 | 0.319 |
| 21 | 0.358 | 0.370 | 0.373 | 0.370 | 0.365 | 0.358 | 0.350 | 0.341 | 0.331 | 0.322 | 0.312 |
| 22 | 0.342 | 0.358 | 0.362 | 0.361 | 0.357 | 0.350 | 0.342 | 0.334 | 0.324 | 0.315 | 0.305 |
| 23 | 0.328 | 0.346 | 0.353 | 0.352 | 0.349 | 0.343 | 0.335 | 0.327 | 0.318 | 0.308 | 0.298 |
| 24 | 0.314 | 0.335 | 0.343 | 0.344 | 0.341 | 0.336 | 0.328 | 0.320 | 0.311 | 0.302 | 0.292 |
| 25 | 0.301 | 0.325 | 0.334 | 0.336 | 0.334 | 0.329 | 0.322 | 0.314 | 0.305 | 0.296 | 0.286 |
| 26 | 0.289 | 0.315 | 0.326 | 0.329 | 0.327 | 0.322 | 0.316 | 0.308 | 0.299 | 0.290 | 0.280 |
| 27 | 0.277 | 0.305 | 0.317 | 0.321 | 0.320 | 0.316 | 0.310 | 0.302 | 0.294 | 0.284 | 0.275 |
| 28 | 0.266 | 0.296 | 0.310 | 0.314 | 0.314 | 0.310 | 0.304 | 0.296 | 0.288 | 0.279 | 0.270 |
| 29 | 0.256 | 0.287 | 0.302 | 0.307 | 0.307 | 0.304 | 0.298 | 0.291 | 0.283 | 0.274 | 0.264 |
| 20 | 0.245 | 0.279 | 0.295 | 0.301 | 0.301 | 0.298 | 0.293 | 0.286 | 0.277 | 0.269 | 0.259 |

Table C. 12
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 110 /$ Annual Growth Rate $=5 \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.975 | 0.928 | 0.876 | 0.829 | 0.789 | 0.754 | 0.725 | 0.700 | 0.678 | 0.659 | 0.643 |
| 2 | 0.890 | 0.816 | 0.759 | 0.715 | 0.680 | 0.652 | 0.628 | 0.608 | 0.591 | 0.576 | 0.563 |
| 3 | 0.807 | 0.735 | 0.684 | 0.647 | 0.618 | 0.594 | 0.575 | 0.558 | 0.543 | 0.530 | 0.518 |
| 4 | 0.737 | 0.674 | 0.631 | 0.599 | 0.575 | 0.555 | 0.538 | 0.523 | 0.510 | 0.498 | 0.487 |
| 5 | 0.678 | 0.625 | 0.589 | 0.563 | 0.542 | 0.525 | 0.510 | 0.497 | 0.485 | 0.474 | 0.463 |
| 6 | 0.628 | 0.585 | 0.556 | 0.533 | 0.516 | 0.500 | 0.487 | 0.475 | 0.464 | 0.453 | 0.443 |
| 7 | 0.585 | 0.551 | 0.527 | 0.509 | 0.493 | 0.480 | 0.468 | 0.456 | 0.446 | 0.436 | 0.426 |
| 8 | 0.547 | 0.521 | 0.502 | 0.487 | 0.474 | 0.462 | 0.451 | 0.440 | 0.430 | 0.421 | 0.411 |
| 9 | 0.513 | 0.495 | 0.480 | 0.468 | 0.456 | 0.446 | 0.436 | 0.426 | 0.416 | 0.407 | 0.398 |
| 10 | 0.483 | 0.472 | 0.461 | 0.451 | 0.441 | 0.431 | 0.422 | 0.413 | 0.404 | 0.395 | 0.386 |
| 11 | 0.456 | 0.450 | 0.443 | 0.435 | 0.427 | 0.418 | 0.410 | 0.401 | 0.392 | 0.383 | 0.374 |
| 12 | 0.431 | 0.431 | 0.427 | 0.421 | 0.414 | 0.406 | 0.398 | 0.390 | 0.381 | 0.373 | 0.364 |
| 13 | 0.409 | 0.413 | 0.412 | 0.408 | 0.402 | 0.395 | 0.388 | 0.380 | 0.371 | 0.363 | 0.354 |
| 14 | 0.388 | 0.397 | 0.398 | 0.396 | 0.391 | 0.385 | 0.378 | 0.370 | 0.362 | 0.354 | 0.345 |
| 15 | 0.369 | 0.382 | 0.386 | 0.385 | 0.381 | 0.375 | 0.369 | 0.361 | 0.353 | 0.345 | 0.337 |
| 17 | 0.351 | 0.368 | 0.374 | 0.374 | 0.371 | 0.366 | 0.360 | 0.353 | 0.345 | 0.337 | 0.329 |


| 18 | 0.319 | 0.342 | 0.352 | 0.354 | 0.353 | 0.349 | 0.344 | 0.337 | 0.330 | 0.322 | 0.314 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.304 | 0.330 | 0.342 | 0.345 | 0.345 | 0.342 | 0.336 | 0.330 | 0.323 | 0.315 | 0.307 |
| 20 | 0.291 | 0.319 | 0.332 | 0.337 | 0.337 | 0.334 | 0.329 | 0.323 | 0.316 | 0.308 | 0.300 |
| 21 | 0.278 | 0.309 | 0.323 | 0.329 | 0.329 | 0.327 | 0.322 | 0.316 | 0.309 | 0.302 | 0.294 |
| 22 | 0.266 | 0.299 | 0.314 | 0.321 | 0.322 | 0.320 | 0.316 | 0.310 | 0.303 | 0.296 | 0.287 |
| 23 | 0.255 | 0.289 | 0.306 | 0.314 | 0.315 | 0.314 | 0.310 | 0.304 | 0.297 | 0.290 | 0.282 |
| 24 | 0.244 | 0.280 | 0.298 | 0.306 | 0.309 | 0.307 | 0.304 | 0.298 | 0.291 | 0.284 | 0.276 |
| 25 | 0.234 | 0.272 | 0.291 | 0.300 | 0.302 | 0.301 | 0.298 | 0.292 | 0.286 | 0.278 | 0.270 |
| 26 | 0.224 | 0.263 | 0.283 | 0.293 | 0.296 | 0.296 | 0.292 | 0.287 | 0.280 | 0.273 | 0.265 |
| 27 | 0.215 | 0.256 | 0.276 | 0.287 | 0.290 | 0.290 | 0.287 | 0.282 | 0.275 | 0.268 | 0.260 |
| 28 | 0.206 | 0.248 | 0.270 | 0.281 | 0.285 | 0.284 | 0.281 | 0.277 | 0.270 | 0.263 | 0.255 |
| 29 | 0.198 | 0.241 | 0.263 | 0.275 | 0.279 | 0.279 | 0.276 | 0.272 | 0.265 | 0.258 | 0.250 |
| 20 | 0.190 | 0.234 | 0.257 | 0.269 | 0.274 | 0.274 | 0.272 | 0.267 | 0.261 | 0.253 | 0.246 |

Table C. 13
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 105 /$ Annual Growth Rate $=5 \%$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.814 | 0.745 | 0.696 | 0.661 | 0.634 | 0.612 | 0.595 | 0.580 | 0.568 | 0.557 | 0.547 |
| 2 | 0.680 | 0.630 | 0.598 | 0.574 | 0.556 | 0.542 | 0.529 | 0.519 | 0.509 | 0.501 | 0.493 |
| 3 | 0.597 | 0.565 | 0.543 | 0.527 | 0.514 | 0.503 | 0.493 | 0.484 | 0.476 | 0.468 | 0.461 |
| 4 | 0.539 | 0.519 | 0.505 | 0.493 | 0.484 | 0.475 | 0.467 | 0.459 | 0.452 | 0.445 | 0.438 |
| 5 | 0.493 | 0.483 | 0.475 | 0.467 | 0.460 | 0.453 | 0.446 | 0.440 | 0.433 | 0.426 | 0.420 |
| 6 | 0.456 | 0.454 | 0.451 | 0.446 | 0.441 | 0.435 | 0.429 | 0.423 | 0.417 | 0.410 | 0.404 |
| 7 | 0.424 | 0.430 | 0.430 | 0.428 | 0.424 | 0.420 | 0.414 | 0.409 | 0.403 | 0.396 | 0.390 |
| 8 | 0.397 | 0.408 | 0.412 | 0.412 | 0.410 | 0.406 | 0.401 | 0.396 | 0.390 | 0.384 | 0.378 |
| 9 | 0.373 | 0.389 | 0.396 | 0.398 | 0.396 | 0.393 | 0.389 | 0.384 | 0.379 | 0.373 | 0.366 |
| 10 | 0.351 | 0.372 | 0.381 | 0.385 | 0.384 | 0.382 | 0.378 | 0.374 | 0.368 | 0.362 | 0.356 |
| 11 | 0.332 | 0.357 | 0.368 | 0.373 | 0.373 | 0.372 | 0.368 | 0.364 | 0.359 | 0.353 | 0.347 |
| 12 | 0.315 | 0.342 | 0.356 | 0.362 | 0.363 | 0.362 | 0.359 | 0.355 | 0.350 | 0.344 | 0.338 |
| 13 | 0.298 | 0.329 | 0.344 | 0.351 | 0.354 | 0.353 | 0.350 | 0.346 | 0.341 | 0.335 | 0.329 |
| 14 | 0.284 | 0.317 | 0.334 | 0.342 | 0.345 | 0.345 | 0.342 | 0.338 | 0.333 | 0.328 | 0.321 |
| 15 | 0.270 | 0.306 | 0.324 | 0.333 | 0.336 | 0.337 | 0.334 | 0.331 | 0.326 | 0.320 | 0.314 |
| 16 | 0.257 | 0.295 | 0.314 | 0.324 | 0.328 | 0.329 | 0.327 | 0.323 | 0.319 | 0.313 | 0.307 |
| 17 | 0.245 | 0.285 | 0.306 | 0.316 | 0.321 | 0.322 | 0.320 | 0.317 | 0.312 | 0.306 | 0.300 |


| 18 | 0.234 | 0.275 | 0.297 | 0.309 | 0.314 | 0.315 | 0.313 | 0.310 | 0.305 | 0.300 | 0.293 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.224 | 0.266 | 0.289 | 0.301 | 0.307 | 0.308 | 0.307 | 0.304 | 0.299 | 0.293 | 0.287 |
| 20 | 0.214 | 0.258 | 0.282 | 0.294 | 0.300 | 0.302 | 0.301 | 0.298 | 0.293 | 0.287 | 0.281 |
| 21 | 0.205 | 0.250 | 0.274 | 0.288 | 0.294 | 0.296 | 0.295 | 0.292 | 0.287 | 0.282 | 0.275 |
| 22 | 0.196 | 0.242 | 0.267 | 0.281 | 0.288 | 0.290 | 0.289 | 0.286 | 0.282 | 0.276 | 0.270 |
| 23 | 0.188 | 0.235 | 0.261 | 0.275 | 0.282 | 0.285 | 0.284 | 0.281 | 0.276 | 0.271 | 0.264 |
| 24 | 0.181 | 0.228 | 0.254 | 0.269 | 0.276 | 0.279 | 0.279 | 0.276 | 0.271 | 0.266 | 0.259 |
| 25 | 0.173 | 0.221 | 0.248 | 0.263 | 0.271 | 0.274 | 0.273 | 0.271 | 0.266 | 0.261 | 0.254 |
| 26 | 0.166 | 0.214 | 0.242 | 0.258 | 0.266 | 0.269 | 0.269 | 0.266 | 0.261 | 0.256 | 0.249 |
| 27 | 0.160 | 0.208 | 0.237 | 0.253 | 0.261 | 0.264 | 0.264 | 0.261 | 0.257 | 0.251 | 0.245 |
| 28 | 0.153 | 0.202 | 0.231 | 0.247 | 0.256 | 0.259 | 0.259 | 0.257 | 0.252 | 0.247 | 0.240 |
| 29 | 0.147 | 0.197 | 0.226 | 0.242 | 0.251 | 0.255 | 0.255 | 0.252 | 0.248 | 0.242 | 0.236 |
| 20 | 0.142 | 0.191 | 0.221 | 0.238 | 0.247 | 0.250 | 0.250 | 0.248 | 0.244 | 0.238 | 0.231 |

Table C. 14
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 100 /$ Annual Growth Rate $=5 \%$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.408 | 0.426 | 0.435 | 0.441 | 0.444 | 0.445 | 0.446 | 0.446 | 0.445 | 0.445 | 0.443 |
| 2 | 0.371 | 0.395 | 0.409 | 0.416 | 0.421 | 0.423 | 0.424 | 0.424 | 0.423 | 0.422 | 0.420 |
| 3 | 0.343 | 0.373 | 0.389 | 0.398 | 0.403 | 0.406 | 0.407 | 0.407 | 0.406 | 0.405 | 0.402 |
| 4 | 0.320 | 0.354 | 0.372 | 0.383 | 0.389 | 0.392 | 0.393 | 0.393 | 0.392 | 0.390 | 0.388 |
| 5 | 0.301 | 0.337 | 0.358 | 0.369 | 0.376 | 0.380 | 0.381 | 0.381 | 0.380 | 0.378 | 0.375 |
| 6 | 0.284 | 0.323 | 0.345 | 0.357 | 0.365 | 0.368 | 0.370 | 0.370 | 0.368 | 0.366 | 0.363 |
| 7 | 0.269 | 0.310 | 0.333 | 0.347 | 0.354 | 0.358 | 0.360 | 0.360 | 0.358 | 0.356 | 0.353 |
| 8 | 0.255 | 0.298 | 0.322 | 0.337 | 0.345 | 0.349 | 0.351 | 0.351 | 0.349 | 0.347 | 0.343 |
| 9 | 0.242 | 0.287 | 0.312 | 0.327 | 0.336 | 0.340 | 0.342 | 0.342 | 0.340 | 0.338 | 0.334 |
| 10 | 0.230 | 0.276 | 0.303 | 0.319 | 0.328 | 0.332 | 0.334 | 0.334 | 0.332 | 0.330 | 0.326 |
| 11 | 0.219 | 0.267 | 0.294 | 0.310 | 0.320 | 0.325 | 0.327 | 0.326 | 0.325 | 0.322 | 0.318 |
| 12 | 0.209 | 0.258 | 0.286 | 0.303 | 0.312 | 0.317 | 0.319 | 0.319 | 0.317 | 0.314 | 0.311 |
| 13 | 0.200 | 0.249 | 0.278 | 0.295 | 0.305 | 0.311 | 0.313 | 0.312 | 0.311 | 0.307 | 0.303 |
| 14 | 0.191 | 0.241 | 0.271 | 0.288 | 0.299 | 0.304 | 0.306 | 0.306 | 0.304 | 0.301 | 0.297 |
| 15 | 0.183 | 0.234 | 0.264 | 0.282 | 0.292 | 0.298 | 0.300 | 0.300 | 0.298 | 0.294 | 0.290 |
| 16 | 0.175 | 0.226 | 0.257 | 0.275 | 0.286 | 0.292 | 0.294 | 0.294 | 0.292 | 0.288 | 0.284 |
| 17 | 0.168 | 0.220 | 0.251 | 0.269 | 0.280 | 0.286 | 0.288 | 0.288 | 0.286 | 0.283 | 0.278 |


| 18 | 0.161 | 0.213 | 0.244 | 0.263 | 0.275 | 0.280 | 0.283 | 0.282 | 0.280 | 0.277 | 0.272 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.155 | 0.207 | 0.239 | 0.258 | 0.269 | 0.275 | 0.277 | 0.277 | 0.275 | 0.272 | 0.267 |
| 20 | 0.148 | 0.201 | 0.233 | 0.252 | 0.264 | 0.270 | 0.272 | 0.272 | 0.270 | 0.266 | 0.262 |
| 21 | 0.142 | 0.195 | 0.227 | 0.247 | 0.259 | 0.265 | 0.267 | 0.267 | 0.265 | 0.261 | 0.257 |
| 22 | 0.137 | 0.189 | 0.222 | 0.242 | 0.254 | 0.260 | 0.263 | 0.262 | 0.260 | 0.256 | 0.252 |
| 23 | 0.132 | 0.184 | 0.217 | 0.237 | 0.249 | 0.255 | 0.258 | 0.258 | 0.255 | 0.252 | 0.247 |
| 24 | 0.126 | 0.179 | 0.212 | 0.232 | 0.244 | 0.251 | 0.253 | 0.253 | 0.251 | 0.247 | 0.242 |
| 25 | 0.122 | 0.174 | 0.207 | 0.228 | 0.240 | 0.246 | 0.249 | 0.249 | 0.246 | 0.243 | 0.238 |
| 26 | 0.117 | 0.169 | 0.203 | 0.223 | 0.236 | 0.242 | 0.245 | 0.245 | 0.242 | 0.238 | 0.233 |
| 27 | 0.113 | 0.165 | 0.198 | 0.219 | 0.232 | 0.238 | 0.241 | 0.240 | 0.238 | 0.234 | 0.229 |
| 28 | 0.108 | 0.160 | 0.194 | 0.215 | 0.227 | 0.234 | 0.237 | 0.236 | 0.234 | 0.230 | 0.225 |
| 29 | 0.104 | 0.156 | 0.190 | 0.211 | 0.223 | 0.230 | 0.233 | 0.233 | 0.230 | 0.226 | 0.221 |
| 20 | 0.101 | 0.152 | 0.186 | 0.207 | 0.220 | 0.226 | 0.229 | 0.229 | 0.226 | 0.222 | 0.217 |

Table C. 15
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 95 /$ Annual Growth Rate $=\mathbf{5 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.078 | 0.141 | 0.191 | 0.229 | 0.258 | 0.281 | 0.298 | 0.312 | 0.323 | 0.332 | 0.339 |
| 2 | 0.121 | 0.186 | 0.232 | 0.264 | 0.288 | 0.306 | 0.319 | 0.329 | 0.336 | 0.342 | 0.346 |
| 3 | 0.138 | 0.201 | 0.244 | 0.274 | 0.295 | 0.311 | 0.322 | 0.330 | 0.336 | 0.340 | 0.343 |
| 4 | 0.145 | 0.206 | 0.248 | 0.276 | 0.296 | 0.310 | 0.320 | 0.327 | 0.332 | 0.335 | 0.337 |
| 5 | 0.146 | 0.207 | 0.247 | 0.275 | 0.294 | 0.307 | 0.316 | 0.322 | 0.326 | 0.328 | 0.330 |
| 6 | 0.146 | 0.205 | 0.245 | 0.272 | 0.290 | 0.303 | 0.311 | 0.317 | 0.320 | 0.322 | 0.322 |
| 7 | 0.143 | 0.203 | 0.242 | 0.268 | 0.286 | 0.298 | 0.306 | 0.311 | 0.314 | 0.315 | 0.315 |
| 8 | 0.140 | 0.199 | 0.238 | 0.264 | 0.281 | 0.293 | 0.301 | 0.305 | 0.308 | 0.309 | 0.308 |
| 9 | 0.137 | 0.195 | 0.234 | 0.260 | 0.277 | 0.288 | 0.295 | 0.300 | 0.302 | 0.302 | 0.302 |
| 10 | 0.133 | 0.191 | 0.229 | 0.255 | 0.272 | 0.283 | 0.290 | 0.294 | 0.296 | 0.296 | 0.295 |
| 11 | 0.129 | 0.187 | 0.225 | 0.250 | 0.267 | 0.278 | 0.285 | 0.289 | 0.290 | 0.290 | 0.289 |
| 12 | 0.125 | 0.182 | 0.221 | 0.246 | 0.262 | 0.273 | 0.280 | 0.283 | 0.285 | 0.285 | 0.283 |
| 13 | 0.121 | 0.178 | 0.216 | 0.241 | 0.258 | 0.268 | 0.275 | 0.278 | 0.280 | 0.279 | 0.278 |
| 14 | 0.117 | 0.174 | 0.212 | 0.237 | 0.253 | 0.264 | 0.270 | 0.273 | 0.274 | 0.274 | 0.272 |
| 15 | 0.113 | 0.170 | 0.207 | 0.233 | 0.249 | 0.259 | 0.265 | 0.269 | 0.269 | 0.269 | 0.267 |
| 17 | 0.109 | 0.165 | 0.203 | 0.228 | 0.245 | 0.255 | 0.261 | 0.264 | 0.265 | 0.264 | 0.261 |
| 106 | 0.161 | 0.199 | 0.224 | 0.240 | 0.250 | 0.256 | 0.259 | 0.260 | 0.259 | 0.256 |  |


| 18 | 0.102 | 0.157 | 0.195 | 0.220 | 0.236 | 0.246 | 0.252 | 0.255 | 0.255 | 0.254 | 0.252 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.099 | 0.153 | 0.191 | 0.216 | 0.232 | 0.242 | 0.248 | 0.251 | 0.251 | 0.249 | 0.247 |
| 20 | 0.095 | 0.150 | 0.187 | 0.212 | 0.228 | 0.238 | 0.244 | 0.246 | 0.247 | 0.245 | 0.242 |
| 21 | 0.092 | 0.146 | 0.183 | 0.208 | 0.224 | 0.234 | 0.240 | 0.242 | 0.242 | 0.241 | 0.238 |
| 22 | 0.089 | 0.142 | 0.180 | 0.204 | 0.220 | 0.230 | 0.236 | 0.238 | 0.238 | 0.237 | 0.233 |
| 23 | 0.086 | 0.139 | 0.176 | 0.201 | 0.217 | 0.227 | 0.232 | 0.234 | 0.234 | 0.232 | 0.229 |
| 24 | 0.083 | 0.136 | 0.173 | 0.197 | 0.213 | 0.223 | 0.228 | 0.230 | 0.230 | 0.228 | 0.225 |
| 25 | 0.080 | 0.132 | 0.169 | 0.194 | 0.210 | 0.219 | 0.225 | 0.227 | 0.227 | 0.225 | 0.221 |
| 26 | 0.077 | 0.129 | 0.166 | 0.190 | 0.206 | 0.216 | 0.221 | 0.223 | 0.223 | 0.221 | 0.217 |
| 27 | 0.075 | 0.126 | 0.162 | 0.187 | 0.203 | 0.212 | 0.218 | 0.220 | 0.219 | 0.217 | 0.214 |
| 28 | 0.072 | 0.123 | 0.159 | 0.184 | 0.200 | 0.209 | 0.214 | 0.216 | 0.216 | 0.214 | 0.210 |
| 29 | 0.070 | 0.120 | 0.156 | 0.181 | 0.196 | 0.206 | 0.211 | 0.213 | 0.212 | 0.210 | 0.206 |
| 30 | 0.068 | 0.117 | 0.153 | 0.177 | 0.193 | 0.203 | 0.208 | 0.210 | 0.209 | 0.207 | 0.203 |

Table C. 16
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 90 /$ Annual Growth Rate $=\mathbf{5 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.004 | 0.022 | 0.052 | 0.086 | 0.118 | 0.147 | 0.172 | 0.193 | 0.212 | 0.227 | 0.241 |
| 2 | 0.020 | 0.060 | 0.103 | 0.142 | 0.174 | 0.201 | 0.222 | 0.239 | 0.254 | 0.265 | 0.275 |
| 3 | 0.035 | 0.084 | 0.130 | 0.168 | 0.199 | 0.222 | 0.241 | 0.256 | 0.267 | 0.277 | 0.284 |
| 4 | 0.046 | 0.099 | 0.145 | 0.182 | 0.211 | 0.233 | 0.249 | 0.262 | 0.272 | 0.280 | 0.286 |
| 5 | 0.054 | 0.108 | 0.154 | 0.190 | 0.217 | 0.237 | 0.253 | 0.264 | 0.273 | 0.280 | 0.284 |
| 6 | 0.059 | 0.114 | 0.160 | 0.194 | 0.220 | 0.239 | 0.254 | 0.264 | 0.272 | 0.278 | 0.281 |
| 7 | 0.062 | 0.118 | 0.163 | 0.196 | 0.221 | 0.240 | 0.253 | 0.263 | 0.270 | 0.275 | 0.278 |
| 8 | 0.064 | 0.120 | 0.164 | 0.197 | 0.221 | 0.239 | 0.251 | 0.261 | 0.267 | 0.271 | 0.274 |
| 9 | 0.065 | 0.121 | 0.165 | 0.197 | 0.220 | 0.237 | 0.249 | 0.258 | 0.264 | 0.267 | 0.269 |
| 10 | 0.066 | 0.121 | 0.164 | 0.196 | 0.219 | 0.235 | 0.247 | 0.255 | 0.260 | 0.263 | 0.265 |
| 11 | 0.066 | 0.120 | 0.163 | 0.194 | 0.217 | 0.233 | 0.244 | 0.251 | 0.256 | 0.259 | 0.260 |
| 12 | 0.065 | 0.120 | 0.162 | 0.193 | 0.215 | 0.230 | 0.241 | 0.248 | 0.253 | 0.255 | 0.256 |
| 13 | 0.065 | 0.118 | 0.160 | 0.191 | 0.212 | 0.227 | 0.238 | 0.245 | 0.249 | 0.251 | 0.251 |
| 14 | 0.064 | 0.117 | 0.159 | 0.189 | 0.210 | 0.225 | 0.235 | 0.241 | 0.245 | 0.247 | 0.247 |
| 15 | 0.063 | 0.115 | 0.157 | 0.186 | 0.207 | 0.222 | 0.231 | 0.238 | 0.241 | 0.243 | 0.243 |
| 16 | 0.062 | 0.114 | 0.154 | 0.184 | 0.204 | 0.219 | 0.228 | 0.234 | 0.238 | 0.239 | 0.239 |
| 17 | 0.060 | 0.112 | 0.152 | 0.181 | 0.202 | 0.216 | 0.225 | 0.231 | 0.234 | 0.235 | 0.234 |


| 18 | 0.059 | 0.110 | 0.150 | 0.179 | 0.199 | 0.213 | 0.222 | 0.227 | 0.230 | 0.231 | 0.230 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.058 | 0.108 | 0.148 | 0.176 | 0.196 | 0.210 | 0.219 | 0.224 | 0.227 | 0.227 | 0.226 |
| 20 | 0.056 | 0.106 | 0.146 | 0.174 | 0.194 | 0.207 | 0.216 | 0.221 | 0.223 | 0.224 | 0.223 |
| 21 | 0.055 | 0.104 | 0.143 | 0.171 | 0.191 | 0.204 | 0.212 | 0.217 | 0.220 | 0.220 | 0.219 |
| 22 | 0.053 | 0.102 | 0.141 | 0.169 | 0.188 | 0.201 | 0.209 | 0.214 | 0.216 | 0.216 | 0.215 |
| 23 | 0.052 | 0.100 | 0.139 | 0.166 | 0.185 | 0.198 | 0.206 | 0.211 | 0.213 | 0.213 | 0.211 |
| 24 | 0.051 | 0.098 | 0.136 | 0.164 | 0.183 | 0.195 | 0.203 | 0.208 | 0.210 | 0.210 | 0.208 |
| 25 | 0.049 | 0.096 | 0.134 | 0.161 | 0.180 | 0.193 | 0.201 | 0.205 | 0.207 | 0.206 | 0.204 |
| 26 | 0.048 | 0.094 | 0.132 | 0.159 | 0.178 | 0.190 | 0.198 | 0.202 | 0.203 | 0.203 | 0.201 |
| 27 | 0.046 | 0.092 | 0.130 | 0.156 | 0.175 | 0.187 | 0.195 | 0.199 | 0.200 | 0.200 | 0.198 |
| 28 | 0.045 | 0.090 | 0.127 | 0.154 | 0.172 | 0.185 | 0.192 | 0.196 | 0.197 | 0.197 | 0.195 |
| 29 | 0.044 | 0.089 | 0.125 | 0.152 | 0.170 | 0.182 | 0.189 | 0.193 | 0.194 | 0.194 | 0.191 |
| 30 | 0.043 | 0.087 | 0.123 | 0.149 | 0.168 | 0.179 | 0.187 | 0.190 | 0.192 | 0.191 | 0.188 |

Table C. 17
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 85 /$ Annual Growth Rate $=\mathbf{5 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.001 | 0.008 | 0.021 | 0.040 | 0.061 | 0.083 | 0.104 | 0.123 | 0.141 | 0.157 |
| 2 | 0.001 | 0.012 | 0.034 | 0.062 | 0.091 | 0.117 | 0.141 | 0.162 | 0.179 | 0.195 | 0.208 |
| 3 | 0.005 | 0.026 | 0.057 | 0.090 | 0.120 | 0.147 | 0.169 | 0.188 | 0.204 | 0.217 | 0.227 |
| 4 | 0.010 | 0.037 | 0.073 | 0.108 | 0.139 | 0.164 | 0.185 | 0.202 | 0.216 | 0.227 | 0.236 |
| 5 | 0.014 | 0.047 | 0.085 | 0.120 | 0.150 | 0.175 | 0.194 | 0.210 | 0.222 | 0.232 | 0.240 |
| 6 | 0.018 | 0.054 | 0.094 | 0.129 | 0.158 | 0.181 | 0.200 | 0.214 | 0.226 | 0.234 | 0.241 |
| 7 | 0.021 | 0.059 | 0.100 | 0.135 | 0.163 | 0.185 | 0.203 | 0.216 | 0.227 | 0.235 | 0.240 |
| 8 | 0.023 | 0.064 | 0.104 | 0.139 | 0.166 | 0.188 | 0.205 | 0.217 | 0.227 | 0.234 | 0.239 |
| 9 | 0.026 | 0.067 | 0.107 | 0.142 | 0.169 | 0.189 | 0.205 | 0.217 | 0.226 | 0.232 | 0.237 |
| 10 | 0.027 | 0.069 | 0.110 | 0.143 | 0.170 | 0.190 | 0.205 | 0.216 | 0.224 | 0.230 | 0.234 |
| 11 | 0.028 | 0.071 | 0.111 | 0.144 | 0.170 | 0.190 | 0.204 | 0.215 | 0.223 | 0.228 | 0.231 |
| 12 | 0.029 | 0.072 | 0.112 | 0.145 | 0.170 | 0.189 | 0.203 | 0.213 | 0.221 | 0.225 | 0.228 |
| 13 | 0.030 | 0.073 | 0.113 | 0.145 | 0.170 | 0.188 | 0.202 | 0.211 | 0.218 | 0.223 | 0.225 |
| 14 | 0.030 | 0.073 | 0.113 | 0.145 | 0.169 | 0.187 | 0.200 | 0.209 | 0.216 | 0.220 | 0.222 |
| 15 | 0.031 | 0.073 | 0.113 | 0.144 | 0.168 | 0.186 | 0.198 | 0.207 | 0.213 | 0.217 | 0.219 |
| 16 | 0.031 | 0.073 | 0.112 | 0.143 | 0.167 | 0.184 | 0.196 | 0.205 | 0.211 | 0.214 | 0.216 |
| 17 | 0.031 | 0.073 | 0.111 | 0.142 | 0.165 | 0.182 | 0.194 | 0.203 | 0.208 | 0.211 | 0.212 |


| 18 | 0.030 | 0.072 | 0.111 | 0.141 | 0.164 | 0.180 | 0.192 | 0.200 | 0.205 | 0.208 | 0.209 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.030 | 0.072 | 0.110 | 0.140 | 0.162 | 0.179 | 0.190 | 0.198 | 0.203 | 0.205 | 0.206 |
| 20 | 0.030 | 0.071 | 0.109 | 0.139 | 0.161 | 0.177 | 0.188 | 0.195 | 0.200 | 0.202 | 0.203 |
| 21 | 0.029 | 0.070 | 0.108 | 0.137 | 0.159 | 0.175 | 0.186 | 0.193 | 0.197 | 0.199 | 0.200 |
| 22 | 0.029 | 0.069 | 0.107 | 0.136 | 0.157 | 0.173 | 0.183 | 0.190 | 0.195 | 0.196 | 0.197 |
| 23 | 0.029 | 0.069 | 0.105 | 0.134 | 0.156 | 0.171 | 0.181 | 0.188 | 0.192 | 0.194 | 0.194 |
| 24 | 0.028 | 0.068 | 0.104 | 0.133 | 0.154 | 0.169 | 0.179 | 0.186 | 0.189 | 0.191 | 0.191 |
| 25 | 0.028 | 0.067 | 0.103 | 0.131 | 0.152 | 0.167 | 0.177 | 0.183 | 0.187 | 0.188 | 0.188 |
| 26 | 0.027 | 0.066 | 0.101 | 0.130 | 0.150 | 0.165 | 0.175 | 0.181 | 0.184 | 0.185 | 0.185 |
| 27 | 0.027 | 0.065 | 0.100 | 0.128 | 0.148 | 0.163 | 0.172 | 0.178 | 0.182 | 0.183 | 0.182 |
| 28 | 0.026 | 0.064 | 0.099 | 0.126 | 0.147 | 0.161 | 0.170 | 0.176 | 0.179 | 0.180 | 0.179 |
| 29 | 0.025 | 0.063 | 0.097 | 0.125 | 0.145 | 0.159 | 0.168 | 0.174 | 0.177 | 0.177 | 0.176 |
| 30 | 0.025 | 0.062 | 0.096 | 0.123 | 0.143 | 0.157 | 0.166 | 0.171 | 0.174 | 0.175 | 0.174 |

Table C. 18
Probability of a Put Expiring in the Money as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 80 /$ Annual Growth Rate $=\mathbf{5 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.001 | 0.003 | 0.009 | 0.019 | 0.032 | 0.046 | 0.061 | 0.077 | 0.091 |
| 2 | 0.000 | 0.001 | 0.008 | 0.021 | 0.039 | 0.059 | 0.080 | 0.099 | 0.117 | 0.134 | 0.149 |
| 3 | 0.000 | 0.005 | 0.019 | 0.040 | 0.064 | 0.088 | 0.110 | 0.130 | 0.147 | 0.162 | 0.175 |
| 4 | 0.001 | 0.011 | 0.031 | 0.056 | 0.083 | 0.107 | 0.129 | 0.148 | 0.164 | 0.178 | 0.189 |
| 5 | 0.002 | 0.016 | 0.040 | 0.069 | 0.096 | 0.121 | 0.142 | 0.160 | 0.175 | 0.187 | 0.197 |
| 6 | 0.004 | 0.021 | 0.048 | 0.078 | 0.106 | 0.130 | 0.151 | 0.168 | 0.182 | 0.193 | 0.202 |
| 7 | 0.005 | 0.025 | 0.055 | 0.086 | 0.113 | 0.137 | 0.157 | 0.173 | 0.186 | 0.196 | 0.204 |
| 8 | 0.007 | 0.029 | 0.060 | 0.091 | 0.119 | 0.142 | 0.161 | 0.176 | 0.188 | 0.198 | 0.205 |
| 9 | 0.008 | 0.032 | 0.064 | 0.096 | 0.123 | 0.146 | 0.164 | 0.178 | 0.189 | 0.198 | 0.205 |
| 10 | 0.009 | 0.035 | 0.068 | 0.099 | 0.126 | 0.148 | 0.166 | 0.179 | 0.190 | 0.198 | 0.204 |
| 11 | 0.010 | 0.037 | 0.070 | 0.102 | 0.128 | 0.150 | 0.167 | 0.180 | 0.190 | 0.197 | 0.203 |
| 12 | 0.011 | 0.039 | 0.072 | 0.104 | 0.130 | 0.151 | 0.167 | 0.180 | 0.189 | 0.196 | 0.201 |
| 12 | 0.012 | 0.040 | 0.074 | 0.105 | 0.131 | 0.151 | 0.167 | 0.179 | 0.188 | 0.195 | 0.199 |
| 13 | 0.012 | 0.041 | 0.075 | 0.106 | 0.132 | 0.152 | 0.167 | 0.179 | 0.187 | 0.193 | 0.197 |
| 17 | 0.013 | 0.042 | 0.076 | 0.107 | 0.132 | 0.151 | 0.166 | 0.178 | 0.186 | 0.191 | 0.195 |
| 17 | 0.013 | 0.044 | 0.077 | 0.107 | 0.132 | 0.151 | 0.165 | 0.175 | 0.182 | 0.187 | 0.190 |
| 15 | 0.077 | 0.107 | 0.132 | 0.151 | 0.166 | 0.176 | 0.184 | 0.189 | 0.193 |  |  |


| 18 | 0.014 | 0.044 | 0.078 | 0.107 | 0.131 | 0.150 | 0.164 | 0.174 | 0.181 | 0.185 | 0.188 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.014 | 0.044 | 0.078 | 0.107 | 0.131 | 0.149 | 0.162 | 0.172 | 0.179 | 0.183 | 0.185 |
| 20 | 0.014 | 0.044 | 0.078 | 0.107 | 0.130 | 0.148 | 0.161 | 0.170 | 0.177 | 0.181 | 0.183 |
| 21 | 0.014 | 0.044 | 0.077 | 0.106 | 0.129 | 0.147 | 0.160 | 0.169 | 0.175 | 0.179 | 0.181 |
| 22 | 0.014 | 0.044 | 0.077 | 0.106 | 0.129 | 0.146 | 0.158 | 0.167 | 0.173 | 0.176 | 0.178 |
| 23 | 0.014 | 0.044 | 0.077 | 0.105 | 0.128 | 0.144 | 0.157 | 0.165 | 0.171 | 0.174 | 0.176 |
| 24 | 0.014 | 0.044 | 0.076 | 0.104 | 0.127 | 0.143 | 0.155 | 0.163 | 0.169 | 0.172 | 0.173 |
| 25 | 0.014 | 0.044 | 0.076 | 0.104 | 0.125 | 0.142 | 0.154 | 0.162 | 0.167 | 0.170 | 0.171 |
| 26 | 0.014 | 0.043 | 0.075 | 0.103 | 0.124 | 0.140 | 0.152 | 0.160 | 0.165 | 0.167 | 0.168 |
| 27 | 0.014 | 0.043 | 0.075 | 0.102 | 0.123 | 0.139 | 0.150 | 0.158 | 0.163 | 0.165 | 0.166 |
| 28 | 0.014 | 0.042 | 0.074 | 0.101 | 0.122 | 0.138 | 0.149 | 0.156 | 0.161 | 0.163 | 0.164 |
| 29 | 0.013 | 0.042 | 0.073 | 0.100 | 0.121 | 0.136 | 0.147 | 0.154 | 0.159 | 0.161 | 0.161 |
| 20 | 0.013 | 0.042 | 0.072 | 0.099 | 0.120 | 0.135 | 0.146 | 0.153 | 0.157 | 0.159 | 0.159 |

Table C. 19
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 120 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.000 | 0.998 | 0.989 | 0.972 | 0.948 | 0.920 | 0.892 | 0.864 | 0.838 | 0.813 | 0.790 |
| 2 | 0.994 | 0.969 | 0.930 | 0.887 | 0.846 | 0.808 | 0.775 | 0.746 | 0.719 | 0.696 | 0.675 |
| 3 | 0.969 | 0.915 | 0.859 | 0.809 | 0.766 | 0.730 | 0.698 | 0.672 | 0.648 | 0.627 | 0.609 |
| 4 | 0.926 | 0.855 | 0.794 | 0.745 | 0.704 | 0.671 | 0.643 | 0.619 | 0.598 | 0.579 | 0.562 |
| 5 | 0.874 | 0.797 | 0.738 | 0.692 | 0.655 | 0.625 | 0.600 | 0.578 | 0.559 | 0.542 | 0.526 |
| 6 | 0.819 | 0.743 | 0.688 | 0.647 | 0.614 | 0.587 | 0.565 | 0.545 | 0.527 | 0.512 | 0.497 |
| 7 | 0.764 | 0.694 | 0.645 | 0.608 | 0.579 | 0.555 | 0.535 | 0.517 | 0.501 | 0.486 | 0.472 |
| 8 | 0.711 | 0.649 | 0.606 | 0.574 | 0.549 | 0.527 | 0.509 | 0.492 | 0.478 | 0.464 | 0.451 |
| 9 | 0.661 | 0.608 | 0.571 | 0.544 | 0.522 | 0.503 | 0.486 | 0.471 | 0.457 | 0.444 | 0.432 |
| 10 | 0.614 | 0.570 | 0.540 | 0.517 | 0.497 | 0.481 | 0.466 | 0.452 | 0.439 | 0.427 | 0.415 |
| 11 | 0.570 | 0.536 | 0.512 | 0.492 | 0.476 | 0.461 | 0.447 | 0.435 | 0.422 | 0.411 | 0.400 |
| 12 | 0.529 | 0.505 | 0.486 | 0.470 | 0.456 | 0.443 | 0.430 | 0.419 | 0.407 | 0.396 | 0.386 |
| 13 | 0.492 | 0.476 | 0.462 | 0.449 | 0.437 | 0.426 | 0.415 | 0.404 | 0.393 | 0.383 | 0.373 |
| 14 | 0.457 | 0.449 | 0.440 | 0.430 | 0.421 | 0.411 | 0.401 | 0.390 | 0.380 | 0.370 | 0.360 |
| 15 | 0.425 | 0.424 | 0.420 | 0.413 | 0.405 | 0.396 | 0.387 | 0.378 | 0.368 | 0.359 | 0.349 |
| 16 | 0.395 | 0.401 | 0.401 | 0.396 | 0.390 | 0.383 | 0.375 | 0.366 | 0.357 | 0.348 | 0.338 |
| 17 | 0.368 | 0.380 | 0.383 | 0.381 | 0.376 | 0.370 | 0.363 | 0.355 | 0.346 | 0.338 | 0.328 |


| 18 | 0.342 | 0.360 | 0.366 | 0.367 | 0.364 | 0.358 | 0.352 | 0.344 | 0.336 | 0.328 | 0.319 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.319 | 0.342 | 0.351 | 0.353 | 0.351 | 0.347 | 0.341 | 0.335 | 0.327 | 0.319 | 0.310 |
| 20 | 0.297 | 0.324 | 0.336 | 0.340 | 0.340 | 0.337 | 0.332 | 0.325 | 0.318 | 0.310 | 0.302 |
| 21 | 0.277 | 0.308 | 0.323 | 0.328 | 0.329 | 0.327 | 0.322 | 0.316 | 0.309 | 0.302 | 0.293 |
| 22 | 0.258 | 0.293 | 0.310 | 0.317 | 0.319 | 0.317 | 0.313 | 0.308 | 0.301 | 0.294 | 0.286 |
| 23 | 0.241 | 0.278 | 0.297 | 0.306 | 0.309 | 0.308 | 0.305 | 0.300 | 0.293 | 0.286 | 0.278 |
| 24 | 0.225 | 0.265 | 0.286 | 0.296 | 0.300 | 0.299 | 0.296 | 0.292 | 0.286 | 0.279 | 0.271 |
| 25 | 0.210 | 0.252 | 0.275 | 0.286 | 0.291 | 0.291 | 0.289 | 0.284 | 0.279 | 0.272 | 0.264 |
| 26 | 0.196 | 0.240 | 0.264 | 0.277 | 0.282 | 0.283 | 0.281 | 0.277 | 0.272 | 0.265 | 0.258 |
| 27 | 0.183 | 0.229 | 0.254 | 0.268 | 0.274 | 0.276 | 0.274 | 0.270 | 0.265 | 0.259 | 0.252 |
| 28 | 0.172 | 0.218 | 0.245 | 0.259 | 0.266 | 0.268 | 0.267 | 0.264 | 0.259 | 0.253 | 0.245 |
| 29 | 0.160 | 0.208 | 0.236 | 0.251 | 0.259 | 0.261 | 0.260 | 0.257 | 0.253 | 0.247 | 0.240 |
| 20 | 0.150 | 0.199 | 0.227 | 0.243 | 0.251 | 0.255 | 0.254 | 0.251 | 0.247 | 0.241 | 0.234 |

Table C. 20
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 115 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.998 | 0.985 | 0.957 | 0.922 | 0.885 | 0.850 | 0.818 | 0.789 | 0.763 | 0.740 | 0.719 |
| 2 | 0.965 | 0.911 | 0.855 | 0.806 | 0.764 | 0.729 | 0.700 | 0.674 | 0.652 | 0.633 | 0.615 |
| 3 | 0.902 | 0.828 | 0.769 | 0.722 | 0.685 | 0.655 | 0.630 | 0.608 | 0.589 | 0.572 | 0.557 |
| 4 | 0.830 | 0.755 | 0.701 | 0.660 | 0.628 | 0.602 | 0.580 | 0.562 | 0.545 | 0.530 | 0.517 |
| 5 | 0.760 | 0.692 | 0.645 | 0.611 | 0.583 | 0.561 | 0.542 | 0.526 | 0.511 | 0.498 | 0.486 |
| 6 | 0.695 | 0.638 | 0.599 | 0.570 | 0.547 | 0.528 | 0.511 | 0.497 | 0.484 | 0.472 | 0.460 |
| 7 | 0.636 | 0.590 | 0.559 | 0.535 | 0.516 | 0.500 | 0.485 | 0.472 | 0.460 | 0.449 | 0.439 |
| 8 | 0.583 | 0.548 | 0.524 | 0.505 | 0.489 | 0.475 | 0.463 | 0.451 | 0.440 | 0.430 | 0.420 |
| 9 | 0.535 | 0.511 | 0.493 | 0.479 | 0.466 | 0.454 | 0.443 | 0.432 | 0.422 | 0.412 | 0.403 |
| 10 | 0.491 | 0.478 | 0.466 | 0.455 | 0.444 | 0.434 | 0.425 | 0.415 | 0.406 | 0.397 | 0.387 |
| 11 | 0.452 | 0.448 | 0.441 | 0.433 | 0.425 | 0.417 | 0.408 | 0.400 | 0.391 | 0.382 | 0.374 |
| 12 | 0.417 | 0.420 | 0.418 | 0.414 | 0.408 | 0.401 | 0.394 | 0.386 | 0.378 | 0.369 | 0.361 |
| 13 | 0.385 | 0.395 | 0.398 | 0.396 | 0.392 | 0.386 | 0.380 | 0.373 | 0.365 | 0.357 | 0.349 |
| 14 | 0.356 | 0.373 | 0.379 | 0.380 | 0.377 | 0.373 | 0.367 | 0.361 | 0.353 | 0.346 | 0.338 |
| 15 | 0.329 | 0.352 | 0.361 | 0.364 | 0.363 | 0.360 | 0.355 | 0.349 | 0.343 | 0.335 | 0.328 |
| 16 | 0.305 | 0.332 | 0.345 | 0.350 | 0.350 | 0.348 | 0.344 | 0.339 | 0.332 | 0.325 | 0.318 |
| 17 | 0.282 | 0.314 | 0.330 | 0.337 | 0.338 | 0.337 | 0.334 | 0.329 | 0.323 | 0.316 | 0.309 |


| 18 | 0.262 | 0.297 | 0.315 | 0.324 | 0.327 | 0.327 | 0.324 | 0.319 | 0.314 | 0.307 | 0.300 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.243 | 0.282 | 0.302 | 0.312 | 0.316 | 0.317 | 0.314 | 0.310 | 0.305 | 0.299 | 0.292 |
| 20 | 0.226 | 0.267 | 0.290 | 0.301 | 0.306 | 0.307 | 0.305 | 0.302 | 0.297 | 0.291 | 0.284 |
| 21 | 0.210 | 0.254 | 0.278 | 0.291 | 0.297 | 0.298 | 0.297 | 0.294 | 0.289 | 0.283 | 0.277 |
| 22 | 0.196 | 0.241 | 0.267 | 0.281 | 0.287 | 0.290 | 0.289 | 0.286 | 0.281 | 0.276 | 0.269 |
| 23 | 0.182 | 0.229 | 0.256 | 0.271 | 0.279 | 0.282 | 0.281 | 0.279 | 0.274 | 0.269 | 0.263 |
| 24 | 0.170 | 0.218 | 0.246 | 0.262 | 0.270 | 0.274 | 0.274 | 0.271 | 0.267 | 0.262 | 0.256 |
| 25 | 0.158 | 0.208 | 0.237 | 0.254 | 0.262 | 0.266 | 0.267 | 0.265 | 0.261 | 0.256 | 0.250 |
| 26 | 0.147 | 0.198 | 0.228 | 0.245 | 0.255 | 0.259 | 0.260 | 0.258 | 0.255 | 0.250 | 0.244 |
| 27 | 0.138 | 0.188 | 0.219 | 0.237 | 0.248 | 0.252 | 0.253 | 0.252 | 0.248 | 0.244 | 0.238 |
| 28 | 0.128 | 0.179 | 0.211 | 0.230 | 0.241 | 0.246 | 0.247 | 0.246 | 0.243 | 0.238 | 0.232 |
| 29 | 0.120 | 0.171 | 0.203 | 0.223 | 0.234 | 0.239 | 0.241 | 0.240 | 0.237 | 0.232 | 0.227 |
| 30 | 0.112 | 0.163 | 0.196 | 0.216 | 0.228 | 0.233 | 0.235 | 0.234 | 0.231 | 0.227 | 0.222 |

Table C. 21
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 110 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.969 | 0.918 | 0.864 | 0.817 | 0.777 | 0.743 | 0.714 | 0.690 | 0.669 | 0.650 | 0.634 |
| 2 | 0.862 | 0.788 | 0.733 | 0.691 | 0.659 | 0.633 | 0.611 | 0.593 | 0.577 | 0.563 | 0.550 |
| 3 | 0.758 | 0.693 | 0.648 | 0.616 | 0.590 | 0.570 | 0.553 | 0.538 | 0.525 | 0.514 | 0.503 |
| 4 | 0.671 | 0.620 | 0.587 | 0.562 | 0.542 | 0.526 | 0.513 | 0.500 | 0.489 | 0.479 | 0.470 |
| 5 | 0.598 | 0.563 | 0.539 | 0.520 | 0.506 | 0.493 | 0.481 | 0.471 | 0.461 | 0.452 | 0.444 |
| 6 | 0.536 | 0.515 | 0.499 | 0.486 | 0.475 | 0.465 | 0.456 | 0.447 | 0.438 | 0.430 | 0.422 |
| 7 | 0.484 | 0.475 | 0.466 | 0.458 | 0.450 | 0.442 | 0.434 | 0.426 | 0.419 | 0.411 | 0.404 |
| 8 | 0.439 | 0.440 | 0.437 | 0.433 | 0.428 | 0.421 | 0.415 | 0.408 | 0.401 | 0.394 | 0.387 |
| 9 | 0.399 | 0.409 | 0.412 | 0.411 | 0.408 | 0.403 | 0.398 | 0.392 | 0.386 | 0.379 | 0.372 |
| 10 | 0.365 | 0.382 | 0.389 | 0.391 | 0.390 | 0.387 | 0.383 | 0.378 | 0.372 | 0.366 | 0.359 |
| 11 | 0.334 | 0.358 | 0.369 | 0.374 | 0.374 | 0.372 | 0.369 | 0.364 | 0.359 | 0.353 | 0.347 |
| 12 | 0.306 | 0.336 | 0.351 | 0.357 | 0.359 | 0.359 | 0.356 | 0.352 | 0.347 | 0.342 | 0.336 |
| 13 | 0.282 | 0.316 | 0.334 | 0.342 | 0.346 | 0.346 | 0.344 | 0.341 | 0.336 | 0.331 | 0.325 |
| 14 | 0.260 | 0.298 | 0.318 | 0.329 | 0.333 | 0.335 | 0.333 | 0.330 | 0.326 | 0.321 | 0.315 |
| 15 | 0.239 | 0.281 | 0.304 | 0.316 | 0.322 | 0.324 | 0.323 | 0.320 | 0.316 | 0.312 | 0.306 |
| 16 | 0.221 | 0.265 | 0.290 | 0.304 | 0.311 | 0.313 | 0.313 | 0.311 | 0.307 | 0.303 | 0.297 |
| 17 | 0.205 | 0.251 | 0.278 | 0.292 | 0.300 | 0.304 | 0.304 | 0.302 | 0.299 | 0.294 | 0.289 |


| 18 | 0.190 | 0.238 | 0.266 | 0.282 | 0.291 | 0.295 | 0.295 | 0.294 | 0.291 | 0.286 | 0.281 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.176 | 0.226 | 0.255 | 0.272 | 0.281 | 0.286 | 0.287 | 0.286 | 0.283 | 0.279 | 0.274 |
| 20 | 0.163 | 0.214 | 0.244 | 0.262 | 0.273 | 0.278 | 0.279 | 0.278 | 0.275 | 0.271 | 0.266 |
| 21 | 0.152 | 0.203 | 0.235 | 0.253 | 0.264 | 0.270 | 0.272 | 0.271 | 0.268 | 0.265 | 0.260 |
| 22 | 0.141 | 0.193 | 0.225 | 0.245 | 0.256 | 0.262 | 0.264 | 0.264 | 0.262 | 0.258 | 0.253 |
| 23 | 0.131 | 0.184 | 0.217 | 0.237 | 0.249 | 0.255 | 0.258 | 0.257 | 0.255 | 0.252 | 0.247 |
| 24 | 0.122 | 0.175 | 0.208 | 0.229 | 0.242 | 0.248 | 0.251 | 0.251 | 0.249 | 0.245 | 0.241 |
| 25 | 0.114 | 0.166 | 0.200 | 0.222 | 0.235 | 0.242 | 0.245 | 0.245 | 0.243 | 0.240 | 0.235 |
| 26 | 0.106 | 0.158 | 0.193 | 0.215 | 0.228 | 0.235 | 0.239 | 0.239 | 0.237 | 0.234 | 0.229 |
| 27 | 0.099 | 0.151 | 0.186 | 0.208 | 0.222 | 0.229 | 0.233 | 0.233 | 0.232 | 0.228 | 0.224 |
| 28 | 0.092 | 0.144 | 0.179 | 0.202 | 0.216 | 0.223 | 0.227 | 0.228 | 0.226 | 0.223 | 0.219 |
| 29 | 0.086 | 0.137 | 0.173 | 0.195 | 0.210 | 0.218 | 0.222 | 0.223 | 0.221 | 0.218 | 0.214 |
| 20 | 0.080 | 0.131 | 0.166 | 0.190 | 0.204 | 0.212 | 0.217 | 0.217 | 0.216 | 0.213 | 0.209 |

Table C. 22
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 105 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.787 | 0.721 | 0.676 | 0.643 | 0.618 | 0.598 | 0.582 | 0.569 | 0.557 | 0.547 | 0.538 |
| 2 | 0.630 | 0.591 | 0.566 | 0.548 | 0.533 | 0.521 | 0.511 | 0.503 | 0.495 | 0.487 | 0.480 |
| 3 | 0.532 | 0.515 | 0.503 | 0.493 | 0.485 | 0.478 | 0.471 | 0.464 | 0.458 | 0.452 | 0.446 |
| 4 | 0.462 | 0.461 | 0.459 | 0.455 | 0.451 | 0.446 | 0.441 | 0.436 | 0.431 | 0.426 | 0.421 |
| 5 | 0.408 | 0.420 | 0.424 | 0.425 | 0.424 | 0.421 | 0.418 | 0.414 | 0.410 | 0.405 | 0.400 |
| 6 | 0.364 | 0.385 | 0.396 | 0.400 | 0.401 | 0.401 | 0.399 | 0.395 | 0.392 | 0.388 | 0.383 |
| 7 | 0.328 | 0.356 | 0.371 | 0.379 | 0.382 | 0.383 | 0.382 | 0.379 | 0.376 | 0.372 | 0.368 |
| 8 | 0.297 | 0.331 | 0.350 | 0.360 | 0.365 | 0.367 | 0.366 | 0.365 | 0.362 | 0.358 | 0.354 |
| 9 | 0.270 | 0.309 | 0.331 | 0.343 | 0.350 | 0.352 | 0.353 | 0.352 | 0.349 | 0.346 | 0.342 |
| 10 | 0.246 | 0.290 | 0.314 | 0.328 | 0.336 | 0.339 | 0.340 | 0.340 | 0.337 | 0.334 | 0.330 |
| 11 | 0.226 | 0.272 | 0.299 | 0.314 | 0.323 | 0.327 | 0.329 | 0.329 | 0.327 | 0.324 | 0.320 |
| 12 | 0.207 | 0.256 | 0.284 | 0.301 | 0.311 | 0.316 | 0.318 | 0.318 | 0.317 | 0.314 | 0.310 |
| 13 | 0.191 | 0.241 | 0.271 | 0.289 | 0.300 | 0.306 | 0.309 | 0.309 | 0.307 | 0.304 | 0.301 |
| 14 | 0.176 | 0.228 | 0.259 | 0.278 | 0.290 | 0.296 | 0299 | 0.300 | 0.298 | 0.296 | 0.292 |
| 15 | 0.162 | 0.215 | 0.248 | 0.268 | 0.280 | 0.287 | 0.290 | 0.291 | 0.290 | 0.287 | 0.284 |
| 16 | 0.150 | 0.204 | 0.238 | 0.258 | 0.271 | 0.279 | 0.282 | 0.283 | 0.282 | 0.280 | 0.276 |
| 17 | 0.139 | 0.193 | 0.228 | 0.249 | 0.263 | 0.270 | 0.274 | 0.275 | 0.275 | 0.272 | 0.269 |


| 18 | 0.129 | 0.183 | 0.218 | 0.241 | 0.255 | 0.263 | 0.267 | 0.268 | 0.267 | 0.265 | 0.262 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.119 | 0.174 | 0.210 | 0.233 | 0.247 | 0.255 | 0.260 | 0.261 | 0.261 | 0.258 | 0.255 |
| 20 | 0.111 | 0.165 | 0.201 | 0.225 | 0.239 | 0.248 | 0.253 | 0.255 | 0.254 | 0.252 | 0.249 |
| 21 | 0.103 | 0.157 | 0.194 | 0.217 | 0.232 | 0.241 | 0.246 | 0.248 | 0.248 | 0.246 | 0.242 |
| 22 | 0.096 | 0.150 | 0.186 | 0.210 | 0.226 | 0.235 | 0.240 | 0.242 | 0.242 | 0.240 | 0.236 |
| 23 | 0.089 | 0.142 | 0.179 | 0.204 | 0.219 | 0.229 | 0.234 | 0.236 | 0.236 | 0.234 | 0.231 |
| 24 | 0.083 | 0.136 | 0.173 | 0.197 | 0.213 | 0.223 | 0.228 | 0.231 | 0.230 | 0.228 | 0.225 |
| 25 | 0.077 | 0.129 | 0.166 | 0.191 | 0.207 | 0.217 | 0.223 | 0.225 | 0.225 | 0.223 | 0.220 |
| 26 | 0.072 | 0.123 | 0.160 | 0.185 | 0.202 | 0.212 | 0.217 | 0.220 | 0.220 | 0.218 | 0.215 |
| 27 | 0.067 | 0.118 | 0.154 | 0.180 | 0.196 | 0.206 | 0.212 | 0.215 | 0.215 | 0.213 | 0.210 |
| 28 | 0.063 | 0.112 | 0.149 | 0.174 | 0.191 | 0.201 | 0.207 | 0.210 | 0.210 | 0.208 | 0.205 |
| 29 | 0.059 | 0.107 | 0.144 | 0.169 | 0.186 | 0.196 | 0.202 | 0.205 | 0.205 | 0.204 | 0.201 |
| 20 | 0.055 | 0.102 | 0.139 | 0.164 | 0.181 | 0.192 | 0.198 | 0.201 | 0.201 | 0.199 | 0.196 |

Table C. 23
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 100 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.371 | 0.398 | 0.413 | 0.422 | 0.428 | 0.431 | 0.433 | 0.435 | 0.435 | 0.435 | 0.435 |
| 2 | 0.321 | 0.357 | 0.377 | 0.390 | 0.398 | 0.403 | 0.406 | 0.408 | 0.409 | 0.409 | 0.408 |
| 3 | 0.284 | 0.326 | 0.351 | 0.366 | 0.376 | 0.382 | 0.386 | 0.388 | 0.389 | 0.388 | 0.388 |
| 4 | 0.255 | 0.302 | 0.329 | 0.347 | 0.358 | 0.365 | 0.369 | 0.371 | 0.372 | 0.372 | 0.371 |
| 5 | 0.231 | 0.281 | 0.311 | 0.330 | 0.342 | 0.349 | 0.354 | 0.356 | 0.357 | 0.357 | 0.356 |
| 6 | 0.210 | 0.262 | 0.294 | 0.314 | 0.327 | 0.336 | 0.341 | 0.343 | 0.345 | 0.344 | 0.343 |
| 7 | 0.192 | 0.246 | 0.280 | 0.301 | 0.315 | 0.323 | 0.329 | 0.332 | 0.333 | 0.333 | 0.331 |
| 8 | 0.176 | 0.231 | 0.266 | 0.288 | 0.303 | 0.312 | 0.318 | 0.321 | 0.322 | 0.322 | 0.320 |
| 9 | 0.161 | 0.218 | 0.254 | 0.277 | 0.292 | 0.302 | 0.308 | 0.311 | 0.312 | 0.312 | 0.310 |
| 10 | 0.149 | 0.206 | 0.242 | 0.266 | 0.282 | 0.292 | 0.298 | 0.301 | 0.303 | 0.302 | 0.301 |
| 11 | 0.137 | 0.194 | 0.232 | 0.256 | 0.273 | 0.283 | 0.289 | 0.293 | 0.294 | 0.294 | 0.292 |
| 12 | 0.127 | 0.184 | 0.222 | 0.247 | 0.264 | 0.274 | 0.281 | 0.284 | 0.286 | 0.285 | 0.284 |
| 13 | 0.117 | 0.174 | 0.213 | 0.238 | 0.255 | 0.266 | 0.273 | 0.277 | 0.278 | 0.278 | 0.276 |
| 14 | 0.109 | 0.165 | 0.204 | 0.230 | 0.247 | 0.258 | 0.265 | 0.269 | 0.271 | 0.270 | 0.269 |
| 15 | 0.101 | 0.157 | 0.196 | 0.222 | 0.240 | 0.251 | 0.258 | 0.262 | 0.263 | 0.263 | 0.262 |
| 16 | 0.094 | 0.149 | 0.189 | 0.215 | 0.233 | 0.244 | 0.251 | 0.255 | 0.257 | 0.256 | 0.255 |
| 17 | 0.087 | 0.142 | 0.181 | 0.208 | 0.226 | 0.238 | 0.245 | 0.249 | 0.250 | 0.250 | 0.248 |


| 18 | 0.081 | 0.135 | 0.174 | 0.201 | 0.219 | 0.231 | 0.239 | 0.243 | 0.244 | 0.244 | 0.242 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.075 | 0.129 | 0.168 | 0.195 | 0.213 | 0.225 | 0.233 | 0.237 | 0.238 | 0.238 | 0.236 |
| 20 | 0.070 | 0.123 | 0.162 | 0.189 | 0.207 | 0.219 | 0.227 | 0.231 | 0.233 | 0.232 | 0.230 |
| 21 | 0.065 | 0.117 | 0.156 | 0.183 | 0.202 | 0.214 | 0.221 | 0.225 | 0.227 | 0.227 | 0.225 |
| 22 | 0.061 | 0.111 | 0.150 | 0.177 | 0.196 | 0.208 | 0.216 | 0.220 | 0.222 | 0.221 | 0.220 |
| 23 | 0.057 | 0.106 | 0.145 | 0.172 | 0.191 | 0.203 | 0.211 | 0.215 | 0.217 | 0.216 | 0.215 |
| 24 | 0.053 | 0.102 | 0.140 | 0.167 | 0.186 | 0.198 | 0.206 | 0.210 | 0.212 | 0.211 | 0.210 |
| 25 | 0.050 | 0.097 | 0.135 | 0.162 | 0.181 | 0.193 | 0.201 | 0.205 | 0.207 | 0.207 | 0.205 |
| 26 | 0.046 | 0.093 | 0.130 | 0.157 | 0.176 | 0.189 | 0.196 | 0.201 | 0.202 | 0.202 | 0.200 |
| 27 | 0.043 | 0.088 | 0.126 | 0.153 | 0.172 | 0.184 | 0.192 | 0.196 | 0.198 | 0.198 | 0.196 |
| 28 | 0.041 | 0.085 | 0.121 | 0.148 | 0.167 | 0.180 | 0.188 | 0.192 | 0.194 | 0.193 | 0.191 |
| 29 | 0.038 | 0.081 | 0.117 | 0.144 | 0.163 | 0.175 | 0.183 | 0.188 | 0.189 | 0.189 | 0.187 |
| 30 | 0.036 | 0.077 | 0.113 | 0.140 | 0.159 | 0.171 | 0.179 | 0.184 | 0.185 | 0.185 | 0.183 |

Table C. 24
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 95 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.065 | 0.125 | 0.176 | 0.215 | 0.245 | 0.268 | 0.287 | 0.302 | 0.313 | 0.323 | 0.331 |
| 2 | 0.096 | 0.160 | 0.208 | 0.243 | 0.269 | 0.288 | 0.303 | 0.314 | 0.323 | 0.330 | 0.335 |
| 3 | 0.105 | 0.168 | 0.214 | 0.247 | 0.271 | 0.289 | 0.302 | 0.312 | 0.319 | 0.325 | 0.329 |
| 4 | 0.105 | 0.168 | 0.213 | 0.245 | 0.268 | 0.285 | 0.297 | 0.306 | 0.313 | 0.317 | 0.320 |
| 5 | 0.103 | 0.164 | 0.208 | 0.240 | 0.263 | 0.279 | 0.291 | 0.299 | 0.305 | 0.309 | 0.312 |
| 6 | 0.098 | 0.159 | 0.203 | 0.234 | 0.256 | 0.272 | 0.284 | 0.292 | 0.297 | 0.301 | 0.303 |
| 7 | 0.093 | 0.153 | 0.197 | 0.228 | 0.250 | 0.266 | 0.277 | 0.284 | 0.290 | 0.293 | 0.295 |
| 8 | 0.088 | 0.147 | 0.191 | 0.221 | 0.243 | 0.259 | 0.270 | 0.277 | 0.282 | 0.285 | 0.287 |
| 9 | 0.083 | 0.141 | 0.184 | 0.215 | 0.237 | 0.252 | 0.263 | 0.270 | 0.275 | 0.278 | 0.279 |
| 10 | 0.078 | 0.135 | 0.178 | 0.209 | 0.230 | 0.246 | 0.256 | 0.263 | 0.268 | 0.271 | 0.272 |
| 11 | 0.073 | 0.129 | 0.172 | 0.202 | 0.224 | 0.239 | 0.250 | 0.257 | 0.261 | 0.264 | 0.265 |
| 12 | 0.069 | 0.124 | 0.166 | 0.196 | 0.218 | 0.233 | 0.244 | 0.251 | 0.255 | 0.257 | 0.258 |
| 13 | 0.065 | 0.118 | 0.160 | 0.191 | 0.212 | 0.227 | 0.238 | 0.245 | 0.249 | 0.251 | 0.251 |
| 14 | 0.061 | 0.113 | 0.155 | 0.185 | 0.207 | 0.222 | 0.232 | 0.239 | 0.243 | 0.245 | 0.245 |
| 15 | 0.057 | 0.108 | 0.149 | 0.180 | 0.201 | 0.216 | 0.226 | 0.233 | 0.237 | 0.239 | 0.239 |
| 17 | 0.053 | 0.104 | 0.144 | 0.174 | 0.196 | 0.211 | 0.221 | 0.228 | 0.231 | 0.233 | 0.233 |
| 10 | 0.099 | 0.139 | 0.169 | 0.191 | 0.206 | 0.216 | 0.222 | 0.226 | 0.228 | 0.228 |  |


| 18 | 0.047 | 0.095 | 0.135 | 0.164 | 0.186 | 0.201 | 0.211 | 0.217 | 0.221 | 0.222 | 0.222 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.044 | 0.091 | 0.130 | 0.160 | 0.181 | 0.196 | 0.206 | 0.212 | 0.216 | 0.217 | 0.217 |
| 20 | 0.041 | 0.087 | 0.126 | 0.155 | 0.176 | 0.191 | 0.201 | 0.207 | 0.211 | 0.213 | 0.212 |
| 21 | 0.038 | 0.083 | 0.122 | 0.151 | 0.172 | 0.187 | 0.197 | 0.203 | 0.206 | 0.208 | 0.207 |
| 22 | 0.036 | 0.080 | 0.118 | 0.147 | 0.167 | 0.182 | 0.192 | 0.198 | 0.202 | 0.203 | 0.203 |
| 23 | 0.034 | 0.076 | 0.114 | 0.142 | 0.163 | 0.178 | 0.188 | 0.194 | 0.197 | 0.199 | 0.198 |
| 24 | 0.032 | 0.073 | 0.110 | 0.138 | 0.159 | 0.174 | 0.184 | 0.190 | 0.193 | 0.194 | 0.194 |
| 25 | 0.030 | 0.070 | 0.106 | 0.135 | 0.155 | 0.170 | 0.180 | 0.186 | 0.189 | 0.190 | 0.190 |
| 26 | 0.028 | 0.067 | 0.103 | 0.131 | 0.151 | 0.166 | 0.176 | 0.182 | 0.185 | 0.186 | 0.186 |
| 27 | 0.026 | 0.064 | 0.100 | 0.127 | 0.148 | 0.162 | 0.172 | 0.178 | 0.181 | 0.182 | 0.182 |
| 28 | 0.025 | 0.061 | 0.096 | 0.124 | 0.144 | 0.159 | 0.168 | 0.174 | 0.177 | 0.178 | 0.178 |
| 29 | 0.023 | 0.059 | 0.093 | 0.121 | 0.141 | 0.155 | 0.165 | 0.171 | 0.174 | 0.175 | 0.174 |
| 30 | 0.022 | 0.056 | 0.090 | 0.117 | 0.137 | 0.152 | 0.161 | 0.167 | 0.170 | 0.171 | 0.170 |

Table C. 25
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 90 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.003 | 0.019 | 0.046 | 0.079 | 0.110 | 0.139 | 0.164 | 0.186 | 0.204 | 0.220 | 0.234 |
| 2 | 0.014 | 0.049 | 0.089 | 0.127 | 0.160 | 0.187 | 0.209 | 0.227 | 0.242 | 0.254 | 0.264 |
| 3 | 0.024 | 0.066 | 0.110 | 0.148 | 0.179 | 0.204 | 0.224 | 0.240 | 0.253 | 0.263 | 0.271 |
| 4 | 0.030 | 0.076 | 0.121 | 0.158 | 0.188 | 0.211 | 0.229 | 0.244 | 0.255 | 0.264 | 0.271 |
| 5 | 0.034 | 0.081 | 0.126 | 0.162 | 0.191 | 0.213 | 0.230 | 0.244 | 0.254 | 0.262 | 0.268 |
| 6 | 0.036 | 0.084 | 0.128 | 0.164 | 0.191 | 0.213 | 0.229 | 0.242 | 0.251 | 0.258 | 0.263 |
| 7 | 0.037 | 0.084 | 0.128 | 0.163 | 0.190 | 0.211 | 0.227 | 0.238 | 0.247 | 0.254 | 0.258 |
| 8 | 0.037 | 0.084 | 0.127 | 0.162 | 0.188 | 0.208 | 0.223 | 0.235 | 0.243 | 0.249 | 0.253 |
| 9 | 0.036 | 0.083 | 0.125 | 0.159 | 0.185 | 0.205 | 0.220 | 0.231 | 0.238 | 0.244 | 0.248 |
| 10 | 0.035 | 0.081 | 0.123 | 0.157 | 0.182 | 0.202 | 0.216 | 0.226 | 0.234 | 0.239 | 0.242 |
| 11 | 0.034 | 0.079 | 0.120 | 0.154 | 0.179 | 0.198 | 0.212 | 0.222 | 0.229 | 0.234 | 0.237 |
| 12 | 0.033 | 0.077 | 0.118 | 0.150 | 0.175 | 0.194 | 0.208 | 0.217 | 0.224 | 0.229 | 0.232 |
| 13 | 0.031 | 0.075 | 0.115 | 0.147 | 0.172 | 0.190 | 0.203 | 0.213 | 0.220 | 0.224 | 0.227 |
| 14 | 0.030 | 0.072 | 0.112 | 0.144 | 0.168 | 0.186 | 0.199 | 0.209 | 0.215 | 0.219 | 0.222 |
| 15 | 0.028 | 0.070 | 0.109 | 0.140 | 0.165 | 0.182 | 0.195 | 0.204 | 0.211 | 0.215 | 0.217 |
| 17 | 0.027 | 0.067 | 0.106 | 0.137 | 0.161 | 0.179 | 0.191 | 0.200 | 0.206 | 0.210 | 0.212 |
| 10 | 0.065 | 0.103 | 0.134 | 0.157 | 0.175 | 0.187 | 0.196 | 0.202 | 0.206 | 0.207 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.024 | 0.063 | 0.100 | 0.131 | 0.154 | 0.171 | 0.183 | 0.192 | 0.198 | 0.201 | 0.203 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.023 | 0.060 | 0.097 | 0.127 | 0.150 | 0.167 | 0.180 | 0.188 | 0.194 | 0.197 | 0.198 |
| 20 | 0.022 | 0.058 | 0.094 | 0.124 | 0.147 | 0.164 | 0.176 | 0.184 | 0.190 | 0.193 | 0.194 |
| 21 | 0.021 | 0.056 | 0.092 | 0.121 | 0.144 | 0.160 | 0.172 | 0.181 | 0.186 | 0.189 | 0.190 |
| 22 | 0.019 | 0.054 | 0.089 | 0.118 | 0.140 | 0.157 | 0.169 | 0.177 | 0.182 | 0.185 | 0.186 |
| 23 | 0.018 | 0.052 | 0.086 | 0.115 | 0.137 | 0.154 | 0.165 | 0.173 | 0.178 | 0.181 | 0.182 |
| 24 | 0.017 | 0.050 | 0.084 | 0.112 | 0.134 | 0.150 | 0.162 | 0.170 | 0.175 | 0.177 | 0.178 |
| 25 | 0.016 | 0.048 | 0.081 | 0.109 | 0.131 | 0.147 | 0.159 | 0.166 | 0.171 | 0.174 | 0.174 |
| 26 | 0.015 | 0.046 | 0.079 | 0.107 | 0.128 | 0.144 | 0.155 | 0.163 | 0.168 | 0.170 | 0.171 |
| 27 | 0.015 | 0.044 | 0.077 | 0.104 | 0.125 | 0.141 | 0.152 | 0.160 | 0.164 | 0.167 | 0.167 |
| 28 | 0.014 | 0.043 | 0.074 | 0.101 | 0.122 | 0.138 | 0.149 | 0.157 | 0.161 | 0.163 | 0.164 |
| 29 | 0.013 | 0.041 | 0.072 | 0.099 | 0.120 | 0.135 | 0.146 | 0.153 | 0.158 | 0.160 | 0.161 |
| 20 | 0.012 | 0.040 | 0.070 | 0.096 | 0.117 | 0.132 | 0.143 | 0.150 | 0.155 | 0.157 | 0.157 |

Table C. 26
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 85 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.001 | 0.007 | 0.019 | 0.037 | 0.057 | 0.078 | 0.098 | 0.118 | 0.135 | 0.151 |
| 2 | 0.001 | 0.009 | 0.028 | 0.054 | 0.081 | 0.107 | 0.131 | 0.152 | 0.170 | 0.185 | 0.199 |
| 3 | 0.003 | 0.019 | 0.046 | 0.077 | 0.107 | 0.133 | 0.156 | 0.175 | 0.191 | 0.205 | 0.216 |
| 4 | 0.006 | 0.027 | 0.058 | 0.091 | 0.121 | 0.147 | 0.168 | 0.186 | 0.201 | 0.213 | 0.223 |
| 5 | 0.008 | 0.033 | 0.067 | 0.100 | 0.130 | 0.155 | 0.175 | 0.192 | 0.205 | 0.216 | 0.225 |
| 6 | 0.010 | 0.037 | 0.072 | 0.106 | 0.135 | 0.159 | 0.178 | 0.194 | 0.207 | 0.217 | 0.224 |
| 7 | 0.011 | 0.040 | 0.076 | 0.109 | 0.138 | 0.161 | 0.180 | 0.195 | 0.206 | 0.216 | 0.223 |
| 8 | 0.012 | 0.042 | 0.078 | 0.111 | 0.139 | 0.162 | 0.180 | 0.194 | 0.205 | 0.213 | 0.220 |
| 9 | 0.013 | 0.043 | 0.079 | 0.112 | 0.139 | 0.161 | 0.179 | 0.192 | 0.203 | 0.211 | 0.217 |
| 10 | 0.013 | 0.043 | 0.079 | 0.112 | 0.139 | 0.160 | 0.177 | 0.190 | 0.200 | 0.208 | 0.213 |
| 11 | 0.013 | 0.044 | 0.079 | 0.111 | 0.138 | 0.159 | 0.175 | 0.188 | 0.198 | 0.205 | 0.210 |
| 12 | 0.013 | 0.043 | 0.079 | 0.110 | 0.136 | 0.157 | 0.173 | 0.185 | 0.195 | 0.201 | 0.206 |
| 13 | 0.013 | 0.043 | 0.078 | 0.109 | 0.135 | 0.155 | 0.171 | 0.183 | 0.191 | 0.198 | 0.202 |
| 14 | 0.013 | 0.042 | 0.077 | 0.108 | 0.133 | 0.153 | 0.168 | 0.180 | 0.188 | 0.194 | 0.198 |
| 15 | 0.012 | 0.042 | 0.075 | 0.106 | 0.131 | 0.151 | 0.165 | 0.177 | 0.185 | 0.191 | 0.194 |
| 16 | 0.012 | 0.041 | 0.074 | 0.104 | 0.129 | 0.148 | 0.163 | 0.174 | 0.182 | 0.187 | 0.191 |
| 17 | 0.012 | 0.040 | 0.073 | 0.102 | 0.127 | 0.146 | 0.160 | 0.171 | 0.178 | 0.184 | 0.187 |


| 18 | 0.011 | 0.039 | 0.071 | 0.100 | 0.124 | 0.143 | 0.157 | 0.168 | 0.175 | 0.180 | 0.183 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.011 | 0.038 | 0.070 | 0.098 | 0.122 | 0.141 | 0.154 | 0.165 | 0.172 | 0.177 | 0.179 |
| 20 | 0.010 | 0.037 | 0.068 | 0.096 | 0.120 | 0.138 | 0.152 | 0.162 | 0.169 | 0.173 | 0.176 |
| 21 | 0.010 | 0.036 | 0.066 | 0.095 | 0.118 | 0.135 | 0.149 | 0.159 | 0.166 | 0.170 | 0.172 |
| 22 | 0.009 | 0.034 | 0.065 | 0.093 | 0.115 | 0.133 | 0.146 | 0.156 | 0.162 | 0.167 | 0.169 |
| 23 | 0.009 | 0.033 | 0.063 | 0.091 | 0.113 | 0.130 | 0.144 | 0.153 | 0.159 | 0.163 | 0.166 |
| 24 | 0.009 | 0.032 | 0.062 | 0.089 | 0.111 | 0.128 | 0.141 | 0.150 | 0.156 | 0.160 | 0.162 |
| 25 | 0.008 | 0.031 | 0.060 | 0.087 | 0.109 | 0.126 | 0.138 | 0.147 | 0.153 | 0.157 | 0.159 |
| 26 | 0.008 | 0.030 | 0.058 | 0.085 | 0.106 | 0.123 | 0.136 | 0.145 | 0.151 | 0.154 | 0.156 |
| 27 | 0.007 | 0.029 | 0.057 | 0.083 | 0.104 | 0.121 | 0.133 | 0.142 | 0.148 | 0.151 | 0.153 |
| 28 | 0.007 | 0.028 | 0.055 | 0.081 | 0.102 | 0.118 | 0.131 | 0.139 | 0.145 | 0.148 | 0.150 |
| 29 | 0.007 | 0.027 | 0.054 | 0.079 | 0.100 | 0.116 | 0.128 | 0.137 | 0.142 | 0.146 | 0.147 |
| 30 | 0.006 | 0.026 | 0.053 | 0.077 | 0.098 | 0.114 | 0.126 | 0.134 | 0.140 | 0.143 | 0.144 |

Table C. 27
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 80 /$ Annual Growth Rate $=\mathbf{1 0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.003 | 0.008 | 0.018 | 0.030 | 0.044 | 0.058 | 0.073 | 0.088 |
| 2 | 0.000 | 0.001 | 0.006 | 0.018 | 0.034 | 0.054 | 0.073 | 0.092 | 0.110 | 0.127 | 0.141 |
| 3 | 0.000 | 0.004 | 0.015 | 0.034 | 0.056 | 0.078 | 0.100 | 0.119 | 0.137 | 0.152 | 0.165 |
| 4 | 0.001 | 0.007 | 0.023 | 0.046 | 0.071 | 0.095 | 0.116 | 0.135 | 0.152 | 0.166 | 0.178 |
| 5 | 0.001 | 0.010 | 0.030 | 0.056 | 0.081 | 0.105 | 0.127 | 0.145 | 0.160 | 0.173 | 0.184 |
| 6 | 0.002 | 0.013 | 0.036 | 0.062 | 0.089 | 0.113 | 0.133 | 0.151 | 0.165 | 0.177 | 0.187 |
| 7 | 0.002 | 0.016 | 0.040 | 0.067 | 0.094 | 0.117 | 0.137 | 0.154 | 0.168 | 0.179 | 0.188 |
| 8 | 0.003 | 0.018 | 0.043 | 0.071 | 0.097 | 0.120 | 0.140 | 0.156 | 0.169 | 0.179 | 0.188 |
| 9 | 0.003 | 0.019 | 0.045 | 0.073 | 0.100 | 0.122 | 0.141 | 0.156 | 0.169 | 0.179 | 0.186 |
| 10 | 0.004 | 0.020 | 0.047 | 0.075 | 0.101 | 0.123 | 0.142 | 0.156 | 0.168 | 0.178 | 0.185 |
| 11 | 0.004 | 0.021 | 0.048 | 0.076 | 0.102 | 0.124 | 0.141 | 0.156 | 0.167 | 0.176 | 0.183 |
| 12 | 0.004 | 0.022 | 0.049 | 0.077 | 0.102 | 0.123 | 0.141 | 0.155 | 0.166 | 0.174 | 0.180 |
| 13 | 0.004 | 0.022 | 0.049 | 0.077 | 0.102 | 0.123 | 0.140 | 0.153 | 0.164 | 0.172 | 0.178 |
| 14 | 0.005 | 0.022 | 0.049 | 0.077 | 0.101 | 0.122 | 0.139 | 0.152 | 0.162 | 0.169 | 0.175 |
| 15 | 0.005 | 0.023 | 0.049 | 0.076 | 0.101 | 0.121 | 0.137 | 0.150 | 0.160 | 0.167 | 0.172 |
| 16 | 0.005 | 0.022 | 0.049 | 0.076 | 0.100 | 0.120 | 0.136 | 0.148 | 0.157 | 0.164 | 0.169 |
| 17 | 0.005 | 0.022 | 0.048 | 0.075 | 0.099 | 0.118 | 0.134 | 0.146 | 0.155 | 0.162 | 0.166 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.004 | 0.022 | 0.048 | 0.074 | 0.098 | 0.117 | 0.132 | 0.144 | 0.153 | 0.159 | 0.164 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.004 | 0.022 | 0.047 | 0.073 | 0.096 | 0.115 | 0.130 | 0.142 | 0.150 | 0.157 | 0.161 |
| 20 | 0.004 | 0.021 | 0.047 | 0.072 | 0.095 | 0.114 | 0.128 | 0.140 | 0.148 | 0.154 | 0.158 |
| 21 | 0.004 | 0.021 | 0.046 | 0.071 | 0.094 | 0.112 | 0.127 | 0.138 | 0.146 | 0.151 | 0.155 |
| 22 | 0.004 | 0.021 | 0.045 | 0.070 | 0.092 | 0.110 | 0.125 | 0.135 | 0.143 | 0.149 | 0.152 |
| 23 | 0.004 | 0.020 | 0.044 | 0.069 | 0.091 | 0.109 | 0.123 | 0.133 | 0.141 | 0.146 | 0.149 |
| 24 | 0.004 | 0.020 | 0.043 | 0.068 | 0.089 | 0.107 | 0.121 | 0.131 | 0.138 | 0.144 | 0.147 |
| 25 | 0.004 | 0.019 | 0.042 | 0.067 | 0.088 | 0.105 | 0.119 | 0.129 | 0.136 | 0.141 | 0.144 |
| 26 | 0.004 | 0.019 | 0.042 | 0.065 | 0.086 | 0.103 | 0.117 | 0.127 | 0.134 | 0.139 | 0.141 |
| 27 | 0.003 | 0.018 | 0.041 | 0.064 | 0.085 | 0.102 | 0.115 | 0.125 | 0.131 | 0.136 | 0.139 |
| 28 | 0.003 | 0.018 | 0.040 | 0.063 | 0.083 | 0.100 | 0.113 | 0.122 | 0.129 | 0.134 | 0.136 |
| 29 | 0.003 | 0.017 | 0.039 | 0.062 | 0.082 | 0.098 | 0.111 | 0.120 | 0.127 | 0.131 | 0.134 |
| 20 | 0.003 | 0.017 | 0.038 | 0.060 | 0.080 | 0.097 | 0.109 | 0.118 | 0.125 | 0.129 | 0.131 |

Table C. 28
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 120 /$ Annual Growth Rate $=\mathbf{1 5 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.000 | 0.998 | 0.988 | 0.969 | 0.943 | 0.915 | 0.886 | 0.858 | 0.831 | 0.806 | 0.784 |
| 2 | 0.991 | 0.961 | 0.918 | 0.873 | 0.831 | 0.794 | 0.761 | 0.732 | 0.707 | 0.684 | 0.664 |
| 3 | 0.955 | 0.894 | 0.835 | 0.785 | 0.744 | 0.709 | 0.679 | 0.653 | 0.631 | 0.611 | 0.594 |
| 4 | 0.895 | 0.820 | 0.760 | 0.713 | 0.675 | 0.645 | 0.619 | 0.597 | 0.577 | 0.560 | 0.544 |
| 5 | 0.824 | 0.749 | 0.694 | 0.653 | 0.620 | 0.594 | 0.572 | 0.553 | 0.536 | 0.520 | 0.506 |
| 6 | 0.750 | 0.683 | 0.636 | 0.602 | 0.575 | 0.552 | 0.533 | 0.517 | 0.502 | 0.488 | 0.475 |
| 7 | 0.679 | 0.624 | 0.586 | 0.558 | 0.536 | 0.517 | 0.501 | 0.486 | 0.473 | 0.461 | 0.449 |
| 8 | 0.612 | 0.570 | 0.542 | 0.520 | 0.502 | 0.487 | 0.473 | 0.460 | 0.448 | 0.437 | 0.426 |
| 9 | 0.550 | 0.523 | 0.503 | 0.486 | 0.472 | 0.460 | 0.448 | 0.437 | 0.426 | 0.416 | 0.406 |
| 10 | 0.494 | 0.480 | 0.467 | 0.456 | 0.446 | 0.435 | 0.426 | 0.416 | 0.407 | 0.397 | 0.388 |
| 11 | 0.443 | 0.441 | 0.436 | 0.429 | 0.422 | 0.414 | 0.406 | 0.397 | 0.389 | 0.380 | 0.372 |
| 12 | 0.398 | 0.406 | 0.407 | 0.404 | 0.400 | 0.394 | 0.387 | 0.380 | 0.372 | 0.365 | 0.357 |
| 13 | 0.357 | 0.374 | 0.381 | 0.382 | 0.380 | 0.376 | 0.370 | 0.364 | 0.358 | 0.350 | 0.343 |
| 14 | 0.320 | 0.345 | 0.357 | 0.361 | 0.361 | 0.359 | 0.355 | 0.350 | 0.344 | 0.337 | 0.330 |
| 15 | 0.287 | 0.319 | 0.335 | 0.342 | 0.344 | 0.344 | 0.341 | 0.336 | 0.331 | 0.325 | 0.318 |
| 16 | 0.258 | 0.295 | 0.315 | 0.325 | 0.329 | 0.329 | 0.327 | 0.324 | 0.319 | 0.313 | 0.307 |
| 17 | 0.231 | 0.273 | 0.296 | 0.308 | 0.314 | 0.316 | 0.315 | 0.312 | 0.307 | 0.302 | 0.296 |


| 18 | 0.208 | 0.253 | 0.279 | 0.293 | 0.300 | 0.303 | 0.303 | 0.301 | 0.297 | 0.292 | 0.286 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.187 | 0.235 | 0.263 | 0.279 | 0.287 | 0.291 | 0.292 | 0.290 | 0.287 | 0.282 | 0.277 |
| 20 | 0.168 | 0.218 | 0.248 | 0.265 | 0.275 | 0.280 | 0.281 | 0.280 | 0.277 | 0.273 | 0.268 |
| 21 | 0.151 | 0.203 | 0.234 | 0.253 | 0.264 | 0.269 | 0.271 | 0.271 | 0.268 | 0.264 | 0.259 |
| 22 | 0.136 | 0.188 | 0.221 | 0.241 | 0.253 | 0.259 | 0.262 | 0.262 | 0.260 | 0.256 | 0.251 |
| 23 | 0.122 | 0.175 | 0.209 | 0.230 | 0.243 | 0.250 | 0.253 | 0.253 | 0.251 | 0.248 | 0.244 |
| 24 | 0.110 | 0.163 | 0.198 | 0.220 | 0.233 | 0.241 | 0.245 | 0.245 | 0.244 | 0.241 | 0.236 |
| 25 | 0.099 | 0.152 | 0.187 | 0.210 | 0.224 | 0.233 | 0.236 | 0.237 | 0.236 | 0.233 | 0.229 |
| 26 | 0.089 | 0.142 | 0.177 | 0.201 | 0.216 | 0.224 | 0.229 | 0.230 | 0.229 | 0.227 | 0.223 |
| 27 | 0.080 | 0.132 | 0.168 | 0.192 | 0.207 | 0.217 | 0.221 | 0.223 | 0.222 | 0.220 | 0.216 |
| 28 | 0.072 | 0.123 | 0.159 | 0.184 | 0.200 | 0.209 | 0.214 | 0.216 | 0.216 | 0.214 | 0.210 |
| 29 | 0.065 | 0.115 | 0.151 | 0.176 | 0.192 | 0.202 | 0.208 | 0.210 | 0.210 | 0.208 | 0.204 |
| 20 | 0.059 | 0.107 | 0.144 | 0.169 | 0.185 | 0.195 | 0.201 | 0.204 | 0.204 | 0.202 | 0.198 |

Table C. 29
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 115 /$ Annual Growth Rate $=15 \%$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.997 | 0.982 | 0.951 | 0.914 | 0.877 | 0.842 | 0.810 | 0.781 | 0.755 | 0.732 | 0.711 |
| 2 | 0.954 | 0.893 | 0.835 | 0.786 | 0.746 | 0.712 | 0.684 | 0.660 | 0.638 | 0.620 | 0.603 |
| 3 | 0.870 | 0.795 | 0.737 | 0.694 | 0.660 | 0.632 | 0.608 | 0.589 | 0.571 | 0.556 | 0.542 |
| 4 | 0.777 | 0.708 | 0.660 | 0.624 | 0.596 | 0.574 | 0.555 | 0.539 | 0.524 | 0.511 | 0.499 |
| 5 | 0.688 | 0.633 | 0.596 | 0.569 | 0.547 | 0.529 | 0.514 | 0.500 | 0.488 | 0.477 | 0.466 |
| 6 | 0.608 | 0.570 | 0.543 | 0.523 | 0.507 | 0.493 | 0.480 | 0.469 | 0.458 | 0.448 | 0.439 |
| 7 | 0.537 | 0.515 | 0.498 | 0.484 | 0.472 | 0.462 | 0.452 | 0.442 | 0.433 | 0.424 | 0.415 |
| 8 | 0.475 | 0.467 | 0.459 | 0.451 | 0.443 | 0.435 | 0.427 | 0.419 | 0.411 | 0.403 | 0.395 |
| 9 | 0.420 | 0.425 | 0.425 | 0.421 | 0.417 | 0.411 | 0.405 | 0.398 | 0.392 | 0.384 | 0.377 |
| 10 | 0.372 | 0.388 | 0.394 | 0.395 | 0.394 | 0.390 | 0.385 | 0.380 | 0.374 | 0.368 | 0.361 |
| 11 | 0.330 | 0.355 | 0.367 | 0.372 | 0.373 | 0.371 | 0.368 | 0.363 | 0.358 | 0.352 | 0.346 |
| 12 | 0.293 | 0.326 | 0.342 | 0.350 | 0.354 | 0.354 | 0.352 | 0.348 | 0.344 | 0.338 | 0.332 |
| 13 | 0.261 | 0.300 | 0.320 | 0.331 | 0.336 | 0.338 | 0.337 | 0.334 | 0.330 | 0.325 | 0.320 |
| 14 | 0.233 | 0.276 | 0.300 | 0.313 | 0.320 | 0.323 | 0.323 | 0.321 | 0.318 | 0.313 | 0.308 |
| 15 | 0.207 | 0.254 | 0.281 | 0.297 | 0.305 | 0.309 | 0.310 | 0.309 | 0.306 | 0.302 | 0.297 |
| 16 | 0.185 | 0.235 | 0.264 | 0.282 | 0.291 | 0.296 | 0.298 | 0.298 | 0.295 | 0.292 | 0.287 |
| 17 | 0.165 | 0.217 | 0.249 | 0.268 | 0.279 | 0.285 | 0.287 | 0.287 | 0.285 | 0.282 | 0.277 |


| 18 | 0.148 | 0.201 | 0.234 | 0.254 | 0.267 | 0.273 | 0.276 | 0.277 | 0.275 | 0.272 | 0.268 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.132 | 0.186 | 0.221 | 0.242 | 0.255 | 0.263 | 0.266 | 0.267 | 0.266 | 0.263 | 0.260 |
| 20 | 0.118 | 0.173 | 0.208 | 0.231 | 0.245 | 0.253 | 0.257 | 0.258 | 0.257 | 0.255 | 0.251 |
| 21 | 0.106 | 0.160 | 0.197 | 0.220 | 0.235 | 0.244 | 0.248 | 0.250 | 0.249 | 0.247 | 0.244 |
| 22 | 0.095 | 0.149 | 0.186 | 0.210 | 0.225 | 0.235 | 0.240 | 0.242 | 0.241 | 0.239 | 0.236 |
| 23 | 0.085 | 0.138 | 0.176 | 0.200 | 0.216 | 0.226 | 0.232 | 0.234 | 0.234 | 0.232 | 0.229 |
| 24 | 0.077 | 0.129 | 0.166 | 0.191 | 0.208 | 0.218 | 0.224 | 0.227 | 0.227 | 0.225 | 0.222 |
| 25 | 0.069 | 0.120 | 0.157 | 0.183 | 0.200 | 0.211 | 0.217 | 0.220 | 0.220 | 0.219 | 0.216 |
| 26 | 0.062 | 0.112 | 0.149 | 0.175 | 0.192 | 0.203 | 0.210 | 0.213 | 0.214 | 0.212 | 0.210 |
| 27 | 0.056 | 0.104 | 0.141 | 0.167 | 0.185 | 0.196 | 0.203 | 0.206 | 0.207 | 0.206 | 0.204 |
| 28 | 0.050 | 0.097 | 0.134 | 0.160 | 0.178 | 0.190 | 0.197 | 0.200 | 0.201 | 0.200 | 0.198 |
| 29 | 0.045 | 0.090 | 0.127 | 0.153 | 0.172 | 0.183 | 0.191 | 0.194 | 0.196 | 0.195 | 0.192 |
| 30 | 0.041 | 0.084 | 0.121 | 0.147 | 0.165 | 0.177 | 0.185 | 0.189 | 0.190 | 0.189 | 0.187 |

Table C. 30
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 110 /$ Annual Growth Rate $=\mathbf{1 5 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.962 | 0.906 | 0.851 | 0.804 | 0.764 | 0.731 | 0.703 | 0.680 | 0.659 | 0.642 | 0.626 |
| 2 | 0.830 | 0.757 | 0.705 | 0.667 | 0.637 | 0.613 | 0.593 | 0.577 | 0.562 | 0.549 | 0.538 |
| 3 | 0.703 | 0.647 | 0.610 | 0.583 | 0.562 | 0.545 | 0.531 | 0.518 | 0.507 | 0.497 | 0.488 |
| 4 | 0.598 | 0.564 | 0.541 | 0.524 | 0.510 | 0.498 | 0.487 | 0.477 | 0.468 | 0.460 | 0.452 |
| 5 | 0.513 | 0.498 | 0.487 | 0.477 | 0.469 | 0.461 | 0.453 | 0.445 | 0.438 | 0.431 | 0.424 |
| 6 | 0.443 | 0.445 | 0.443 | 0.440 | 0.435 | 0.430 | 0.425 | 0.419 | 0.413 | 0.407 | 0.401 |
| 7 | 0.384 | 0.400 | 0.406 | 0.408 | 0.407 | 0.404 | 0.401 | 0.397 | 0.392 | 0.386 | 0.381 |
| 8 | 0.335 | 0.361 | 0.374 | 0.380 | 0.382 | 0.382 | 0.380 | 0.377 | 0.373 | 0.368 | 0.363 |
| 9 | 0.293 | 0.328 | 0.346 | 0.356 | 0.361 | 0.362 | 0.362 | 0.359 | 0.356 | 0.352 | 0.348 |
| 10 | 0.258 | 0.299 | 0.322 | 0.334 | 0.341 | 0.344 | 0.345 | 0.344 | 0.341 | 0.337 | 0.333 |
| 11 | 0.227 | 0.273 | 0.300 | 0.315 | 0.324 | 0.328 | 0.330 | 0.329 | 0.327 | 0.324 | 0.320 |
| 12 | 0.201 | 0.250 | 0.280 | 0.297 | 0.308 | 0.313 | 0.316 | 0.316 | 0.314 | 0.312 | 0.308 |
| 13 | 0.178 | 0.230 | 0.262 | 0.281 | 0.293 | 0.300 | 0.303 | 0.304 | 0.303 | 0.300 | 0.297 |
| 14 | 0.157 | 0.212 | 0.245 | 0.266 | 0.279 | 0.287 | 0.291 | 0.292 | 0.292 | 0.289 | 0.286 |
| 15 | 0.140 | 0.195 | 0.230 | 0.253 | 0.267 | 0.275 | 0.280 | 0.281 | 0.281 | 0.279 | 0.276 |
| 16 | 0.124 | 0.180 | 0.216 | 0.240 | 0.255 | 0.264 | 0.269 | 0.271 | 0.271 | 0.270 | 0.267 |
| 17 | 0.111 | 0.166 | 0.204 | 0.228 | 0.244 | 0.254 | 0.259 | 0.262 | 0.262 | 0.261 | 0.258 |


| 18 | 0.099 | 0.154 | 0.192 | 0.217 | 0.234 | 0.244 | 0.250 | 0.253 | 0.254 | 0.253 | 0.250 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.088 | 0.143 | 0.181 | 0.207 | 0.224 | 0.235 | 0.241 | 0.245 | 0.245 | 0.245 | 0.242 |
| 20 | 0.079 | 0.132 | 0.171 | 0.197 | 0.215 | 0.226 | 0.233 | 0.237 | 0.238 | 0.237 | 0.235 |
| 21 | 0.071 | 0.123 | 0.161 | 0.188 | 0.206 | 0.218 | 0.225 | 0.229 | 0.230 | 0.230 | 0.228 |
| 22 | 0.063 | 0.114 | 0.153 | 0.180 | 0.198 | 0.210 | 0.218 | 0.222 | 0.223 | 0.223 | 0.221 |
| 23 | 0.057 | 0.106 | 0.144 | 0.172 | 0.190 | 0.203 | 0.211 | 0.215 | 0.216 | 0.216 | 0.214 |
| 24 | 0.051 | 0.099 | 0.137 | 0.164 | 0.183 | 0.196 | 0.204 | 0.208 | 0.210 | 0.210 | 0.208 |
| 25 | 0.046 | 0.092 | 0.129 | 0.157 | 0.176 | 0.189 | 0.197 | 0.202 | 0.204 | 0.204 | 0.202 |
| 26 | 0.041 | 0.085 | 0.123 | 0.150 | 0.170 | 0.183 | 0.191 | 0.196 | 0.198 | 0.198 | 0.196 |
| 27 | 0.037 | 0.080 | 0.116 | 0.144 | 0.163 | 0.177 | 0.185 | 0.190 | 0.192 | 0.192 | 0.191 |
| 28 | 0.033 | 0.074 | 0.110 | 0.138 | 0.157 | 0.171 | 0.179 | 0.184 | 0.187 | 0.187 | 0.186 |
| 29 | 0.030 | 0.069 | 0.105 | 0.132 | 0.152 | 0.165 | 0.174 | 0.179 | 0.182 | 0.182 | 0.181 |
| 30 | 0.027 | 0.065 | 0.099 | 0.127 | 0.146 | 0.160 | 0.169 | 0.174 | 0.176 | 0.177 | 0.176 |

Table C. 31
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 105 /$ Annual Growth Rate $=\mathbf{1 5 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.758 | 0.696 | 0.654 | 0.625 | 0.602 | 0.584 | 0.570 | 0.558 | 0.547 | 0.537 | 0.529 |
| 2 | 0.577 | 0.551 | 0.534 | 0.520 | 0.510 | 0.501 | 0.493 | 0.486 | 0.480 | 0.474 | 0.468 |
| 3 | 0.465 | 0.465 | 0.463 | 0.460 | 0.457 | 0.453 | 0.449 | 0.444 | 0.440 | 0.436 | 0.431 |
| 4 | 0.387 | 0.405 | 0.413 | 0.417 | 0.418 | 0.418 | 0.416 | 0.414 | 0.411 | 0.407 | 0.404 |
| 5 | 0.327 | 0.358 | 0.374 | 0.383 | 0.388 | 0.390 | 0.390 | 0.389 | 0.387 | 0.385 | 0.381 |
| 6 | 0.280 | 0.320 | 0.342 | 0.355 | 0.363 | 0.367 | 0.369 | 0.369 | 0.367 | 0.365 | 0.362 |
| 7 | 0.242 | 0.288 | 0.315 | 0.331 | 0.341 | 0.347 | 0.350 | 0.351 | 0.350 | 0.348 | 0.346 |
| 8 | 0.210 | 0.261 | 0.292 | 0.310 | 0.322 | 0.329 | 0.333 | 0.335 | 0.334 | 0.333 | 0.331 |
| 9 | 0.184 | 0.238 | 0.271 | 0.292 | 0.305 | 0.313 | 0.318 | 0.320 | 0.320 | 0.320 | 0.318 |
| 10 | 0.161 | 0.217 | 0.252 | 0.275 | 0.290 | 0.299 | 0.304 | 0.307 | 0.308 | 0.307 | 0.305 |
| 11 | 0.142 | 0.199 | 0.236 | 0.260 | 0.275 | 0.285 | 0.292 | 0.295 | 0.296 | 0.296 | 0.294 |
| 12 | 0.125 | 0.182 | 0.221 | 0.246 | 0.263 | 0.273 | 0.280 | 0.284 | 0.285 | 0.285 | 0.283 |
| 13 | 0.111 | 0.168 | 0.207 | 0.233 | 0.251 | 0.262 | 0.269 | 0.273 | 0.275 | 0.275 | 0.273 |
| 14 | 0.098 | 0.155 | 0.194 | 0.221 | 0.239 | 0.251 | 0.259 | 0.263 | 0.265 | 0.265 | 0.264 |
| 15 | 0.087 | 0.143 | 0.183 | 0.210 | 0.229 | 0.242 | 0.249 | 0.254 | 0.256 | 0.257 | 0.255 |
| 16 | 0.078 | 0.132 | 0.172 | 0.200 | 0.219 | 0.232 | 0.240 | 0.245 | 0.248 | 0.248 | 0.247 |
| 17 | 0.069 | 0.122 | 0.162 | 0.191 | 0.210 | 0.223 | 0.232 | 0.237 | 0.240 | 0.240 | 0.239 |


| 18 | 0.062 | 0.113 | 0.153 | 0.182 | 0.202 | 0.215 | 0.224 | 0.229 | 0.232 | 0.233 | 0.232 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.055 | 0.105 | 0.145 | 0.174 | 0.194 | 0.207 | 0.216 | 0.222 | 0.225 | 0.226 | 0.225 |
| 20 | 0.049 | 0.098 | 0.137 | 0.166 | 0.186 | 0.200 | 0.209 | 0.215 | 0.218 | 0.219 | 0.218 |
| 21 | 0.044 | 0.091 | 0.129 | 0.158 | 0.179 | 0.193 | 0.202 | 0.208 | 0.211 | 0.212 | 0.212 |
| 22 | 0.039 | 0.084 | 0.123 | 0.151 | 0.172 | 0.186 | 0.196 | 0.202 | 0.205 | 0.206 | 0.206 |
| 23 | 0.035 | 0.078 | 0.116 | 0.145 | 0.165 | 0.180 | 0.190 | 0.196 | 0.199 | 0.200 | 0.200 |
| 24 | 0.032 | 0.073 | 0.110 | 0.138 | 0.159 | 0.174 | 0.184 | 0.190 | 0.193 | 0.194 | 0.194 |
| 25 | 0.028 | 0.068 | 0.104 | 0.133 | 0.153 | 0.168 | 0.178 | 0.184 | 0.188 | 0.189 | 0.189 |
| 26 | 0.026 | 0.063 | 0.099 | 0.127 | 0.148 | 0.162 | 0.172 | 0.179 | 0.182 | 0.184 | 0.183 |
| 27 | 0.023 | 0.059 | 0.094 | 0.122 | 0.142 | 0.157 | 0.167 | 0.174 | 0.177 | 0.179 | 0.178 |
| 28 | 0.021 | 0.055 | 0.089 | 0.117 | 0.137 | 0.152 | 0.162 | 0.169 | 0.172 | 0.174 | 0.173 |
| 29 | 0.019 | 0.051 | 0.085 | 0.112 | 0.132 | 0.147 | 0.157 | 0.164 | 0.168 | 0.169 | 0.169 |
| 30 | 0.017 | 0.048 | 0.080 | 0.107 | 0.128 | 0.142 | 0.153 | 0.159 | 0.163 | 0.164 | 0.164 |

Table C. 32
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 100 /$ Annual Growth Rate $=\mathbf{1 5 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.335 | 0.370 | 0.390 | 0.403 | 0.411 | 0.417 | 0.421 | 0.423 | 0.425 | 0.426 | 0.426 |
| 2 | 0.274 | 0.319 | 0.347 | 0.364 | 0.376 | 0.384 | 0.389 | 0.392 | 0.394 | 0.395 | 0.396 |
| 3 | 0.230 | 0.283 | 0.315 | 0.335 | 0.349 | 0.358 | 0.365 | 0.369 | 0.371 | 0.373 | 0.373 |
| 4 | 0.197 | 0.253 | 0.289 | 0.312 | 0.327 | 0.338 | 0.345 | 0.349 | 0.352 | 0.354 | 0.354 |
| 5 | 0.171 | 0.229 | 0.267 | 0.292 | 0.308 | 0.320 | 0.328 | 0.333 | 0.336 | 0.337 | 0.338 |
| 6 | 0.148 | 0.208 | 0.248 | 0.274 | 0.292 | 0.304 | 0.312 | 0.318 | 0.321 | 0.323 | 0.323 |
| 7 | 0.130 | 0.190 | 0.231 | 0.258 | 0.277 | 0.290 | 0.299 | 0.304 | 0.308 | 0.310 | 0.310 |
| 8 | 0.114 | 0.174 | 0.215 | 0.244 | 0.263 | 0.277 | 0.286 | 0.292 | 0.296 | 0.298 | 0.298 |
| 9 | 0.101 | 0.160 | 0.202 | 0.231 | 0.251 | 0.265 | 0.275 | 0.281 | 0.285 | 0.287 | 0.287 |
| 10 | 0.089 | 0.147 | 0.189 | 0.219 | 0.240 | 0.254 | 0.264 | 0.270 | 0.274 | 0.276 | 0.277 |
| 11 | 0.079 | 0.135 | 0.178 | 0.208 | 0.229 | 0.244 | 0.254 | 0.261 | 0.265 | 0.267 | 0.267 |
| 12 | 0.070 | 0.125 | 0.167 | 0.198 | 0.219 | 0.234 | 0.245 | 0.251 | 0.256 | 0.258 | 0.258 |
| 13 | 0.062 | 0.116 | 0.158 | 0.188 | 0.210 | 0.225 | 0.236 | 0.243 | 0.247 | 0.249 | 0.250 |
| 14 | 0.056 | 0.107 | 0.149 | 0.179 | 0.201 | 0.217 | 0.228 | 0.235 | 0.239 | 0.241 | 0.242 |
| 15 | 0.050 | 0.099 | 0.140 | 0.171 | 0.193 | 0.209 | 0.220 | 0.227 | 0.231 | 0.234 | 0.234 |
| 16 | 0.044 | 0.092 | 0.133 | 0.163 | 0.185 | 0.201 | 0.212 | 0.220 | 0.224 | 0.226 | 0.227 |
| 17 | 0.040 | 0.086 | 0.125 | 0.156 | 0.178 | 0.194 | 0.205 | 0.213 | 0.217 | 0.220 | 0.220 |


| 18 | 0.035 | 0.079 | 0.119 | 0.149 | 0.171 | 0.187 | 0.198 | 0.206 | 0.211 | 0.213 | 0.214 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.032 | 0.074 | 0.112 | 0.142 | 0.165 | 0.181 | 0.192 | 0.200 | 0.204 | 0.207 | 0.207 |
| 20 | 0.028 | 0.069 | 0.106 | 0.136 | 0.159 | 0.175 | 0.186 | 0.194 | 0.198 | 0.201 | 0.201 |
| 21 | 0.026 | 0.064 | 0.101 | 0.130 | 0.153 | 0.169 | 0.180 | 0.188 | 0.192 | 0.195 | 0.196 |
| 22 | 0.023 | 0.060 | 0.096 | 0.125 | 0.147 | 0.163 | 0.174 | 0.182 | 0.187 | 0.189 | 0.190 |
| 23 | 0.021 | 0.056 | 0.091 | 0.120 | 0.142 | 0.158 | 0.169 | 0.177 | 0.182 | 0.184 | 0.185 |
| 24 | 0.019 | 0.052 | 0.086 | 0.115 | 0.137 | 0.153 | 0.164 | 0.172 | 0.176 | 0.179 | 0.180 |
| 25 | 0.017 | 0.048 | 0.082 | 0.110 | 0.132 | 0.148 | 0.159 | 0.167 | 0.172 | 0.174 | 0.175 |
| 26 | 0.015 | 0.045 | 0.078 | 0.105 | 0.127 | 0.143 | 0.154 | 0.162 | 0.167 | 0.169 | 0.170 |
| 27 | 0.013 | 0.042 | 0.074 | 0.101 | 0.123 | 0.138 | 0.150 | 0.157 | 0.162 | 0.165 | 0.165 |
| 28 | 0.012 | 0.039 | 0.070 | 0.097 | 0.118 | 0.134 | 0.145 | 0.153 | 0.158 | 0.160 | 0.161 |
| 29 | 0.011 | 0.037 | 0.087 | 0.093 | 0.114 | 0.130 | 0.141 | 0.149 | 0.154 | 0.156 | 0.157 |
| 20 | 0.010 | 0.035 | 0.064 | 0.089 | 0.110 | 0.126 | 0.137 | 0.145 | 0.150 | 0.152 | 0.153 |

Table C. 33
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 95 /$ Annual Growth Rate $=\mathbf{1 5} \%$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.054 | 0.111 | 0.161 | 0.201 | 0.232 | 0.257 | 0.276 | 0.292 | 0.304 | 0.314 | 0.323 |
| 2 | 0.075 | 0.136 | 0.185 | 0.222 | 0.250 | 0.271 | 0.287 | 0.300 | 0.310 | 0.317 | 0.324 |
| 3 | 0.078 | 0.138 | 0.186 | 0.222 | 0.248 | 0.268 | 0.283 | 0.295 | 0.303 | 0.310 | 0.315 |
| 4 | 0.074 | 0.134 | 0.181 | 0.216 | 0.242 | 0.261 | 0.275 | 0.286 | 0.294 | 0.300 | 0.305 |
| 5 | 0.069 | 0.127 | 0.173 | 0.208 | 0.234 | 0.253 | 0.267 | 0.277 | 0.285 | 0.290 | 0.294 |
| 6 | 0.063 | 0.120 | 0.165 | 0.200 | 0.225 | 0.244 | 0.258 | 0.268 | 0.275 | 0.281 | 0.284 |
| 7 | 0.058 | 0.112 | 0.157 | 0.191 | 0.217 | 0.235 | 0.249 | 0.259 | 0.266 | 0.271 | 0.275 |
| 8 | 0.052 | 0.105 | 0.149 | 0.183 | 0.208 | 0.227 | 0.241 | 0.251 | 0.258 | 0.263 | 0.266 |
| 9 | 0.047 | 0.098 | 0.142 | 0.175 | 0.200 | 0.219 | 0.233 | 0.242 | 0.249 | 0.254 | 0.257 |
| 10 | 0.043 | 0.092 | 0.134 | 0.168 | 0.193 | 0.211 | 0.225 | 0.235 | 0.241 | 0.246 | 0.249 |
| 11 | 0.038 | 0.086 | 0.128 | 0.160 | 0.185 | 0.204 | 0.217 | 0.227 | 0.234 | 0.238 | 0.241 |
| 12 | 0.035 | 0.080 | 0.121 | 0.154 | 0.178 | 0.197 | 0.210 | 0.220 | 0.227 | 0.231 | 0.234 |
| 13 | 0.031 | 0.074 | 0.115 | 0.147 | 0.172 | 0.190 | 0.203 | 0.213 | 0.220 | 0.224 | 0.227 |
| 14 | 0.028 | 0.069 | 0.109 | 0.141 | 0.165 | 0.184 | 0.197 | 0.206 | 0.213 | 0.217 | 0.220 |
| 15 | 0.025 | 0.065 | 0.103 | 0.135 | 0.159 | 0.177 | 0.191 | 0.200 | 0.207 | 0.211 | 0.213 |
| 17 | 0.023 | 0.061 | 0.098 | 0.129 | 0.153 | 0.172 | 0.185 | 0.194 | 0.201 | 0.205 | 0.207 |
| 10.057 | 0.093 | 0.124 | 0.148 | 0.166 | 0.179 | 0.188 | 0.195 | 0.199 | 0.201 |  |  |


| 18 | 0.019 | 0.053 | 0.089 | 0.119 | 0.143 | 0.160 | 0.174 | 0.183 | 0.189 | 0.193 | 0.195 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.017 | 0.049 | 0.084 | 0.114 | 0.137 | 0.155 | 0.168 | 0.178 | 0.184 | 0.188 | 0.190 |
| 20 | 0.015 | 0.046 | 0.080 | 0.109 | 0.133 | 0.150 | 0.163 | 0.172 | 0.179 | 0.183 | 0.185 |
| 21 | 0.014 | 0.043 | 0.076 | 0.105 | 0.128 | 0.145 | 0.158 | 0.168 | 0.174 | 0.178 | 0.180 |
| 22 | 0.012 | 0.040 | 0.072 | 0.101 | 0.124 | 0.141 | 0.154 | 0.163 | 0.169 | 0.173 | 0.175 |
| 23 | 0.011 | 0.038 | 0.069 | 0.097 | 0.119 | 0.136 | 0.149 | 0.158 | 0.164 | 0.168 | 0.170 |
| 24 | 0.010 | 0.035 | 0.066 | 0.093 | 0.115 | 0.132 | 0.145 | 0.154 | 0.160 | 0.164 | 0.165 |
| 25 | 0.009 | 0.033 | 0.062 | 0.089 | 0.111 | 0.128 | 0.141 | 0.150 | 0.156 | 0.159 | 0.161 |
| 26 | 0.008 | 0.031 | 0.059 | 0.086 | 0.107 | 0.124 | 0.137 | 0.145 | 0.151 | 0.155 | 0.157 |
| 27 | 0.007 | 0.029 | 0.057 | 0.082 | 0.104 | 0.120 | 0.133 | 0.142 | 0.147 | 0.151 | 0.153 |
| 28 | 0.007 | 0.027 | 0.054 | 0.079 | 0.100 | 0.117 | 0.129 | 0.138 | 0.144 | 0.147 | 0.149 |
| 29 | 0.006 | 0.025 | 0.051 | 0.076 | 0.097 | 0.113 | 0.125 | 0.134 | 0.140 | 0.143 | 0.145 |
| 30 | 0.005 | 0.024 | 0.049 | 0.073 | 0.094 | 0.110 | 0.122 | 0.130 | 0.136 | 0.140 | 0.141 |

Table C. 34
Probability of a Put Expiring in the Money as a Function of Time and Volatility

Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 90 /$ Annual Growth Rate $=\mathbf{1 5 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.002 | 0.016 | 0.041 | 0.072 | 0.103 | 0.131 | 0.156 | 0.178 | 0.197 | 0.213 | 0.227 |
| 2 | 0.010 | 0.039 | 0.077 | 0.114 | 0.146 | 0.173 | 0.196 | 0.215 | 0.230 | 0.243 | 0.254 |
| 3 | 0.016 | 0.052 | 0.093 | 0.130 | 0.161 | 0.187 | 0.208 | 0.225 | 0.238 | 0.249 | 0.258 |
| 4 | 0.019 | 0.057 | 0.099 | 0.136 | 0.166 | 0.191 | 0.210 | 0.226 | 0.239 | 0.248 | 0.256 |
| 5 | 0.021 | 0.060 | 0.101 | 0.137 | 0.167 | 0.191 | 0.209 | 0.224 | 0.236 | 0.245 | 0.252 |
| 6 | 0.021 | 0.060 | 0.101 | 0.136 | 0.165 | 0.188 | 0.206 | 0.220 | 0.231 | 0.239 | 0.246 |
| 7 | 0.020 | 0.058 | 0.099 | 0.134 | 0.162 | 0.184 | 0.202 | 0.215 | 0.226 | 0.234 | 0.240 |
| 8 | 0.019 | 0.057 | 0.096 | 0.130 | 0.158 | 0.180 | 0.197 | 0.210 | 0.220 | 0.228 | 0.233 |
| 9 | 0.018 | 0.054 | 0.093 | 0.127 | 0.154 | 0.176 | 0.192 | 0.205 | 0.215 | 0.222 | 0.227 |
| 10 | 0.017 | 0.052 | 0.090 | 0.123 | 0.150 | 0.171 | 0.187 | 0.200 | 0.209 | 0.216 | 0.221 |
| 11 | 0.016 | 0.049 | 0.086 | 0.119 | 0.145 | 0.166 | 0.182 | 0.194 | 0.204 | 0.210 | 0.215 |
| 12 | 0.015 | 0.047 | 0.083 | 0.115 | 0.141 | 0.161 | 0.177 | 0.189 | 0.198 | 0.205 | 0.209 |
| 13 | 0.014 | 0.044 | 0.079 | 0.111 | 0.137 | 0.157 | 0.172 | 0.184 | 0.193 | 0.199 | 0.203 |
| 14 | 0.012 | 0.042 | 0.076 | 0.107 | 0.132 | 0.152 | 0.168 | 0.179 | 0.188 | 0.194 | 0.198 |
| 15 | 0.011 | 0.039 | 0.073 | 0.103 | 0.128 | 0.148 | 0.163 | 0.174 | 0.183 | 0.188 | 0.192 |
| 17 | 0.010 | 0.037 | 0.070 | 0.099 | 0.124 | 0.143 | 0.158 | 0.169 | 0.178 | 0.183 | 0.187 |
| 17 | 0.010 | 0.035 | 0.066 | 0.096 | 0.120 | 0.139 | 0.154 | 0.165 | 0.173 | 0.178 | 0.182 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.009 | 0.033 | 0.084 | 0.092 | 0.116 | 0.135 | 0.150 | 0.160 | 0.168 | 0.174 | 0.177 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.008 | 0.031 | 0.061 | 0.089 | 0.112 | 0.131 | 0.145 | 0.156 | 0.164 | 0.169 | 0.173 |
| 20 | 0.007 | 0.029 | 0.058 | 0.085 | 0.109 | 0.127 | 0.141 | 0.152 | 0.160 | 0.165 | 0.168 |
| 21 | 0.007 | 0.027 | 0.055 | 0.082 | 0.105 | 0.123 | 0.137 | 0.148 | 0.155 | 0.160 | 0.164 |
| 22 | 0.006 | 0.026 | 0.053 | 0.079 | 0.102 | 0.120 | 0.134 | 0.144 | 0.151 | 0.156 | 0.159 |
| 23 | 0.005 | 0.024 | 0.050 | 0.076 | 0.098 | 0.116 | 0.130 | 0.140 | 0.147 | 0.152 | 0.155 |
| 24 | 0.005 | 0.023 | 0.048 | 0.073 | 0.095 | 0.113 | 0.126 | 0.136 | 0.144 | 0.148 | 0.151 |
| 25 | 0.004 | 0.021 | 0.046 | 0.071 | 0.092 | 0.110 | 0.123 | 0.133 | 0.140 | 0.145 | 0.147 |
| 26 | 0.004 | 0.020 | 0.044 | 0.068 | 0.089 | 0.106 | 0.120 | 0.129 | 0.136 | 0.141 | 0.144 |
| 27 | 0.004 | 0.019 | 0.042 | 0.066 | 0.086 | 0.103 | 0.116 | 0.126 | 0.133 | 0.137 | 0.140 |
| 28 | 0.003 | 0.018 | 0.040 | 0.063 | 0.084 | 0.100 | 0.113 | 0.123 | 0.129 | 0.134 | 0.137 |
| 29 | 0.003 | 0.017 | 0.038 | 0.061 | 0.081 | 0.097 | 0.110 | 0.120 | 0.126 | 0.131 | 0.133 |
| 20 | 0.003 | 0.016 | 0.037 | 0.059 | 0.078 | 0.095 | 0.107 | 0.116 | 0.123 | 0.127 | 0.130 |

Table C. 35
Probability of a Put Expiring in the Money as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 85 /$ Annual Growth Rate $=\mathbf{1 5 \%}$

Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.001 | 0.006 | 0.017 | 0.033 | 0.053 | 0.073 | 0.094 | 0.113 | 0.130 | 0.146 |
| 2 | 0.001 | 0.007 | 0.024 | 0.047 | 0.073 | 0.098 | 0.122 | 0.142 | 0.161 | 0.176 | 0.190 |
| 3 | 0.002 | 0.014 | 0.037 | 0.066 | 0.094 | 0.120 | 0.143 | 0.162 | 0.179 | 0.193 | 0.205 |
| 4 | 0.003 | 0.019 | 0.046 | 0.076 | 0.105 | 0.131 | 0.153 | 0.171 | 0.186 | 0.199 | 0.210 |
| 5 | 0.004 | 0.023 | 0.052 | 0.083 | 0.111 | 0.136 | 0.157 | 0.175 | 0.189 | 0.201 | 0.210 |
| 6 | 0.005 | 0.025 | 0.055 | 0.086 | 0.114 | 0.138 | 0.159 | 0.175 | 0.189 | 0.200 | 0.208 |
| 7 | 0.005 | 0.026 | 0.056 | 0.087 | 0.115 | 0.139 | 0.158 | 0.174 | 0.187 | 0.197 | 0.205 |
| 8 | 0.006 | 0.027 | 0.057 | 0.087 | 0.115 | 0.138 | 0.157 | 0.172 | 0.185 | 0.194 | 0.202 |
| 9 | 0.006 | 0.027 | 0.056 | 0.087 | 0.114 | 0.136 | 0.155 | 0.170 | 0.181 | 0.191 | 0.198 |
| 10 | 0.006 | 0.026 | 0.056 | 0.085 | 0.112 | 0.134 | 0.152 | 0.167 | 0.178 | 0.187 | 0.193 |
| 11 | 0.005 | 0.026 | 0.054 | 0.084 | 0.110 | 0.132 | 0.149 | 0.163 | 0.174 | 0.183 | 0.189 |
| 12 | 0.005 | 0.025 | 0.053 | 0.082 | 0.108 | 0.129 | 0.146 | 0.160 | 0.170 | 0.179 | 0.185 |
| 13 | 0.005 | 0.024 | 0.052 | 0.080 | 0.105 | 0.126 | 0.143 | 0.156 | 0.167 | 0.174 | 0.180 |
| 14 | 0.005 | 0.023 | 0.050 | 0.078 | 0.103 | 0.123 | 0.140 | 0.153 | 0.163 | 0.170 | 0.176 |
| 15 | 0.004 | 0.022 | 0.048 | 0.076 | 0.100 | 0.120 | 0.136 | 0.149 | 0.159 | 0.166 | 0.172 |
| 16 | 0.004 | 0.021 | 0.047 | 0.073 | 0.097 | 0.117 | 0.133 | 0.146 | 0.155 | 0.162 | 0.167 |
| 17 | 0.004 | 0.020 | 0.045 | 0.071 | 0.095 | 0.114 | 0.130 | 0.142 | 0.151 | 0.158 | 0.163 |


| 18 | 0.004 | 0.019 | 0.043 | 0.069 | 0.092 | 0.111 | 0.127 | 0.139 | 0.148 | 0.155 | 0.159 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.003 | 0.018 | 0.042 | 0.067 | 0.089 | 0.108 | 0.124 | 0.135 | 0.144 | 0.151 | 0.155 |
| 20 | 0.003 | 0.017 | 0.040 | 0.065 | 0.087 | 0.106 | 0.120 | 0.132 | 0.141 | 0.147 | 0.151 |
| 21 | 0.003 | 0.016 | 0.039 | 0.063 | 0.084 | 0.103 | 0.117 | 0.129 | 0.137 | 0.144 | 0.148 |
| 22 | 0.003 | 0.016 | 0.037 | 0.060 | 0.082 | 0.100 | 0.114 | 0.126 | 0.134 | 0.140 | 0.144 |
| 23 | 0.002 | 0.015 | 0.035 | 0.058 | 0.080 | 0.097 | 0.112 | 0.123 | 0.131 | 0.137 | 0.141 |
| 24 | 0.002 | 0.014 | 0.034 | 0.056 | 0.077 | 0.095 | 0.109 | 0.120 | 0.128 | 0.133 | 0.137 |
| 25 | 0.002 | 0.013 | 0.033 | 0.055 | 0.075 | 0.092 | 0.106 | 0.117 | 0.124 | 0.130 | 0.134 |
| 26 | 0.002 | 0.012 | 0.031 | 0.053 | 0.073 | 0.090 | 0.103 | 0.114 | 0.121 | 0.127 | 0.131 |
| 27 | 0.002 | 0.012 | 0.030 | 0.051 | 0.070 | 0.087 | 0.101 | 0.111 | 0.119 | 0.124 | 0.127 |
| 28 | 0.002 | 0.011 | 0.029 | 0.049 | 0.068 | 0.085 | 0.098 | 0.108 | 0.116 | 0.121 | 0.124 |
| 29 | 0.001 | 0.010 | 0.028 | 0.047 | 0.066 | 0.082 | 0.096 | 0.106 | 0.113 | 0.118 | 0.121 |
| 30 | 0.001 | 0.010 | 0.026 | 0.046 | 0.064 | 0.080 | 0.093 | 0.103 | 0.110 | 0.115 | 0.118 |

Table C. 36
Probability of a Put Expiring in the Money as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 80 /$ Annual Growth Rate $=\mathbf{1 5 \%}$

## Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.002 | 0.008 | 0.016 | 0.028 | 0.041 | 0.055 | 0.070 | 0.084 |
| 2 | 0.000 | 0.001 | 0.005 | 0.015 | 0.030 | 0.048 | 0.067 | 0.086 | 0.103 | 0.120 | 0.134 |
| 3 | 0.000 | 0.003 | 0.012 | 0.028 | 0.048 | 0.070 | 0.091 | 0.110 | 0.127 | 0.143 | 0.156 |
| 4 | 0.000 | 0.005 | 0.018 | 0.038 | 0.060 | 0.083 | 0.104 | 0.123 | 0.140 | 0.154 | 0.166 |
| 5 | 0.001 | 0.007 | 0.022 | 0.044 | 0.068 | 0.091 | 0.112 | 0.131 | 0.146 | 0.160 | 0.171 |
| 6 | 0.001 | 0.008 | 0.026 | 0.049 | 0.074 | 0.097 | 0.117 | 0.135 | 0.150 | 0.162 | 0.173 |
| 7 | 0.001 | 0.010 | 0.028 | 0.052 | 0.077 | 0.100 | 0.119 | 0.137 | 0.151 | 0.163 | 0.172 |
| 8 | 0.001 | 0.011 | 0.030 | 0.054 | 0.079 | 0.101 | 0.121 | 0.137 | 0.151 | 0.162 | 0.171 |
| 9 | 0.001 | 0.011 | 0.031 | 0.055 | 0.080 | 0.102 | 0.121 | 0.137 | 0.150 | 0.161 | 0.169 |
| 10 | 0.001 | 0.012 | 0.032 | 0.056 | 0.080 | 0.102 | 0.120 | 0.136 | 0.148 | 0.158 | 0.167 |
| 11 | 0.002 | 0.012 | 0.032 | 0.056 | 0.080 | 0.101 | 0.119 | 0.134 | 0.146 | 0.156 | 0.164 |
| 12 | 0.002 | 0.012 | 0.032 | 0.055 | 0.079 | 0.100 | 0.117 | 0.132 | 0.144 | 0.153 | 0.161 |
| 13 | 0.002 | 0.012 | 0.031 | 0.055 | 0.078 | 0.098 | 0.116 | 0.130 | 0.142 | 0.151 | 0.158 |
| 14 | 0.001 | 0.011 | 0.031 | 0.054 | 0.077 | 0.097 | 0.114 | 0.128 | 0.139 | 0.148 | 0.154 |
| 15 | 0.001 | 0.011 | 0.030 | 0.053 | 0.075 | 0.095 | 0.112 | 0.125 | 0.136 | 0.145 | 0.151 |
| 16 | 0.001 | 0.011 | 0.030 | 0.052 | 0.074 | 0.093 | 0.110 | 0.123 | 0.134 | 0.142 | 0.148 |
| 17 | 0.001 | 0.011 | 0.029 | 0.051 | 0.072 | 0.091 | 0.108 | 0.121 | 0.131 | 0.139 | 0.145 |


| 18 | 0.001 | 0.010 | 0.028 | 0.050 | 0.071 | 0.090 | 0.105 | 0.118 | 0.128 | 0.136 | 0.141 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.001 | 0.010 | 0.027 | 0.048 | 0.069 | 0.088 | 0.103 | 0.115 | 0.125 | 0.133 | 0.138 |
| 20 | 0.001 | 0.009 | 0.026 | 0.047 | 0.068 | 0.086 | 0.101 | 0.113 | 0.123 | 0.130 | 0.135 |
| 21 | 0.001 | 0.009 | 0.026 | 0.046 | 0.066 | 0.084 | 0.099 | 0.111 | 0.120 | 0.127 | 0.132 |
| 22 | 0.001 | 0.009 | 0.025 | 0.045 | 0.064 | 0.082 | 0.096 | 0.108 | 0.117 | 0.124 | 0.129 |
| 23 | 0.001 | 0.008 | 0.024 | 0.043 | 0.063 | 0.080 | 0.094 | 0.106 | 0.115 | 0.121 | 0.126 |
| 24 | 0.001 | 0.008 | 0.023 | 0.042 | 0.061 | 0.078 | 0.092 | 0.103 | 0.112 | 0.119 | 0.123 |
| 25 | 0.001 | 0.008 | 0.022 | 0.041 | 0.059 | 0.076 | 0.090 | 0.101 | 0.110 | 0.116 | 0.120 |
| 26 | 0.001 | 0.007 | 0.021 | 0.040 | 0.058 | 0.074 | 0.088 | 0.099 | 0.107 | 0.113 | 0.118 |
| 27 | 0.001 | 0.007 | 0.021 | 0.038 | 0.056 | 0.072 | 0.086 | 0.096 | 0.105 | 0.111 | 0.115 |
| 28 | 0.001 | 0.006 | 0.020 | 0.037 | 0.055 | 0.070 | 0.084 | 0.094 | 0.102 | 0.108 | 0.112 |
| 29 | 0.001 | 0.006 | 0.019 | 0.036 | 0.053 | 0.069 | 0.082 | 0.092 | 0.100 | 0.106 | 0.110 |
| 20 | 0.001 | 0.006 | 0.018 | 0.035 | 0.052 | 0.067 | 0.080 | 0.090 | 0.098 | 0.103 | 0.107 |

Table C. 37
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 120 /$ Annual Growth Rate $=\mathbf{2 0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.000 | 0.997 | 0.986 | 0.965 | 0.938 | 0.909 | 0.879 | 0.851 | 0.824 | 0.800 | 0.777 |
| 2 | 0.987 | 0.952 | 0.905 | 0.859 | 0.816 | 0.779 | 0.747 | 0.719 | 0.694 | 0.672 | 0.652 |
| 3 | 0.937 | 0.869 | 0.810 | 0.760 | 0.720 | 0.687 | 0.659 | 0.635 | 0.614 | 0.595 | 0.579 |
| 4 | 0.856 | 0.780 | 0.723 | 0.679 | 0.645 | 0.617 | 0.594 | 0.574 | 0.557 | 0.541 | 0.527 |
| 5 | 0.763 | 0.694 | 0.647 | 0.612 | 0.585 | 0.563 | 0.544 | 0.527 | 0.512 | 0.499 | 0.487 |
| 6 | 0.670 | 0.618 | 0.582 | 0.556 | 0.535 | 0.517 | 0.502 | 0.489 | 0.476 | 0.465 | 0.454 |
| 7 | 0.583 | 0.549 | 0.526 | 0.508 | 0.492 | 0.479 | 0.467 | 0.456 | 0.445 | 0.436 | 0.426 |
| 8 | 0.505 | 0.489 | 0.477 | 0.466 | 0.456 | 0.446 | 0.437 | 0.428 | 0.419 | 0.410 | 0.402 |
| 9 | 0.435 | 0.437 | 0.434 | 0.429 | 0.423 | 0.417 | 0.410 | 0.403 | 0.396 | 0.388 | 0.381 |
| 10 | 0.375 | 0.390 | 0.396 | 0.397 | 0.395 | 0.391 | 0.386 | 0.381 | 0.375 | 0.368 | 0.361 |
| 11 | 0.322 | 0.349 | 0.362 | 0.367 | 0.369 | 0.368 | 0.365 | 0.361 | 0.356 | 0.350 | 0.344 |
| 12 | 0.277 | 0.313 | 0.332 | 0.341 | 0.346 | 0.347 | 0.345 | 0.343 | 0.339 | 0.334 | 0.328 |
| 13 | 0.238 | 0.281 | 0.304 | 0.318 | 0.325 | 0.328 | 0.328 | 0.326 | 0.323 | 0.319 | 0.314 |
| 14 | 0.204 | 0.252 | 0.280 | 0.296 | 0.305 | 0.310 | 0.311 | 0.311 | 0.308 | 0.305 | 0.300 |
| 15 | 0.175 | 0.227 | 0.258 | 0.277 | 0.288 | 0.294 | 0.296 | 0.296 | 0.295 | 0.292 | 0.288 |
| 17 | 0.129 | 0.184 | 0.219 | 0.242 | 0.256 | 0.265 | 0.269 | 0.271 | 0.270 | 0.268 | 0.265 |
| 150 | 0.204 | 0.238 | 0.259 | 0.271 | 0.279 | 0.282 | 0.283 | 0.282 | 0.280 | 0.276 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.111 | 0.166 | 0.203 | 0.227 | 0.242 | 0.252 | 0.257 | 0.259 | 0.259 | 0.258 | 0.255 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.095 | 0.150 | 0.188 | 0.213 | 0.229 | 0.240 | 0.246 | 0.249 | 0.249 | 0.248 | 0.245 |
| 20 | 0.082 | 0.135 | 0.174 | 0.200 | 0.217 | 0.228 | 0.235 | 0.238 | 0.239 | 0.238 | 0.236 |
| 21 | 0.070 | 0.122 | 0.161 | 0.188 | 0.206 | 0.218 | 0.225 | 0.229 | 0.230 | 0.230 | 0.228 |
| 22 | 0.060 | 0.111 | 0.149 | 0.177 | 0.195 | 0.208 | 0.215 | 0.220 | 0.221 | 0.221 | 0.219 |
| 23 | 0.052 | 0.100 | 0.139 | 0.166 | 0.186 | 0.198 | 0.206 | 0.211 | 0.213 | 0.213 | 0.212 |
| 24 | 0.045 | 0.091 | 0.129 | 0.157 | 0.176 | 0.189 | 0.198 | 0.203 | 0.205 | 0.205 | 0.204 |
| 25 | 0.039 | 0.082 | 0.120 | 0.148 | 0.168 | 0.181 | 0.190 | 0.195 | 0.198 | 0.198 | 0.197 |
| 26 | 0.033 | 0.075 | 0.111 | 0.139 | 0.159 | 0.173 | 0.182 | 0.188 | 0.191 | 0.191 | 0.190 |
| 27 | 0.029 | 0.068 | 0.104 | 0.131 | 0.152 | 0.166 | 0.175 | 0.181 | 0.184 | 0.185 | 0.184 |
| 28 | 0.025 | 0.062 | 0.096 | 0.124 | 0.144 | 0.159 | 0.168 | 0.174 | 0.177 | 0.178 | 0.178 |
| 29 | 0.021 | 0.056 | 0.090 | 0.117 | 0.137 | 0.152 | 0.162 | 0.168 | 0.171 | 0.172 | 0.172 |
| 30 | 0.018 | 0.051 | 0.084 | 0.111 | 0.131 | 0.146 | 0.156 | 0.162 | 0.165 | 0.167 | 0.166 |

Table C. 38
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 115 /$ Annual Growth Rate $=\mathbf{2 0} \%$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.997 | 0.978 | 0.945 | 0.907 | 0.868 | 0.833 | 0.801 | 0.772 | 0.747 | 0.724 | 0.704 |
| 2 | 0.939 | 0.873 | 0.814 | 0.766 | 0.727 | 0.695 | 0.667 | 0.644 | 0.624 | 0.607 | 0.591 |
| 3 | 0.831 | 0.757 | 0.704 | 0.664 | 0.633 | 0.608 | 0.587 | 0.569 | 0.553 | 0.540 | 0.527 |
| 4 | 0.716 | 0.656 | 0.616 | 0.587 | 0.564 | 0.546 | 0.530 | 0.516 | 0.503 | 0.492 | 0.482 |
| 5 | 0.609 | 0.571 | 0.545 | 0.526 | 0.510 | 0.497 | 0.485 | 0.474 | 0.465 | 0.455 | 0.446 |
| 6 | 0.516 | 0.499 | 0.487 | 0.476 | 0.466 | 0.457 | 0.449 | 0.441 | 0.433 | 0.425 | 0.417 |
| 7 | 0.436 | 0.439 | 0.437 | 0.434 | 0.429 | 0.424 | 0.418 | 0.412 | 0.406 | 0.399 | 0.393 |
| 8 | 0.369 | 0.387 | 0.395 | 0.398 | 0.397 | 0.395 | 0.392 | 0.387 | 0.382 | 0.377 | 0.371 |
| 9 | 0.312 | 0.343 | 0.358 | 0.366 | 0.369 | 0.370 | 0.368 | 0.365 | 0.362 | 0.357 | 0.352 |
| 10 | 0.264 | 0.304 | 0.326 | 0.338 | 0.344 | 0.347 | 0.347 | 0.346 | 0.343 | 0.339 | 0.335 |
| 11 | 0.224 | 0.271 | 0.298 | 0.313 | 0.322 | 0.327 | 0.328 | 0.328 | 0.326 | 0.323 | 0.319 |
| 12 | 0.190 | 0.242 | 0.272 | 0.291 | 0.302 | 0.308 | 0.311 | 0.312 | 0.311 | 0.308 | 0.305 |
| 13 | 0.162 | 0.216 | 0.250 | 0.271 | 0.284 | 0.292 | 0.296 | 0.297 | 0.297 | 0.295 | 0.292 |
| 14 | 0.138 | 0.193 | 0.229 | 0.252 | 0.267 | 0.276 | 0.281 | 0.283 | 0.284 | 0.282 | 0.280 |
| 15 | 0.117 | 0.174 | 0.211 | 0.236 | 0.252 | 0.262 | 0.268 | 0.271 | 0.271 | 0.270 | 0.268 |
| 16 | 0.100 | 0.156 | 0.195 | 0.221 | 0.238 | 0.249 | 0.255 | 0.259 | 0.260 | 0.259 | 0.258 |
| 17 | 0.085 | 0.140 | 0.180 | 0.206 | 0.225 | 0.236 | 0.244 | 0.248 | 0.249 | 0.249 | 0.248 |


| 18 | 0.073 | 0.126 | 0.166 | 0.194 | 0.212 | 0.225 | 0.233 | 0.237 | 0.239 | 0.239 | 0.238 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.062 | 0.114 | 0.153 | 0.182 | 0.201 | 0.214 | 0.223 | 0.228 | 0.230 | 0.230 | 0.229 |
| 20 | 0.053 | 0.103 | 0.142 | 0.171 | 0.191 | 0.204 | 0.213 | 0.218 | 0.221 | 0.222 | 0.221 |
| 21 | 0.046 | 0.093 | 0.132 | 0.160 | 0.181 | 0.195 | 0.204 | 0.210 | 0.213 | 0.214 | 0.213 |
| 22 | 0.039 | 0.084 | 0.122 | 0.151 | 0.172 | 0.186 | 0.196 | 0.202 | 0.205 | 0.206 | 0.205 |
| 23 | 0.034 | 0.076 | 0.113 | 0.142 | 0.163 | 0.178 | 0.188 | 0.194 | 0.197 | 0.198 | 0.198 |
| 24 | 0.029 | 0.069 | 0.105 | 0.134 | 0.155 | 0.170 | 0.180 | 0.186 | 0.190 | 0.191 | 0.191 |
| 25 | 0.025 | 0.062 | 0.098 | 0.126 | 0.147 | 0.162 | 0.173 | 0.179 | 0.183 | 0.185 | 0.185 |
| 26 | 0.021 | 0.056 | 0.091 | 0.119 | 0.140 | 0.155 | 0.166 | 0.173 | 0.177 | 0.178 | 0.178 |
| 27 | 0.018 | 0.051 | 0.085 | 0.112 | 0.133 | 0.149 | 0.159 | 0.166 | 0.170 | 0.172 | 0.173 |
| 28 | 0.016 | 0.046 | 0.079 | 0.106 | 0.127 | 0.142 | 0.153 | 0.160 | 0.165 | 0.167 | 0.167 |
| 29 | 0.014 | 0.042 | 0.073 | 0.100 | 0.121 | 0.136 | 0.147 | 0.155 | 0.159 | 0.161 | 0.161 |
| 20 | 0.012 | 0.038 | 0.068 | 0.095 | 0.115 | 0.131 | 0.142 | 0.149 | 0.153 | 0.156 | 0.156 |

Table C. 39
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 110 /$ Annual Growth Rate $=\mathbf{2 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.953 | 0.894 | 0.838 | 0.790 | 0.751 | 0.719 | 0.692 | 0.669 | 0.650 | 0.633 | 0.617 |
| 2 | 0.793 | 0.724 | 0.677 | 0.642 | 0.615 | 0.594 | 0.576 | 0.561 | 0.547 | 0.536 | 0.525 |
| 3 | 0.643 | 0.600 | 0.571 | 0.551 | 0.534 | 0.521 | 0.509 | 0.498 | 0.489 | 0.480 | 0.472 |
| 4 | 0.523 | 0.507 | 0.495 | 0.485 | 0.477 | 0.469 | 0.461 | 0.454 | 0.448 | 0.441 | 0.435 |
| 5 | 0.427 | 0.434 | 0.436 | 0.435 | 0.432 | 0.429 | 0.425 | 0.420 | 0.415 | 0.410 | 0.405 |
| 6 | 0.352 | 0.376 | 0.388 | 0.394 | 0.396 | 0.396 | 0.394 | 0.392 | 0.388 | 0.384 | 0.380 |
| 7 | 0.291 | 0.328 | 0.348 | 0.359 | 0.365 | 0.368 | 0.369 | 0.367 | 0.365 | 0.362 | 0.359 |
| 8 | 0.243 | 0.288 | 0.314 | 0.330 | 0.339 | 0.344 | 0.346 | 0.346 | 0.345 | 0.343 | 0.340 |
| 9 | 0.203 | 0.254 | 0.285 | 0.304 | 0.315 | 0.322 | 0.326 | 0.328 | 0.327 | 0.326 | 0.323 |
| 10 | 0.170 | 0.225 | 0.259 | 0.281 | 0.295 | 0.303 | 0.308 | 0.311 | 0.311 | 0.310 | 0.308 |
| 11 | 0.143 | 0.200 | 0.237 | 0.261 | 0.276 | 0.286 | 0.292 | 0.295 | 0.296 | 0.296 | 0.294 |
| 12 | 0.120 | 0.178 | 0.217 | 0.242 | 0.259 | 0.270 | 0.277 | 0.281 | 0.283 | 0.283 | 0.282 |
| 13 | 0.102 | 0.159 | 0.199 | 0.226 | 0.244 | 0.256 | 0.264 | 0.268 | 0.270 | 0.271 | 0.270 |
| 14 | 0.086 | 0.142 | 0.183 | 0.211 | 0.230 | 0.243 | 0.251 | 0.256 | 0.259 | 0.259 | 0.259 |
| 15 | 0.073 | 0.127 | 0.168 | 0.197 | 0.217 | 0.231 | 0.239 | 0.245 | 0.248 | 0.249 | 0.248 |
| 16 | 0.062 | 0.114 | 0.155 | 0.184 | 0.205 | 0.219 | 0.229 | 0.235 | 0.238 | 0.239 | 0.239 |
| 17 | 0.053 | 0.103 | 0.143 | 0.173 | 0.194 | 0.209 | 0.218 | 0.225 | 0.228 | 0.230 | 0.230 |


| 18 | 0.045 | 0.092 | 0.132 | 0.162 | 0.184 | 0.199 | 0.209 | 0.216 | 0.219 | 0.221 | 0.221 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.038 | 0.083 | 0.122 | 0.152 | 0.174 | 0.189 | 0.200 | 0.207 | 0.211 | 0.213 | 0.213 |
| 20 | 0.033 | 0.075 | 0.113 | 0.143 | 0.165 | 0.181 | 0.192 | 0.199 | 0.203 | 0.205 | 0.205 |
| 21 | 0.028 | 0.068 | 0.105 | 0.135 | 0.157 | 0.172 | 0.184 | 0.191 | 0.195 | 0.198 | 0.198 |
| 22 | 0.024 | 0.061 | 0.098 | 0.127 | 0.149 | 0.165 | 0.176 | 0.184 | 0.188 | 0.191 | 0.191 |
| 23 | 0.020 | 0.055 | 0.091 | 0.119 | 0.141 | 0.158 | 0.169 | 0.177 | 0.181 | 0.184 | 0.185 |
| 24 | 0.018 | 0.050 | 0.084 | 0.113 | 0.134 | 0.151 | 0.162 | 0.170 | 0.175 | 0.178 | 0.178 |
| 25 | 0.015 | 0.045 | 0.078 | 0.106 | 0.128 | 0.144 | 0.156 | 0.164 | 0.169 | 0.171 | 0.172 |
| 26 | 0.013 | 0.041 | 0.073 | 0.100 | 0.122 | 0.138 | 0.150 | 0.158 | 0.163 | 0.166 | 0.167 |
| 27 | 0.011 | 0.037 | 0.068 | 0.095 | 0.116 | 0.132 | 0.144 | 0.152 | 0.157 | 0.160 | 0.161 |
| 28 | 0.009 | 0.034 | 0.063 | 0.089 | 0.111 | 0.127 | 0.138 | 0.147 | 0.152 | 0.155 | 0.156 |
| 29 | 0.008 | 0.031 | 0.059 | 0.084 | 0.105 | 0.121 | 0.133 | 0.141 | 0.147 | 0.150 | 0.151 |
| 20 | 0.007 | 0.028 | 0.055 | 0.080 | 0.100 | 0.116 | 0.128 | 0.136 | 0.142 | 0.145 | 0.146 |

Table C. 40
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\$ 100 /$ Strike Price $=\$ 105 /$ Annual Growth Rate $=\mathbf{2 0 \%}$
Volatility

| Mo | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.65 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.727 | 0.670 | 0.633 | 0.606 | 0.586 | 0.570 | 0.557 | 0.546 | 0.536 | 0.528 | 0.520 |
| 2 | 0.523 | 0.510 | 0.501 | 0.493 | 0.487 | 0.481 | 0.475 | 0.470 | 0.465 | 0.460 | 0.455 |
| 3 | 0.400 | 0.416 | 0.424 | 0.427 | 0.429 | 0.428 | 0.427 | 0.425 | 0.422 | 0.419 | 0.416 |
| 4 | 0.315 | 0.350 | 0.369 | 0.380 | 0.386 | 0.390 | 0.391 | 0.391 | 0.390 | 0.389 | 0.386 |
| 5 | 0.254 | 0.300 | 0.326 | 0.343 | 0.353 | 0.360 | 0.363 | 0.365 | 0.365 | 0.364 | 0.363 |
| 6 | 0.206 | 0.259 | 0.292 | 0.312 | 0.326 | 0.334 | 0.339 | 0.342 | 0.343 | 0.343 | 0.342 |
| 7 | 0.170 | 0.227 | 0.263 | 0.287 | 0.302 | 0.312 | 0.319 | 0.323 | 0.325 | 0.325 | 0.324 |
| 8 | 0.140 | 0.199 | 0.238 | 0.264 | 0.281 | 0.293 | 0.301 | 0.305 | 0.308 | 0.309 | 0.309 |
| 9 | 0.117 | 0.176 | 0.217 | 0.244 | 0.263 | 0.276 | 0.284 | 0.290 | 0.293 | 0.294 | 0.294 |
| 10 | 0.098 | 0.156 | 0.198 | 0.227 | 0.247 | 0.260 | 0.270 | 0.276 | 0.279 | 0.281 | 0.281 |
| 11 | 0.082 | 0.139 | 0.181 | 0.211 | 0.232 | 0.246 | 0.256 | 0.263 | 0.267 | 0.269 | 0.269 |
| 12 | 0.069 | 0.124 | 0.166 | 0.197 | 0.218 | 0.233 | 0.244 | 0.251 | 0.255 | 0.257 | 0.258 |
| 13 | 0.058 | 0.111 | 0.153 | 0.184 | 0.206 | 0.221 | 0.232 | 0.240 | 0.244 | 0.247 | 0.247 |
| 14 | 0.049 | 0.099 | 0.141 | 0.172 | 0.194 | 0.210 | 0.222 | 0.229 | 0.234 | 0.237 | 0.238 |
| 15 | 0.042 | 0.089 | 0.130 | 0.161 | 0.184 | 0.200 | 0.212 | 0.220 | 0.225 | 0.227 | 0.229 |
| 16 | 0.035 | 0.080 | 0.120 | 0.151 | 0.174 | 0.191 | 0.202 | 0.211 | 0.216 | 0.219 | 0.220 |
| 17 | 0.030 | 0.072 | 0.111 | 0.142 | 0.165 | 0.182 | 0.194 | 0.202 | 0.207 | 0.211 | 0.212 |


| 18 | 0.026 | 0.065 | 0.102 | 0.133 | 0.156 | 0.173 | 0.185 | 0.194 | 0.200 | 0.203 | 0.204 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.022 | 0.058 | 0.095 | 0.125 | 0.148 | 0.165 | 0.178 | 0.186 | 0.192 | 0.195 | 0.197 |
| 20 | 0.019 | 0.053 | 0.088 | 0.118 | 0.141 | 0.158 | 0.170 | 0.179 | 0.185 | 0.188 | 0.190 |
| 21 | 0.016 | 0.048 | 0.082 | 0.111 | 0.134 | 0.151 | 0.164 | 0.172 | 0.178 | 0.182 | 0.183 |
| 22 | 0.014 | 0.043 | 0.076 | 0.104 | 0.127 | 0.144 | 0.157 | 0.166 | 0.172 | 0.175 | 0.177 |
| 23 | 0.012 | 0.039 | 0.071 | 0.099 | 0.121 | 0.138 | 0.151 | 0.160 | 0.166 | 0.169 | 0.171 |
| 24 | 0.010 | 0.035 | 0.066 | 0.093 | 0.115 | 0.132 | 0.145 | 0.154 | 0.160 | 0.164 | 0.165 |
| 25 | 0.009 | 0.032 | 0.061 | 0.088 | 0.110 | 0.127 | 0.139 | 0.148 | 0.154 | 0.158 | 0.160 |
| 26 | 0.007 | 0.029 | 0.057 | 0.083 | 0.104 | 0.121 | 0.134 | 0.143 | 0.149 | 0.153 | 0.155 |
| 27 | 0.006 | 0.026 | 0.053 | 0.078 | 0.100 | 0.116 | 0.129 | 0.138 | 0.144 | 0.148 | 0.150 |
| 28 | 0.005 | 0.024 | 0.049 | 0.074 | 0.095 | 0.111 | 0.124 | 0.133 | 0.139 | 0.143 | 0.145 |
| 29 | 0.005 | 0.022 | 0.046 | 0.070 | 0.091 | 0.107 | 0.119 | 0.128 | 0.134 | 0.138 | 0.140 |
| 30 | 0.004 | 0.020 | 0.043 | 0.066 | 0.086 | 0.103 | 0.115 | 0.124 | 0.130 | 0.134 | 0.136 |

Table C. 41
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 100 /$ Annual Growth Rate $=\mathbf{2 0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.301 | 0.343 | 0.368 | 0.385 | 0.396 | 0.403 | 0.408 | 0.412 | 0.415 | 0.416 | 0.417 |
| 2 | 0.230 | 0.284 | 0.317 | 0.339 | 0.354 | 0.364 | 0.372 | 0.377 | 0.380 | 0.382 | 0.384 |
| 3 | 0.183 | 0.242 | 0.280 | 0.306 | 0.323 | 0.335 | 0.344 | 0.350 | 0.354 | 0.357 | 0.358 |
| 4 | 0.148 | 0.209 | 0.251 | 0.279 | 0.298 | 0.312 | 0.322 | 0.328 | 0.333 | 0.336 | 0.338 |
| 5 | 0.122 | 0.183 | 0.226 | 0.256 | 0.277 | 0.292 | 0.302 | 0.310 | 0.315 | 0.318 | 0.320 |
| 6 | 0.100 | 0.161 | 0.205 | 0.236 | 0.258 | 0.274 | 0.285 | 0.293 | 0.299 | 0.302 | 0.304 |
| 7 | 0.084 | 0.142 | 0.187 | 0.219 | 0.242 | 0.258 | 0.270 | 0.278 | 0.284 | 0.288 | 0.290 |
| 8 | 0.070 | 0.126 | 0.171 | 0.203 | 0.227 | 0.244 | 0.256 | 0.265 | 0.271 | 0.275 | 0.277 |
| 9 | 0.059 | 0.113 | 0.156 | 0.189 | 0.213 | 0.231 | 0.243 | 0.252 | 0.259 | 0.263 | 0.265 |
| 10 | 0.049 | 0.101 | 0.144 | 0.177 | 0.201 | 0.219 | 0.232 | 0.241 | 0.247 | 0.252 | 0.254 |
| 11 | 0.042 | 0.090 | 0.132 | 0.165 | 0.190 | 0.208 | 0.221 | 0.231 | 0.237 | 0.241 | 0.244 |
| 12 | 0.035 | 0.081 | 0.122 | 0.155 | 0.179 | 0.198 | 0.211 | 0.221 | 0.227 | 0.232 | 0.234 |
| 13 | 0.030 | 0.073 | 0.113 | 0.145 | 0.170 | 0.188 | 0.202 | 0.211 | 0.218 | 0.223 | 0.225 |
| 14 | 0.025 | 0.065 | 0.104 | 0.136 | 0.161 | 0.179 | 0.193 | 0.203 | 0.210 | 0.214 | 0.217 |
| 15 | 0.022 | 0.059 | 0.096 | 0.128 | 0.152 | 0.171 | 0.185 | 0.195 | 0.202 | 0.206 | 0.209 |
| 17 | 0.016 | 0.048 | 0.083 | 0.113 | 0.137 | 0.156 | 0.170 | 0.180 | 0.187 | 0.191 | 0.194 |
| 18 | 0.053 | 0.089 | 0.120 | 0.145 | 0.163 | 0.177 | 0.187 | 0.194 | 0.199 | 0.201 |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.013 | 0.043 | 0.077 | 0.107 | 0.130 | 0.149 | 0.163 | 0.173 | 0.180 | 0.185 | 0.187 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.011 | 0.039 | 0.071 | 0.100 | 0.124 | 0.142 | 0.156 | 0.166 | 0.173 | 0.178 | 0.181 |
| 20 | 0.010 | 0.035 | 0.066 | 0.095 | 0.118 | 0.136 | 0.150 | 0.160 | 0.167 | 0.172 | 0.175 |
| 21 | 0.008 | 0.032 | 0.062 | 0.089 | 0.112 | 0.130 | 0.144 | 0.154 | 0.161 | 0.166 | 0.169 |
| 22 | 0.007 | 0.029 | 0.057 | 0.084 | 0.107 | 0.125 | 0.139 | 0.149 | 0.156 | 0.160 | 0.163 |
| 23 | 0.006 | 0.026 | 0.053 | 0.080 | 0.102 | 0.120 | 0.133 | 0.143 | 0.150 | 0.155 | 0.158 |
| 24 | 0.005 | 0.024 | 0.050 | 0.075 | 0.097 | 0.115 | 0.128 | 0.138 | 0.145 | 0.150 | 0.153 |
| 25 | 0.005 | 0.022 | 0.046 | 0.071 | 0.093 | 0.110 | 0.123 | 0.133 | 0.140 | 0.145 | 0.148 |
| 26 | 0.004 | 0.020 | 0.043 | 0.067 | 0.088 | 0.105 | 0.119 | 0.129 | 0.136 | 0.140 | 0.143 |
| 27 | 0.003 | 0.018 | 0.040 | 0.064 | 0.084 | 0.101 | 0.114 | 0.124 | 0.131 | 0.136 | 0.138 |
| 28 | 0.003 | 0.016 | 0.038 | 0.060 | 0.080 | 0.097 | 0.110 | 0.120 | 0.127 | 0.131 | 0.134 |
| 29 | 0.002 | 0.015 | 0.035 | 0.057 | 0.077 | 0.093 | 0.106 | 0.116 | 0.123 | 0.127 | 0.130 |
| 20 | 0.002 | 0.013 | 0.033 | 0.054 | 0.073 | 0.089 | 0.102 | 0.112 | 0.119 | 0.123 | 0.126 |

Table C. 42
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 9 5} /$ Annual Growth Rate $=\mathbf{2 0 \%}$

Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.044 | 0.098 | 0.148 | 0.188 | 0.220 | 0.245 | 0.265 | 0.282 | 0.295 | 0.306 | 0.315 |
| 2 | 0.058 | 0.115 | 0.164 | 0.202 | 0.232 | 0.254 | 0.272 | 0.286 | 0.297 | 0.305 | 0.312 |
| 3 | 0.056 | 0.113 | 0.160 | 0.198 | 0.226 | 0.248 | 0.265 | 0.278 | 0.288 | 0.295 | 0.301 |
| 4 | 0.051 | 0.105 | 0.152 | 0.189 | 0.217 | 0.238 | 0.254 | 0.267 | 0.277 | 0.284 | 0.289 |
| 5 | 0.045 | 0.097 | 0.142 | 0.178 | 0.206 | 0.227 | 0.244 | 0.256 | 0.265 | 0.272 | 0.278 |
| 6 | 0.039 | 0.088 | 0.133 | 0.168 | 0.196 | 0.217 | 0.233 | 0.245 | 0.254 | 0.261 | 0.266 |
| 7 | 0.034 | 0.080 | 0.123 | 0.159 | 0.186 | 0.207 | 0.223 | 0.235 | 0.244 | 0.251 | 0.256 |
| 8 | 0.029 | 0.073 | 0.115 | 0.149 | 0.176 | 0.197 | 0.213 | 0.225 | 0.234 | 0.241 | 0.246 |
| 9 | 0.025 | 0.066 | 0.106 | 0.141 | 0.167 | 0.188 | 0.204 | 0.216 | 0.225 | 0.232 | 0.236 |
| 10 | 0.021 | 0.059 | 0.099 | 0.132 | 0.159 | 0.180 | 0.196 | 0.207 | 0.216 | 0.223 | 0.227 |
| 11 | 0.018 | 0.054 | 0.092 | 0.125 | 0.151 | 0.172 | 0.187 | 0.199 | 0.208 | 0.214 | 0.219 |
| 12 | 0.016 | 0.049 | 0.085 | 0.117 | 0.144 | 0.164 | 0.180 | 0.191 | 0.200 | 0.206 | 0.211 |
| 13 | 0.014 | 0.044 | 0.079 | 0.111 | 0.136 | 0.157 | 0.172 | 0.184 | 0.193 | 0.199 | 0.203 |
| 14 | 0.012 | 0.040 | 0.074 | 0.104 | 0.130 | 0.150 | 0.165 | 0.177 | 0.186 | 0.192 | 0.196 |
| 15 | 0.010 | 0.036 | 0.069 | 0.099 | 0.124 | 0.143 | 0.159 | 0.170 | 0.179 | 0.185 | 0.189 |
| 17 | 0.007 | 0.030 | 0.059 | 0.088 | 0.112 | 0.131 | 0.147 | 0.158 | 0.166 | 0.172 | 0.176 |
| 109 | 0.033 | 0.064 | 0.093 | 0.118 | 0.137 | 0.153 | 0.164 | 0.173 | 0.179 | 0.183 |  |


| 18 | 0.006 | 0.027 | 0.055 | 0.083 | 0.107 | 0.126 | 0.141 | 0.152 | 0.161 | 0.167 | 0.170 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.005 | 0.025 | 0.052 | 0.079 | 0.102 | 0.121 | 0.135 | 0.147 | 0.155 | 0.161 | 0.165 |
| 20 | 0.005 | 0.022 | 0.048 | 0.074 | 0.097 | 0.116 | 0.130 | 0.142 | 0.150 | 0.156 | 0.159 |
| 21 | 0.004 | 0.020 | 0.045 | 0.070 | 0.093 | 0.111 | 0.125 | 0.136 | 0.145 | 0.150 | 0.154 |
| 22 | 0.003 | 0.019 | 0.042 | 0.066 | 0.088 | 0.106 | 0.121 | 0.132 | 0.140 | 0.145 | 0.149 |
| 23 | 0.003 | 0.017 | 0.039 | 0.063 | 0.084 | 0.102 | 0.116 | 0.127 | 0.135 | 0.141 | 0.144 |
| 24 | 0.003 | 0.015 | 0.037 | 0.060 | 0.080 | 0.098 | 0.112 | 0.123 | 0.131 | 0.136 | 0.140 |
| 25 | 0.002 | 0.014 | 0.034 | 0.056 | 0.077 | 0.094 | 0.108 | 0.118 | 0.126 | 0.132 | 0.135 |
| 26 | 0.002 | 0.013 | 0.032 | 0.053 | 0.073 | 0.090 | 0.104 | 0.114 | 0.122 | 0.128 | 0.131 |
| 27 | 0.002 | 0.012 | 0.030 | 0.051 | 0.070 | 0.087 | 0.100 | 0.111 | 0.118 | 0.124 | 0.127 |
| 28 | 0.001 | 0.011 | 0.028 | 0.048 | 0.067 | 0.083 | 0.097 | 0.107 | 0.114 | 0.120 | 0.123 |
| 29 | 0.001 | 0.010 | 0.026 | 0.045 | 0.064 | 0.080 | 0.093 | 0.103 | 0.111 | 0.116 | 0.119 |
| 30 | 0.001 | 0.009 | 0.024 | 0.043 | 0.061 | 0.077 | 0.090 | 0.100 | 0.107 | 0.112 | 0.116 |

Table C. 43
Probability of a Put Expiring in the Money as a Function of Time and Volatility
Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\$ 90 /$ Annual Growth Rate $=\mathbf{2 0 \%}$
Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.002 | 0.013 | 0.036 | 0.066 | 0.095 | 0.123 | 0.149 | 0.170 | 0.190 | 0.206 | 0.220 |
| 2 | 0.007 | 0.031 | 0.066 | 0.101 | 0.133 | 0.161 | 0.184 | 0.203 | 0.219 | 0.233 | 0.244 |
| 3 | 0.010 | 0.040 | 0.077 | 0.113 | 0.144 | 0.171 | 0.192 | 0.210 | 0.225 | 0.236 | 0.246 |
| 4 | 0.012 | 0.043 | 0.080 | 0.116 | 0.147 | 0.172 | 0.192 | 0.209 | 0.223 | 0.233 | 0.242 |
| 5 | 0.012 | 0.043 | 0.080 | 0.115 | 0.145 | 0.169 | 0.189 | 0.205 | 0.218 | 0.228 | 0.236 |
| 6 | 0.012 | 0.041 | 0.078 | 0.112 | 0.141 | 0.165 | 0.184 | 0.200 | 0.212 | 0.222 | 0.229 |
| 7 | 0.011 | 0.039 | 0.075 | 0.108 | 0.137 | 0.160 | 0.179 | 0.194 | 0.206 | 0.215 | 0.222 |
| 8 | 0.010 | 0.037 | 0.071 | 0.104 | 0.132 | 0.155 | 0.173 | 0.188 | 0.199 | 0.208 | 0.215 |
| 9 | 0.009 | 0.034 | 0.067 | 0.099 | 0.127 | 0.149 | 0.167 | 0.181 | 0.192 | 0.201 | 0.208 |
| 10 | 0.008 | 0.032 | 0.064 | 0.095 | 0.121 | 0.144 | 0.161 | 0.175 | 0.186 | 0.194 | 0.201 |
| 11 | 0.007 | 0.029 | 0.060 | 0.090 | 0.116 | 0.138 | 0.155 | 0.169 | 0.180 | 0.188 | 0.194 |
| 12 | 0.006 | 0.027 | 0.056 | 0.086 | 0.111 | 0.133 | 0.150 | 0.163 | 0.174 | 0.182 | 0.188 |
| 13 | 0.005 | 0.025 | 0.053 | 0.081 | 0.107 | 0.128 | 0.144 | 0.158 | 0.168 | 0.176 | 0.181 |
| 14 | 0.005 | 0.023 | 0.050 | 0.077 | 0.102 | 0.123 | 0.139 | 0.152 | 0.162 | 0.170 | 0.175 |
| 15 | 0.004 | 0.021 | 0.047 | 0.073 | 0.098 | 0.118 | 0.134 | 0.147 | 0.157 | 0.164 | 0.170 |
| 16 | 0.004 | 0.019 | 0.044 | 0.070 | 0.093 | 0.113 | 0.129 | 0.142 | 0.152 | 0.159 | 0.164 |
| 17 | 0.003 | 0.017 | 0.041 | 0.066 | 0.089 | 0.109 | 0.125 | 0.137 | 0.147 | 0.154 | 0.159 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.003 | 0.016 | 0.038 | 0.063 | 0.085 | 0.105 | 0.120 | 0.132 | 0.142 | 0.149 | 0.154 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.002 | 0.015 | 0.036 | 0.060 | 0.082 | 0.100 | 0.116 | 0.128 | 0.137 | 0.144 | 0.149 |
| 20 | 0.002 | 0.013 | 0.034 | 0.057 | 0.078 | 0.097 | 0.112 | 0.124 | 0.133 | 0.139 | 0.144 |
| 21 | 0.002 | 0.012 | 0.031 | 0.054 | 0.075 | 0.093 | 0.108 | 0.119 | 0.128 | 0.135 | 0.140 |
| 22 | 0.002 | 0.011 | 0.029 | 0.051 | 0.071 | 0.089 | 0.104 | 0.115 | 0.124 | 0.131 | 0.135 |
| 23 | 0.001 | 0.010 | 0.028 | 0.048 | 0.068 | 0.086 | 0.100 | 0.112 | 0.120 | 0.127 | 0.131 |
| 24 | 0.001 | 0.009 | 0.026 | 0.046 | 0.065 | 0.083 | 0.097 | 0.108 | 0.116 | 0.123 | 0.127 |
| 25 | 0.001 | 0.009 | 0.024 | 0.044 | 0.063 | 0.079 | 0.093 | 0.104 | 0.113 | 0.119 | 0.123 |
| 26 | 0.001 | 0.008 | 0.023 | 0.041 | 0.060 | 0.076 | 0.090 | 0.101 | 0.109 | 0.115 | 0.120 |
| 27 | 0.001 | 0.007 | 0.021 | 0.039 | 0.057 | 0.073 | 0.087 | 0.098 | 0.106 | 0.112 | 0.116 |
| 28 | 0.001 | 0.007 | 0.020 | 0.037 | 0.055 | 0.071 | 0.084 | 0.094 | 0.102 | 0.108 | 0.112 |
| 29 | 0.001 | 0.006 | 0.019 | 0.035 | 0.053 | 0.068 | 0.081 | 0.091 | 0.099 | 0.105 | 0.109 |
| 20 | 0.000 | 0.005 | 0.018 | 0.034 | 0.050 | 0.065 | 0.078 | 0.088 | 0.096 | 0.102 | 0.106 |

Table C. 44
Probability of a Put Expiring in the Money as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 8 5} /$ Annual Growth Rate $=\mathbf{2 0 \%}$

## Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.001 | 0.005 | 0.015 | 0.031 | 0.049 | 0.069 | 0.089 | 0.108 | 0.125 | 0.141 |
| 2 | 0.000 | 0.005 | 0.019 | 0.041 | 0.065 | 0.090 | 0.113 | 0.133 | 0.152 | 0.168 | 0.182 |
| 3 | 0.001 | 0.010 | 0.030 | 0.056 | 0.083 | 0.108 | 0.131 | 0.150 | 0.167 | 0.182 | 0.194 |
| 4 | 0.002 | 0.013 | 0.036 | 0.064 | 0.091 | 0.116 | 0.138 | 0.157 | 0.173 | 0.186 | 0.197 |
| 5 | 0.002 | 0.015 | 0.039 | 0.067 | 0.095 | 0.119 | 0.141 | 0.159 | 0.173 | 0.186 | 0.196 |
| 6 | 0.002 | 0.016 | 0.041 | 0.069 | 0.096 | 0.120 | 0.140 | 0.158 | 0.172 | 0.184 | 0.193 |
| 7 | 0.003 | 0.016 | 0.041 | 0.069 | 0.095 | 0.119 | 0.139 | 0.155 | 0.169 | 0.180 | 0.189 |
| 8 | 0.003 | 0.016 | 0.040 | 0.068 | 0.094 | 0.117 | 0.136 | 0.152 | 0.165 | 0.176 | 0.185 |
| 9 | 0.002 | 0.016 | 0.039 | 0.066 | 0.092 | 0.114 | 0.133 | 0.149 | 0.161 | 0.172 | 0.180 |
| 10 | 0.002 | 0.015 | 0.038 | 0.064 | 0.089 | 0.111 | 0.130 | 0.145 | 0.157 | 0.167 | 0.175 |
| 11 | 0.002 | 0.014 | 0.036 | 0.062 | 0.086 | 0.108 | 0.126 | 0.141 | 0.153 | 0.162 | 0.170 |
| 12 | 0.002 | 0.013 | 0.035 | 0.060 | 0.083 | 0.104 | 0.122 | 0.137 | 0.148 | 0.158 | 0.165 |
| 13 | 0.002 | 0.013 | 0.033 | 0.057 | 0.081 | 0.101 | 0.118 | 0.133 | 0.144 | 0.153 | 0.160 |
| 14 | 0.002 | 0.012 | 0.031 | 0.055 | 0.078 | 0.098 | 0.115 | 0.129 | 0.140 | 0.148 | 0.155 |
| 15 | 0.001 | 0.011 | 0.030 | 0.052 | 0.075 | 0.094 | 0.111 | 0.125 | 0.136 | 0.144 | 0.151 |
| 17 | 0.001 | 0.010 | 0.028 | 0.050 | 0.072 | 0.091 | 0.108 | 0.121 | 0.131 | 0.140 | 0.146 |
| 17 | 0.001 | 0.009 | 0.027 | 0.048 | 0.069 | 0.088 | 0.104 | 0.117 | 0.128 | 0.136 | 0.142 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.001 | 0.009 | 0.025 | 0.046 | 0.066 | 0.085 | 0.101 | 0.113 | 0.124 | 0.131 | 0.137 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.001 | 0.008 | 0.024 | 0.044 | 0.064 | 0.082 | 0.097 | 0.110 | 0.120 | 0.128 | 0.133 |
| 20 | 0.001 | 0.007 | 0.022 | 0.042 | 0.061 | 0.079 | 0.094 | 0.106 | 0.116 | 0.124 | 0.129 |
| 21 | 0.001 | 0.007 | 0.021 | 0.040 | 0.059 | 0.076 | 0.091 | 0.103 | 0.113 | 0.120 | 0.125 |
| 22 | 0.001 | 0.006 | 0.020 | 0.038 | 0.056 | 0.073 | 0.088 | 0.100 | 0.109 | 0.116 | 0.122 |
| 23 | 0.001 | 0.006 | 0.019 | 0.036 | 0.054 | 0.071 | 0.085 | 0.097 | 0.106 | 0.113 | 0.118 |
| 24 | 0.000 | 0.005 | 0.018 | 0.034 | 0.052 | 0.068 | 0.082 | 0.094 | 0.103 | 0.110 | 0.115 |
| 25 | 0.000 | 0.005 | 0.017 | 0.033 | 0.050 | 0.066 | 0.079 | 0.091 | 0.100 | 0.106 | 0.111 |
| 26 | 0.000 | 0.004 | 0.016 | 0.031 | 0.048 | 0.063 | 0.077 | 0.088 | 0.097 | 0.103 | 0.108 |
| 27 | 0.000 | 0.004 | 0.015 | 0.030 | 0.046 | 0.061 | 0.074 | 0.085 | 0.094 | 0.100 | 0.105 |
| 28 | 0.000 | 0.004 | 0.014 | 0.028 | 0.044 | 0.059 | 0.072 | 0.082 | 0.091 | 0.097 | 0.102 |
| 29 | 0.000 | 0.003 | 0.013 | 0.027 | 0.042 | 0.057 | 0.069 | 0.080 | 0.088 | 0.094 | 0.099 |
| 30 | 0.000 | 0.003 | 0.012 | 0.026 | 0.041 | 0.055 | 0.067 | 0.077 | 0.085 | 0.092 | 0.096 |

Table C. 45
Probability of a Put Expiring in the Money as a Function of Time and Volatility

## Stock Price $=\mathbf{\$ 1 0 0} /$ Strike Price $=\mathbf{\$ 8 0} /$ Annual Growth Rate $=\mathbf{2 0 \%}$

## Volatility

| Mo | $\mathbf{0 . 1 5}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 3 0}$ | $\mathbf{0 . 3 5}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 4 5}$ | $\mathbf{0 . 5 0}$ | $\mathbf{0 . 5 5}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 6 5}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.000 | 0.000 | 0.000 | 0.002 | 0.007 | 0.015 | 0.026 | 0.039 | 0.052 | 0.067 | 0.081 |
| 2 | 0.000 | 0.000 | 0.004 | 0.013 | 0.026 | 0.043 | 0.061 | 0.080 | 0.097 | 0.113 | 0.128 |
| 3 | 0.000 | 0.002 | 0.009 | 0.023 | 0.041 | 0.062 | 0.082 | 0.101 | 0.118 | 0.133 | 0.147 |
| 4 | 0.000 | 0.003 | 0.013 | 0.030 | 0.051 | 0.073 | 0.093 | 0.112 | 0.128 | 0.143 | 0.155 |
| 5 | 0.000 | 0.004 | 0.016 | 0.035 | 0.057 | 0.079 | 0.099 | 0.117 | 0.133 | 0.147 | 0.159 |
| 6 | 0.000 | 0.005 | 0.018 | 0.038 | 0.060 | 0.082 | 0.102 | 0.120 | 0.135 | 0.148 | 0.159 |
| 7 | 0.000 | 0.006 | 0.020 | 0.040 | 0.062 | 0.084 | 0.103 | 0.121 | 0.135 | 0.148 | 0.158 |
| 8 | 0.000 | 0.006 | 0.020 | 0.041 | 0.063 | 0.084 | 0.103 | 0.120 | 0.134 | 0.146 | 0.156 |
| 9 | 0.001 | 0.006 | 0.021 | 0.041 | 0.063 | 0.084 | 0.102 | 0.119 | 0.132 | 0.144 | 0.153 |
| 10 | 0.001 | 0.006 | 0.021 | 0.041 | 0.062 | 0.083 | 0.101 | 0.117 | 0.130 | 0.141 | 0.150 |
| 11 | 0.001 | 0.006 | 0.020 | 0.040 | 0.061 | 0.081 | 0.099 | 0.114 | 0.127 | 0.138 | 0.146 |
| 12 | 0.000 | 0.006 | 0.020 | 0.039 | 0.060 | 0.080 | 0.097 | 0.112 | 0.124 | 0.135 | 0.143 |
| 13 | 0.000 | 0.006 | 0.019 | 0.038 | 0.058 | 0.078 | 0.095 | 0.109 | 0.121 | 0.131 | 0.139 |
| 14 | 0.000 | 0.005 | 0.019 | 0.037 | 0.057 | 0.076 | 0.092 | 0.107 | 0.118 | 0.128 | 0.135 |
| 15 | 0.000 | 0.005 | 0.018 | 0.036 | 0.055 | 0.074 | 0.090 | 0.104 | 0.115 | 0.125 | 0.132 |
| 16 | 0.000 | 0.005 | 0.017 | 0.035 | 0.053 | 0.072 | 0.087 | 0.101 | 0.112 | 0.121 | 0.128 |
| 17 | 0.000 | 0.005 | 0.016 | 0.033 | 0.052 | 0.069 | 0.085 | 0.098 | 0.109 | 0.118 | 0.125 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |


| 18 | 0.000 | 0.004 | 0.016 | 0.032 | 0.050 | 0.067 | 0.083 | 0.096 | 0.106 | 0.115 | 0.121 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19 | 0.000 | 0.004 | 0.015 | 0.031 | 0.048 | 0.065 | 0.080 | 0.093 | 0.103 | 0.112 | 0.118 |
| 20 | 0.000 | 0.004 | 0.014 | 0.029 | 0.047 | 0.063 | 0.078 | 0.090 | 0.100 | 0.108 | 0.115 |
| 21 | 0.000 | 0.004 | 0.013 | 0.028 | 0.045 | 0.061 | 0.075 | 0.088 | 0.098 | 0.105 | 0.111 |
| 22 | 0.000 | 0.003 | 0.013 | 0.027 | 0.043 | 0.059 | 0.073 | 0.085 | 0.095 | 0.102 | 0.108 |
| 23 | 0.000 | 0.003 | 0.012 | 0.026 | 0.042 | 0.057 | 0.071 | 0.083 | 0.092 | 0.100 | 0.105 |
| 24 | 0.000 | 0.003 | 0.011 | 0.025 | 0.040 | 0.055 | 0.069 | 0.080 | 0.089 | 0.097 | 0.102 |
| 25 | 0.000 | 0.003 | 0.011 | 0.024 | 0.039 | 0.053 | 0.067 | 0.078 | 0.087 | 0.094 | 0.100 |
| 26 | 0.000 | 0.002 | 0.010 | 0.023 | 0.037 | 0.052 | 0.064 | 0.075 | 0.084 | 0.091 | 0.097 |
| 27 | 0.000 | 0.002 | 0.010 | 0.022 | 0.036 | 0.050 | 0.062 | 0.073 | 0.082 | 0.089 | 0.094 |
| 28 | 0.000 | 0.002 | 0.009 | 0.021 | 0.034 | 0.048 | 0.060 | 0.071 | 0.080 | 0.086 | 0.091 |
| 29 | 0.000 | 0.002 | 0.009 | 0.020 | 0.033 | 0.046 | 0.059 | 0.069 | 0.077 | 0.084 | 0.089 |
| 20 | 0.000 | 0.002 | 0.008 | 0.019 | 0.032 | 0.045 | 0.057 | 0.067 | 0.075 | 0.082 | 0.086 |

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[^0]:    * The risk-free interest rate is regarded as the interest rate on U.S. Treasury bills of the same duration as the option.

[^1]:    * A put is said to be out of the money if the strike price of the put is less than the current stock price. It is at the money if the two are essentially equal, and it is in the money if the strike price is greater than the stock price.

[^2]:    * The New York Stock Exchange no longer trades options and transferred any options that had been traded exclusively there to the Chicago Board Options Exchange in 1997.

[^3]:    * The Philadelphia Stock Exchange, for example, does not permit GTC orders at prices set above the market. Any stop buy or stop-limit buy requests must be done on a daily basis.

[^4]:    *For reference purposes, I'll call this lower-strike LEAP put the insurance put.

